

1620 GENERAL PROGRAM LIBRARY

DOES (Disk Oriented Equation Solver)

5.0.037

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1620
Correction

5.0.037
February 8, 1966

Page 4 has been revised.

COMMON USERS GROUP PROGRAM REVIEW AND EVALUATION
(fill out in typewriter, ink or pencil)

Program No. _____

Date _____

Program Name: _____

1. Does the abstract adequately describe what the program is and what it does? Yes _____ No _____

Comment _____

2. Does the program do what the abstract says? Yes _____ No _____

Comment _____

3. Is the description clear, understandable, and adequate? Yes _____ No _____

Comment _____

4. Are the Operating Instructions understandable and in sufficient detail? Yes _____ No _____

Comment _____

Are the Sense Switch options adequately described (if applicable)? Yes _____ No _____

Are the mnemonic labels identified or sufficiently understandable? Yes _____ No _____

Comment _____

5. Does the source program compile satisfactorily (if applicable)? Yes _____ No _____

Comment _____

6. Does the object program run satisfactorily? Yes _____ No _____

Comment _____

7. Number of test cases run _____. Are any restrictions as to data, size, range, etc. covered adequately in description? Yes _____ No _____

Comment _____

8. Does the Program meet the minimal standards of COMMON? Yes _____ No _____

Comment _____

9. Were all necessary parts of the program received? Yes _____ No _____

Comment _____

10. Please list on the back any suggestions to improve the usefulness of the program.
These will be passed onto the author for his consideration.

Please return to:

Mr. Richard L. Pratt
Data Corporation
7500 Old Xenia Pike
Dayton, Ohio 45432

Your Name _____
Company _____

Address _____

Users Group Code _____

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1620 USERS GROUP LIBRARY
PROGRAM ABSTRACT

1. TITLE (If subroutine, state in Title): "DOES" (Disk Oriented Equation Solver)
Subject Classification: 5.0
2. Author; Organization: Mr. Robert Stephenson
University Computing Center of the University of Cincinnati
Date: 1/28/65 Users Group Membership Code: 3015
3. Direct Inquiries to Name: Dr. Carl F. Evert, Director
University of Cincinnati Phone: 475-2333
4. Description/Purpose: (5. Method; 6. Restriction/Range; When Applicable):
This program utilizes the 1311 Disk to extend the capacity
of the 1620 for the solution of simultaneous algebraic equations or
matrix inversion. 200 x 200 matrices may be inverted.

DOES
(Disk Oriented Equation Solver)

Author: Mr. Robert Stephenson
University Computing Center
University of Cincinnati

Date: 1/29/65

Membership Code: 3015

"Modifications or revisions to this program, as they occur, will be announced in the appropriate Catalog of Programs for IBM Data Processing Systems. When such an announcement occurs, users should order a complete new program from the Program Information Department."

7. Specifications (Check or fill in appropriate spaces):

- a. Storage used by program: 40K and 1311 Disk
- b. Equipment required by program: Card X; Magnetic Tape ; Number of Drives ; Paper Tape ; Disk File X; Number of Drives 1; TNS, TNF, MF X; Auto divide X; Indirect addressing X; Floating Point Hardware X; 1620 Model I X; Model II ; 1443 Printer ; Index Registers ; Binary Capabilities ; Other (specify)
Can program be used on lesser machine? Yes. Specify which requirements can be easily removed see "Additional Remarks."
- c. Programmed in: Fortran without Format ; Fortran with Format ; Fortran II ; Other Fortran (specify) ; SPS (specify assembler used) SPS-IID; Other (specify)
- d. Type of Program: Mainline, complete X; Subroutine ; If subroutine, for use with SPS (specify type of SPS) ; Fortran (specify type of Fortran) ; Other (specify)
8. Additional Remarks: Program could be used on a 20K machine with no difficulty
and with reassemble, it could be used on machines without the automatic
floating point feature.

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v

Deck Labelling Sheet

| <u>Deck</u> | <u>Name</u> |
|-------------|---------------------------|
| 1 | Source Deck (01010-13200) |
| 2 | Object Deck (1-68) |
| 3 | Sample Problem Input |
| 4 | Sample Problem Output |

PROGRAM WRITE-UP

- a) DOES (Disk Oriented Equation Solver)
- b) Date: 1/29/65
- c) Dr. Carl F. Evert, Director; University of Cincinnati;
475-2333; Membership Code - 3015
- d) Program Description

The technique used for this inversion is based on a process described by Sherman.¹

Sherman states: Given a matrix [A] differing from another matrix [a] only in the elements of one column, the inverse of [A], [B], can be found knowing the inverse of [a], [b], and the elements of the kth column of [A]. Where the kth column is the column of difference between [A] and [a]. The expressions for calculating the elements of [B] are:

$$B_{kj} = b_{kj}/z_k \quad j = 1, 2, 3, \dots, N.$$

$$z_n = \sum_{r=1}^N b_{nr} A_{rk} \quad n = 1, 2, 3, \dots, N.$$

$$B_{ij} = b_{ij} - z_i B_{kj} \quad i = 1, 2, \dots, k-1, k+1, \dots, N. \\ j = 1, 2, 3, \dots, N.$$

N = The size of the matrices.

B_{ab} = The element of [B] located in the ath row and the bth column.

b_{ab} = The element of [b] located in the ath row and the bth column.

A_{rk} = All the elements in the kth column of [A], since r=1, 2, 3, ... N.

Z_n = The matrix product of the nth row of [b] and the kth column of [A].

Consider the following example:

$$[A] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad [b] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad [A] = \begin{bmatrix} 7 & 0 & 0 \\ 5 & 1 & 0 \\ 8 & 0 & 1 \end{bmatrix}$$

k = 1 and N = 3.

¹ Sherman, Jack; "Adjustment of an Inverse Matrix Corresponding to a Change in the Elements of a Given Column," U.S. Department of Commerce, National Bureau of Standards, Applied Mathematics Series # 29.

$$z_1 = [1 & 0 & 0] \cdot \begin{bmatrix} 7 \\ 8 \\ 5 \end{bmatrix} = 7.$$

$$z_2 = [0 & 1 & 0] \cdot \begin{bmatrix} 7 \\ 5 \\ 8 \end{bmatrix} = 5.$$

$$z_3 = [0 & 0 & 1] \cdot \begin{bmatrix} 7 \\ 5 \\ 8 \end{bmatrix} = 8.$$

$$B_{11} = b_{11}/z_1 = 1/7. \quad B_{12} = b_{12}/z_1 = 0/7 = 0. \quad B_{13} = b_{13}/z_1 = 0/7 = 0.$$

$$B_{21} = b_{21} - z_2 B_{11} = 0 - 5(1/7) = -5/7.$$

$$B_{22} = b_{22} - z_2 B_{12} = 1 - 5(0) = 1.$$

$$B_{23} = b_{23} - z_2 B_{13} = 0 - 5(0) = 0.$$

$$B_{31} = b_{31} - z_3 B_{11} = 0 - 8(1/7) = -8/7.$$

$$B_{32} = b_{32} - z_3 B_{12} = 0 - 8(0) = 0.$$

$$B_{33} = b_{33} - z_3 B_{13} = 1 - 8(0) = 1.$$

$$[A]^{-1} = [B] = \begin{bmatrix} 1/7 & 0 & 0 \\ -5/7 & 1 & 0 \\ -8/7 & 0 & 1 \end{bmatrix}$$

The general inversion program starts by generating a $N \times N$ identity matrix and storing it on the disk. The matrix on the disk is the [b] matrix. The first column of data is read into memory. An inversion process is then performed letting [A] be a matrix different from an identity matrix only in the first column, and that column is the one just read. As the inversion is performed, the [B] matrix is stored on the disk replacing the identity matrix. A second column of data is read into memory and [A] matrix is now different from an identity matrix in the first two columns, however, it differs from a matrix [a], whose inverse is now on the disk, only in the second column. The [B] matrix from the previous inversion now becomes the [b] matrix for this inversion. This process continues until all the columns of data have been read, at that time the matrix on the disk is the desired inverse of the input matrix.

The common method of attack on problems of systems of simultaneous linear equations is to use a matrix inversion technique. The system

$$a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n = c_1$$

$$a_{21}x_1 + a_{22}x_2 + \dots + a_{2n}x_n = c_2$$

.....

$$a_{nn}x_1 + a_{n2}x_2 + \dots + a_{nn}x_n = c_n$$

can be represented in matrix form by

$$\begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \dots \\ x_n \end{bmatrix} = \begin{bmatrix} c_1 \\ c_2 \\ \dots \\ c_n \end{bmatrix}$$

If we call the coefficient matrix A, the variable or unknown matrix x and the constant matrix c, we have

$$AX = C.$$

If we premultiply both sides by A^{-1} , the inverse of A, we have

$$A^{-1}(AX) = A^{-1}C$$

or

$$(A^{-1}A)X = A^{-1}C$$

$$X = A^{-1}C$$

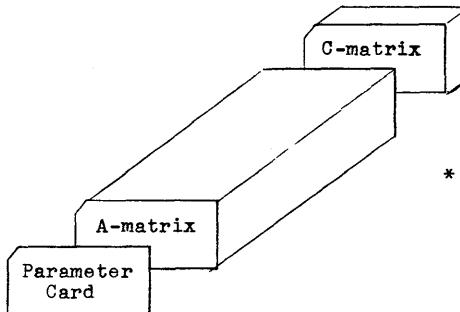
The problem is then to invert the Z matrix and multiply it into the C matrix.

e) Input/Output Formats

The first card contains 1 parameter, the number of equations, punched in the first four columns and right justified.*

The next set of cards is the A or coefficient matrix punched by columns. The format is like the Fortran format 5(E14.7,2X), but unlike Fortran no deviation is allowed. Each new row is to be started on a new card, and all numbers are to be normalized.

If desired, the program will compute the equation solutions. The C matrix is put on cards in the same manner as a column of the A matrix, and it follows the A matrix in input.



* WARNING: If this parameter is greater than 200 or is not right justified in the columns indicated, it is possible for the Monitor System to be destroyed.

Output Format

The incomplete and complete inverse are punched in the same format, 5(E14.7,2X), as the input. The complete inverse has headers between the rows, but the incomplete inverse does not.

The solutions are punched one to a card with the number and solution of each unknown.

f) Restrictions

This program is designed to handle up to 200 simultaneous equations using an IBM 1620 - 1311 system. The program was assembled on a 1620 with 40K storage, automatic floating point hardware, and indirect addressing using SPS-IID. It could be used on a 20K machine with no difficulty and with reassembly, it could be used on machines without the automatic floating point feature.

This program is compatible with Monitor I as it is issued from IBM. The first 20 cylinders of disk storage are used for the 200 equation problem, but for smaller problems, the cylinder usage can be computed by

$$\text{Number of Sectors} = \frac{(\text{Number of Equations})^2}{10}$$

and there are 200 sectors per cylinder.

g) Operating Instructions

1. Cold - Start Monitor I
2. Load Program and input cards into read stacker.
3. Ready Punch
4. Push reader start

Details

Switch Settings

At least one program switch must be on to get any output.

SWITCH 1 - On to make intermediate exit
SWITCH 2 - On to compute and punch equation solutions.
SWITCH 3 - On to restart after intermediate exit.
SWITCH 4 - On to punch completed inverse matrix.

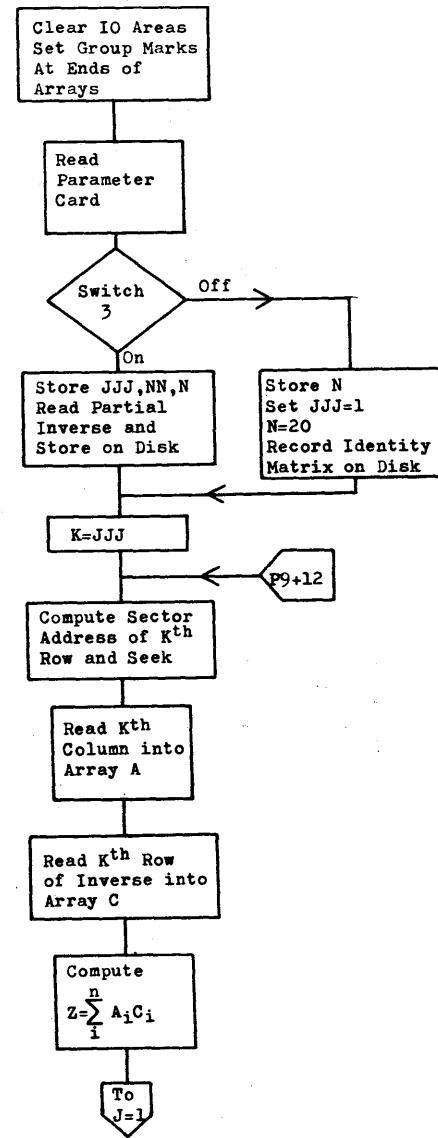
All Check Switches to STOP

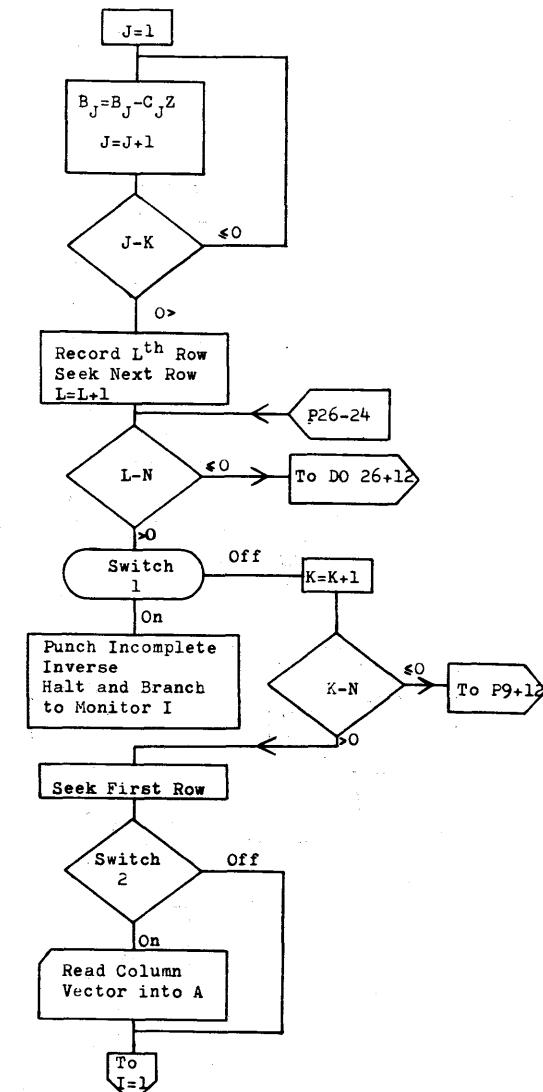
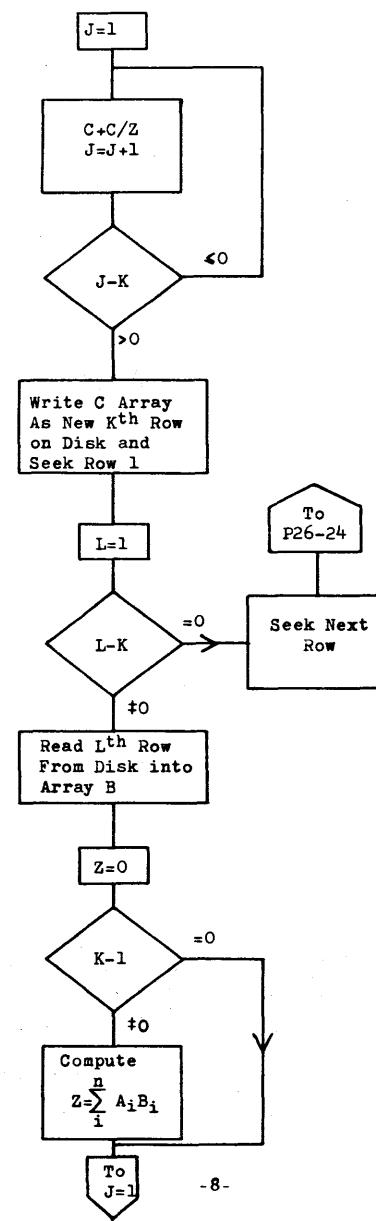
Intermediate Exit

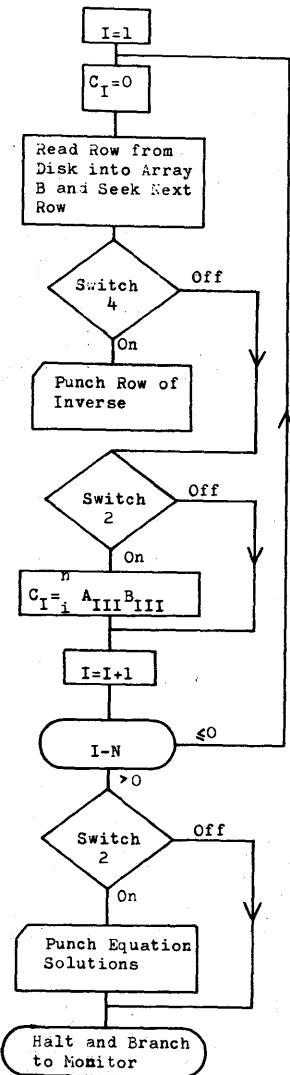
If desired, the program can be stopped during a run and the partially inverted matrix punched for restart later. To do this turn on Switch 1 at the desired stopping point.

To restart place the incomplete inverse deck in the reader followed by the part of the A matrix not already read by the program. If in doubt, the first card of the incomplete inverse should be printed. It contains 3 parameters, the number of equations, the next column to be read, and the number of sectors per column (always 20).

Flow Chart







01010*DISK ORIENTED EQUATION SOLVER
01020 START TFM *+18,I0-1,,INITIALIZATION

| | | |
|-------------|---|----------------------|
| 01030 | TDM | |
| 01040 | AM *-6,1 | 02402 16 02420 -5502 |
| 01050 | CM *-18,I0+158 | 02414 15 00000 00000 |
| 01060 | BNH *-36 | 02426 11 02420 -0001 |
| 01061 | TFM *+18,A-9 | 02438 14 02420 -5661 |
| 01062 | TDM | 02450 47 02414 01100 |
| 01063 | AM *-6,1 | 02462 16 02480 -5688 |
| 01064 | CM *-18,C+1990 | 02474 15 00000 00000 |
| 01065 | BNH *-36 | 02486 11 02480 -0001 |
| 01066 | TD B-11,GM | 02498 14 02480 J1691 |
| 01067 | TD C-11,GM | 02510 47 02474 01100 |
| 01068 | TD ONE-11,GM | 02522 25 07688 05687 |
| 01070 | RNCD I0-1,,,READ PARAMETER CARD | 02534 25 09690 05687 |
| 01080 | SF IO-1 | 02546 25 11692 05687 |
| 01090 | BNC3 P1 | 02558 36 05502 00500 |
| 01100 P450 | SF IO+4,,,CONTINUATION OF OLD JOB | 02570 32 05502 00000 |
| 01110 | SF IO+7 | 02582 47 02806 00300 |
| 01120 | TF JJJ,IO+2,,, JJJ IS COLUMN TO BE READ NEXT | 02594 32 05507 00000 |
| 01125 | TFM JJJ-3,0,10 | 02606 32 05510 00000 |
| 01130 | TFM NN,20,9,, NN IS SECTOR COUNT | 02618 26 05666 05505 |
| 01140 | TF N,IO+10 ,, N IS NUMBER OF ROWS AND COLUMNS IN MATRIX | 02630 16 05663 000-0 |
| 01150 | TFM MAT1,0 | 02642 16 05494 00-20 |
| 01160 | SK DCF | 02654 26 05671 05513 |
| 01170 D0475 | TFM MM1,,, READ PARTIAL INVERSE AND | 02666 16 05491 -0000 |
| 01180 | BTM READ,B,, RECORD ON DISK | 02678 34 05486 00701 |
| 01190 | TFM CORE,B-9 | 02690 16 05676 -0001 |
| 01200 | WDGN DCF | 02702 17 11858 -7699 |
| 01205 | A MAT1,NN | 02714 16 05499 -7690 |
| 01206 | SK DCF | 02726 38 05486 00700 |
| 01210 | AM MM,1 | 02738 21 05491 05494 |
| 01220 | C MM,N | 02750 34 05486 00701 |
| 01230 P475 | RNH D0475+12 | 02762 11 05676 -0001 |
| 01240 | B7 P9 | 02774 24 05676 05671 |
| 01250 P1 | TF N,IO+2,,,START OF NEW JOB | 02786 47 02702 01100 |
| 02020 | TFM NN,20,9 | 02798 49 03150 00000 |
| 02030 | TFM JJJ,1 | 02806 26 05671 05505 |
| 02040 | TFM MAT1,0 | 02818 16 05494 00-20 |
| 02045 | TFM CORE,B-9 | 02830 16 05666 -0001 |
| 02050 | SK DCF | 02842 16 05491 -0000 |
| 02060 | TFL B,ONE,, RECORD IDENTITY MATRIX ON DISK | 02854 16 05499 -7690 |
| 02070 | TFM L,2 | 02866 34 05486 00701 |
| 02080 | MM L,10 | 02878 06 07699 11703 |
| 02090 | SF 95 | 02890 16 05686 -0002 |
| | | 02902 13 05686 -0010 |
| | | 02914 32 00095 00000 |

| | | | | | | |
|-------|------|---------------------------------------|-------|----|-------|-------|
| 02100 | AM | 99,B-10 | 02926 | 11 | 00099 | -7689 |
| 02110 | TFL | -99,ZERO | 02938 | 06 | 0009R | 11713 |
| 02120 | AM | L+1 | 02950 | 11 | 05686 | -0001 |
| 02130 | C | L+N | 02962 | 24 | 05686 | 05671 |
| 02140 | BNH | *-72 | 02974 | 47 | 02902 | 01100 |
| 02150 | TFM | M+1 | 02986 | 16 | 05681 | -0001 |
| 02160 | B7 | P6 | 02998 | 49 | 03078 | 00000 |
| 02170 | MM | M+10 | 03006 | 13 | 05681 | -0010 |
| 02180 | SF | 95 | 03018 | 32 | 00095 | 00000 |
| 02190 | AM | 99,B-10 | 03030 | 11 | 00099 | -7689 |
| 02200 | TFL | -99,ONE | 03042 | 06 | 0009R | 11703 |
| 02210 | SM | 99,10 | 03054 | 12 | 00099 | -0010 |
| 02220 | TFL | -99,ZERO | 03066 | 06 | 0009R | 11713 |
| 02230 | P6 | WDGN DCF | 03078 | 38 | 05486 | 00700 |
| 02240 | A | MAT1,NN | 03090 | 21 | 05491 | 05494 |
| 02245 | SK | DCF | 03102 | 34 | 05486 | 00701 |
| 02250 | AM | M,1 | 03114 | 11 | 05681 | -0001 |
| 02260 | C | M+N | 03126 | 24 | 05681 | 05671 |
| 02270 | BNH | *-132 | 03138 | 47 | 03006 | 01100 |
| 02275 | P9 | TF K,JJJ,, BEGINNING OF MAIN LOOP | 03150 | 26 | 11718 | 05666 |
| 02280 | TF | FAC,K,, COMPUTE SECTOR ADDRESS OF | 03162 | 26 | 11728 | 11718 |
| 02290 | SM | FAC,1,, K TH ROW OF INVERSE | 03174 | 12 | 11728 | -0001 |
| 02300 | M | FAC,NN | 03186 | 23 | 11728 | 05494 |
| 03010 | SF | 97 | 03198 | 32 | 00097 | 00000 |
| 03030 | TF | MAT1,99 | 03210 | 26 | 05491 | 00099 |
| 03040 | SK | DCF | 03222 | 34 | 05486 | 00701 |
| 03050 | BTM | READ,A,, READ K TH COLUMN OF MATRIX | 03234 | 17 | 11858 | -5697 |
| 03060 | TFM | CORE,C-9 | 03246 | 16 | 05499 | -9692 |
| 03070 | RDGN | DCF | 03258 | 36 | 05486 | 00700 |
| 03090 | TFL | Z,ZERO | 03270 | 06 | 11738 | 11713 |
| 03100 | D013 | TFM MM,1,, COMPUTE Z | 03282 | 16 | 05676 | -0001 |
| 03110 | MM | MM,10 | 03294 | 13 | 05676 | -0010 |
| 03120 | SF | 95 | 03306 | 32 | 00095 | 00000 |
| 03130 | AM | 99,C-10 | 03318 | 11 | 00099 | -9691 |
| 03140 | TFL | FAC,-99 | 03330 | 06 | 11728 | 0009R |
| 03150 | AM | 99,A-C | 03342 | 11 | 00099 | -400M |
| 03170 | FMUL | FAC,-99 | 03354 | 03 | 11728 | 0009R |
| 03180 | FADD | Z,FAC | 03366 | 01 | 11738 | 11728 |
| 03190 | AM | MM,1 | 03378 | 11 | 05676 | -0001 |
| 03200 | C | MM,K | 03390 | 24 | 05676 | 11718 |
| 03210 | P13 | BNH D013+12 | 03402 | 47 | 03294 | 01100 |
| 03220 | D014 | TFM J+1,, DIVIDE ELEMENTS OF K TH ROW | 03414 | 16 | 11748 | -0001 |
| 03230 | MM | J+10,, OF INVERSE BY Z | 03426 | 13 | 11748 | -0010 |
| 03240 | SF | 95 | 03438 | 32 | 00095 | 00000 |
| 03250 | AM | 99,C-10 | 03450 | 11 | 00099 | -9691 |
| 03260 | FDIV | -99,Z | 03462 | 09 | 0009R | 11738 |

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| | | | | | | |
|-------|------|---|-------|----|-------|-------|
| 03270 | AM | J+1 | 03474 | 11 | 11748 | -0001 |
| 03280 | C | J+K | 03486 | 24 | 11748 | 11718 |
| 03290 | P14 | BNH D014+12 | 03498 | 47 | 03426 | 01100 |
| 03300 | TFM | CORE,C-9,,RECORD NEW K TH ROW ON DISK | 03510 | 16 | 05499 | -9692 |
| 04010 | WDGN | DCF | 03522 | 38 | 05486 | 00700 |
| 04020 | TFM | MAT1,0 | 03534 | 16 | 05491 | -0000 |
| 04030 | SK | DCF | 03546 | 34 | 05486 | 00701 |
| 04040 | D026 | TFM L,1,, LOOP FOR ADJUSTMENT OF ENTIRE | 03558 | 16 | 05686 | -0001 |
| 04050 | C | L,K,, MATRIX | 03570 | 24 | 05686 | 11718 |
| 04060 | BNE | P20 | 03582 | 47 | 03626 | 01200 |
| 04070 | P17 | A MAT1,NN | 03594 | 21 | 05491 | 05494 |
| 04080 | SK | DCF | 03606 | 34 | 05486 | 00701 |
| 04090 | B7 | P26-24 | 03618 | 49 | 04094 | 00000 |
| 04100 | P20 | CORE,B-9 | 03626 | 16 | 05499 | -7690 |
| 04110 | RDGN | DCF | 03638 | 36 | 05486 | 00700 |
| 04130 | TFL | Z,ZERO | 03650 | 06 | 11738 | 11713 |
| 04140 | CM | K,1 | 03662 | 14 | 11718 | -0001 |
| 04150 | BZ | P23 | 03674 | 46 | 03842 | 01200 |
| 04160 | P21 | MM,1,, COMPUTE Z | 03686 | 16 | 05676 | -0001 |
| 04170 | MM | MM,10 | 03698 | 13 | 05676 | -0010 |
| 04180 | SF | 95 | 03710 | 32 | 00095 | 00000 |
| 04190 | AM | 99,R-10 | 03722 | 11 | 00099 | -7689 |
| 04200 | TFL | FAC,-99 | 03734 | 06 | 11728 | 0009R |
| 04210 | AM | 99,A-B | 03746 | 11 | 00099 | -200K |
| 04230 | FMUL | FAC,-99 | 03758 | 03 | 11728 | 0009R |
| 04240 | FADD | Z,FAC | 03770 | 01 | 11738 | 11728 |
| 04250 | AM | MM,1 | 03782 | 11 | 05676 | -0001 |
| 04260 | C | MM,K | 03794 | 24 | 05676 | 11718 |
| 04270 | P22 | BNH P21+12 | 03806 | 47 | 03698 | 01100 |
| 04280 | C | L,K | 03818 | 24 | 05686 | 11718 |
| 04290 | RNH | P24 | 03830 | 47 | 03890 | 01100 |
| 04300 | P23 | MM,L,10 | 03842 | 13 | 05686 | -0010 |
| 05010 | SF | 95 | 03854 | 32 | 00095 | 00000 |
| 05020 | AM | 99,A-10 | 03866 | 11 | 00099 | -5687 |
| 05030 | FADD | Z,-99 | 03878 | 01 | 11738 | 0009R |
| 05040 | P24 | TFM J+1,, ADJUST J TH ROW | 03890 | 16 | 11748 | -0001 |
| 05050 | MM | J,10 | 03902 | 13 | 11748 | -0010 |
| 05060 | SF | 95 | 03914 | 32 | 00095 | 00000 |
| 05070 | AM | 99,C-10 | 03926 | 11 | 00099 | -9691 |
| 05080 | TFL | FAC,-99 | 03938 | 06 | 11728 | 0009R |
| 05090 | FMUL | FAC,Z | 03950 | 03 | 11728 | 11738 |
| 05100 | MM | J,10 | 03962 | 13 | 11748 | -0010 |
| 05110 | SF | 95 | 03974 | 32 | 00095 | 00000 |
| 05120 | AM | 99,R-10 | 03986 | 11 | 00099 | -7689 |
| 05130 | FSUB | -99,FAC | 03998 | 02 | 0009R | 11728 |
| 05140 | AM | J+1 | 04010 | 11 | 11748 | -0001 |

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| | | | | | | |
|------------|------|------------------------------------|-------|----|-------|-------|
| 05150 | C | J,K | 04022 | 24 | 11748 | 11718 |
| 05160 P25 | BNH | P24+12 | 04034 | 47 | 03902 | 01100 |
| 05170 | TFM | CORE,B-9,,,RECORD J TH ROW | 04046 | 16 | 05499 | -7690 |
| 05180 | WDGN | DCF | 04058 | 38 | 05486 | 00700 |
| 05185 | A | MAT1,NN | 04070 | 21 | 05491 | 05494 |
| | SK | DCF | 04082 | 34 | 05486 | 00701 |
| 05190 | AM | L+1 | 04094 | 11 | 05686 | -0001 |
| 05200 | C | L,N | 04106 | 24 | 05686 | 05671 |
| 05210 P26 | BNH | D026+12 | 04118 | 47 | 03570 | 01100 |
| 05220 | BNC1 | P100-24 | 04130 | 47 | 04566 | 00100 |
| 05230 P30 | TFM | MAT1,0,,, PUNCH INCOMPLETE INVERSE | 04142 | 16 | 05491 | -0000 |
| 05240 | SK | DCF | 04154 | 34 | 05486 | 00701 |
| 05250 | TF | IM,K | 04166 | 26 | 11753 | 11718 |
| 05260 | AM | IM,1 | 04178 | 11 | 11753 | -0001 |
| 05261 | BTM | PUNCH+12,400 | 04190 | 17 | 12326 | -0400 |
| 05270 | BT | KDONNA,IM,,,PUNCH IM,NN,N | 04202 | 27 | 12768 | 11753 |
| 05280 | TF | I0+6,WORD+6 | 04214 | 26 | 05509 | 11761 |
| 05290 | BT | KDONNA,NN | 04226 | 27 | 12768 | 05494 |
| 05300 | TF | I0+14,WORD+6 | 04238 | 26 | 05517 | 11761 |
| 06010 | BT | KDONNA,N | 04250 | 27 | 12768 | 05671 |
| 06020 | TF | I0+22,WORD+6 | 04262 | 26 | 05525 | 11761 |
| 06030 | BTM | PUNCH | 04274 | 17 | 12314 | -0000 |
| 06040 D032 | TFM | J,1 | 04286 | 16 | 11748 | -0001 |
| 06050 | TFM | CORE,B-9 | 04298 | 16 | 05499 | -7690 |
| 06060 | RDGN | DCF | 04310 | 36 | 05486 | 00700 |
| 06070 | A | MAT1,NN | 04322 | 21 | 05491 | 05494 |
| | SK | DCF | 04334 | 34 | 05486 | 00701 |
| 06080 | TFM | L+1 | 04346 | 16 | 05686 | -0001 |
| 06090 | TFM | *+35,B | 04358 | 16 | 04393 | -7699 |
| 06100 | TFM | *+30,I0+26 | 04370 | 16 | 04400 | -5529 |
| 06110 | BTFL | DONNA | 04382 | 07 | 12408 | 00000 |
| 06120 | TF | ,WORD+26 | 04394 | 26 | 00000 | 11781 |
| 06130 | AM | L,1 | 04406 | 11 | 05686 | -0001 |
| 06140 | AM | *-25,10 | 04418 | 11 | 04393 | -0010 |
| 06150 | AM | *-30,32 | 04430 | 11 | 04400 | -0032 |
| 06160 | C | L,N | 04442 | 24 | 05686 | 05671 |
| 06170 | BH | LC | 04454 | 46 | 04510 | 01100 |
| 06180 | CM | *-66,I0+158 | 04466 | 14 | 04400 | -5661 |
| 06190 | BNH | *-96 | 04478 | 47 | 04382 | 01100 |
| 06200 | BTM | PUNCH | 04490 | 17 | 12314 | -0000 |
| 06210 | B7 | *-132 | 04502 | 49 | 04370 | 00000 |
| 06220 LC | BTM | PUNCH | 04510 | 17 | 12314 | -0000 |
| 06230 | AM | J,1 | 04522 | 11 | 11748 | -0001 |
| 06240 | C | J,N | 04534 | 24 | 11748 | 05671 |
| 06250 P32 | BNH | D032+12 | 04546 | 47 | 04298 | 01100 |
| 06260 | B7 | P210 | 04558 | 49 | 05462 | 00000 |

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|------------|------|--|-------|----|-------|-------|
| 06270 | AM | K,1 | 04566 | 11 | 11718 | -0001 |
| 06280 | C | K,N | 04578 | 24 | 11718 | 05671 |
| 06290 P100 | BNH | P9+12,,, END OF MAIN LOOP | 04590 | 47 | 03162 | 01100 |
| 06300 | TFM | MAT1,0 | 04602 | 16 | 05491 | -0000 |
| 07010 | SK | DCF | 04614 | 34 | 05486 | 00701 |
| 07020 | BNC2 | P110 | 04626 | 47 | 04650 | 00200 |
| 07030 P105 | BTM | READ,A,,, READ COLUMN VECTOR FOR EQUATION SOLUTION | 04638 | 17 | 11858 | -5697 |
| 07040 P110 | TFM | J,1 | 04650 | 16 | 12967 | -0001 |
| 07050 | MM | I+10 | 04662 | 13 | 12967 | -0010 |
| 07060 | SF | 95 | 04674 | 32 | 00095 | 00000 |
| 07070 | AM | 99,C-10 | 04686 | 11 | 00099 | -9691 |
| 07080 | TFL | -99,ZERO | 04698 | 06 | 0009R | 11713 |
| 07090 | TFM | CORE,B-9 | 04710 | 16 | 05499 | -7690 |
| 07100 | RDGN | DCF | 04722 | 36 | 05486 | 00700 |
| 07110 | A | MAT1,NN | 04734 | 21 | 05491 | 05494 |
| | SK | DCF | 04746 | 34 | 05486 | 00701 |
| 07120 | BNC4 | P601 | 04758 | 47 | 05006 | 00400 |
| 07130 P600 | BT | KDONNA,I,,,PUNCH ROW OF INVERSE | 04770 | 27 | 12768 | 12967 |
| 07135 | BTM | PUNCH+12,400 | 04782 | 17 | 12326 | -0400 |
| 07140 | TF | I0+76,LAB1+6 | 04794 | 26 | 05579 | 11809 |
| 07150 | TF | I0+84,WORD+6 | 04806 | 26 | 05587 | 11761 |
| 07160 | BTM | PUNCH | 04818 | 17 | 12314 | -0000 |
| 07170 | TFM | L,1 | 04830 | 16 | 05686 | -0001 |
| 07180 | TFM | *+35,B | 04842 | 16 | 04877 | -7699 |
| 07190 | TFM | *+30,I0+26 | 04854 | 16 | 04884 | -5529 |
| 07200 | BTFL | DONNA | 04866 | 07 | 12408 | 00000 |
| 07210 | TF | ,WORD+26 | 04878 | 26 | 00000 | 11781 |
| 07220 | AM | L,1 | 04890 | 11 | 05686 | -0001 |
| 07230 | AM | *-25,10 | 04902 | 11 | 04877 | -0010 |
| 07240 | AM | *-30,32 | 04914 | 11 | 04884 | -0032 |
| 07250 | C | L,N | 04926 | 24 | 05686 | 05671 |
| 07260 | BH | LC1 | 04938 | 46 | 04994 | 01100 |
| 07270 | CM | *-66,I0+158 | 04950 | 14 | 04884 | -5661 |
| 07280 | BNH | *-96 | 04962 | 47 | 04866 | 01100 |
| 07290 | BTM | PUNCH | 04974 | 17 | 12314 | -0000 |
| 07300 | B7 | *-132 | 04986 | 49 | 04854 | 00000 |
| 08010 LC1 | BTM | PUNCH | 04994 | 17 | 12314 | -0000 |
| 08020 P601 | BNC2 | P200-24 | 05006 | 47 | 05186 | 00200 |
| 08030 P120 | TFM | III,1,,, COMPUTE EQUATION SOLUTIONS | 05018 | 16 | 11819 | -0001 |
| 08040 | MM | III,10 | 05030 | 13 | 11819 | -0010 |
| 08050 | SF | 95 | 05042 | 32 | 00095 | 00000 |
| 08060 | AM | 99,A-10 | 05054 | 11 | 00099 | -5687 |
| 08070 | TFL | FAC,-99 | 05066 | 06 | 11728 | 0009R |
| 08080 | AM | 99,B-A | 05078 | 11 | 00099 | -2002 |
| 08100 | FMUL | FAC,-99 | 05090 | 03 | 11728 | 0009R |

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|-------------|------|--------------------------------|-------|-------|-------|-------|
| 08110 | MM | I,10 | 05102 | 13 | 12967 | -0010 |
| 08120 | SF | 95 | 05114 | 32 | 00095 | 00000 |
| 08130 | AM | 99,C-10 | 05126 | 11 | 00099 | -9691 |
| 08140 | FADD | -99,FAC | 05138 | 01 | 0009R | 11728 |
| 08150 | AM | III+1 | 05150 | 11 | 11819 | -0001 |
| 08160 | C | III,N | 05162 | 24 | 11819 | 05671 |
| 08140 P140 | BNH | P120+12 | 05174 | 47 | 05030 | 01100 |
| 08180 | AM | I,1 | 05186 | 11 | 12967 | -0001 |
| 08190 | C | I,N | 05198 | 24 | 12967 | 05671 |
| 08200 P200 | BNH | P110+12 | 05210 | 47 | 04662 | 01100 |
| 08210 | BNC2 | P210 | 05222 | 47 | 05462 | 00200 |
| 08211 | BTM | PUNCH+12,400 | 05234 | 17 | 12326 | -0400 |
| 08220 P205 | WACD | IO,,, PUNCH EQUATION SOLUTIONS | 05246 | 39 | 05503 | 00400 |
| 08230 | WACD | IO | 05258 | 39 | 05503 | 00400 |
| 08240 | TF | IO+30,LAB2+14 | 05270 | 26 | 05533 | 11835 |
| 08250 | TF | IO+88,LAB3+14 | 05282 | 26 | 05591 | 11851 |
| 08270 | BTM | PUNCH | 05294 | 17 | 12314 | -0000 |
| 08280 | WACD | IO | 05306 | 39 | 05503 | 00400 |
| 08290 D0209 | TFM | J,1 | 05318 | 16 | 11748 | -0001 |
| 09060 | BT | KDONNA,J | 05330 | 27 | 12768 | 11748 |
| 09070 | TF | IO+24,WORD+6 | 05342 | 26 | 05527 | 11761 |
| 09080 | MM | J,10 | 05354 | 13 | 11748 | -0010 |
| 09090 | SF | 95 | 05366 | 32 | 00095 | 00000 |
| 09100 | AM | 99,C-10 | 05378 | 11 | 00099 | -9691 |
| 09110 | BTFL | DONNA,-99 | 05390 | 07 | 12408 | 0009R |
| 09120 | TF | IO+94,WORD+26 | 05402 | 26 | 05597 | 11781 |
| 09180 | BTM | PUNCH | 05414 | 17 | 12314 | -0000 |
| 09190 | AM | J,1 | 05426 | 11 | 11748 | -0001 |
| 09200 | C | J,N | 05438 | 24 | 11748 | 05671 |
| 09210 P209 | BNH | D0209+12 | 05450 | 47 | 05330 | 01100 |
| 09220 P210 | H | | 05462 | 48 | 00000 | 00000 |
| 09225 | B | 796 | 05474 | 49 | 00796 | 00000 |
| 09230 DCF | DC | 1,1 | 05486 | 00001 | | |
| 09240 MATI | DC | 5,0 | 05491 | 00005 | | |
| 09250 NN | DC | 3,0 | 05494 | 00003 | | |
| 09260 CORE | DC | 5,0 | 05499 | 00005 | | |
| 09261 | DC | 1,- | 05500 | 00001 | | |
| 09270 IO | DAS | 80 | 05503 | 00160 | | |
| 09280 JJJ | DS | 5 | 05666 | 00005 | | |
| 09290 N | DS | 5 | 05671 | 00005 | | |
| 09300 MM | DS | 5 | 05676 | 00005 | | |
| 10010 M | DS | 5 | 05681 | 00005 | | |
| 10020 L | DS | 5 | 05686 | 00005 | | |
| 10021 GM | DGM | | 05687 | 00001 | | |
| 10030 A | DSR | 10,200 | 05697 | 02000 | | |
| 10031 | DS | 2 | 07689 | 00002 | | |

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|------------|------|-------------------------------|-------|----------------|--|--|
| 10040 R | DSB | 10,200 | 07699 | 02000 | | |
| 10041 | DS | 2 | 09691 | 00002 | | |
| 10050 C | DSB | 10,200 | 09701 | 02000 | | |
| 10051 | DS | 2 | 11693 | 00002 | | |
| 10060 | DC | 8,10000000 | 11701 | 00008 | | |
| 10070 ONE | DC | 2,1 | 11703 | 00002 | | |
| 10080 | DC | 8,0 | 11711 | 00008 | | |
| 10090 ZERO | DC | 2,-99 | 11713 | 00002 | | |
| 10100 K | DS | 5 | 11718 | 00005 | | |
| 10110 FAC | DS | 10 | 11728 | 00010 | | |
| 10120 Z | DS | 10 | 11738 | 00010 | | |
| 10130 J | DS | 10 | 11748 | 00010 | | |
| 10140 IM | DS | 5 | 11753 | 00005 | | |
| 10150 WORD | DAS | 24 | 11755 | 00048 | | |
| 10160 LAB1 | DAC | 4,ROW, | 11803 | 00008 | | |
| 10170 JJ | DS | 5 | 11814 | 00005 | | |
| 10180 III | DS | 5 | 11819 | 00005 | | |
| 10190 LAB2 | DAC | 8,VARIABLE | 11821 | 00016 | | |
| 10200 LAB3 | DAC | 8,SOLUTION | 11837 | 00016 | | |
| 10220 | DORG | *+6 | 11857 | | | |
| 10230 READ | TFM | L,1,,SUBROUTINE TO READ ARRAY | 11858 | 16 05686 -0001 | | |
| 10231 | RACD | IO | 11870 | 37 05503 00500 | | |
| 10240 | TFM | IN,IO+26 | 11882 | 16 12952 -5529 | | |
| 10250 | TFM | LAST+6,*+20 | 11894 | 16 12312 J1914 | | |
| 10260 | B7 | EDIT | 11906 | 49 12030 00000 | | |
| 10270 | TFL | READ-1,WORD+8,6 | 11914 | 06 1185P 11763 | | |
| 10280 | AM | L,1 | 11926 | 11 05686 -0001 | | |
| 10290 | AM | READ-1,10 | 11938 | 11 11857 -0010 | | |
| 10300 | AM | IN,58 | 11950 | 11 12952 -0058 | | |
| 11010 | C | L,N | 11962 | 24 05686 05671 | | |
| 11020 | BNH | *+24 | 11974 | 47 11998 01100 | | |
| 11030 | BB | | 11986 | 42 00000 00000 | | |
| 11040 | CM | IN,10+158 | 11998 | 14 12952 -5661 | | |
| 11050 | BNH | READ+36 | 12010 | 47 11894 01100 | | |
| 11051 | B7 | READ+12 | 12022 | 49 11870 00000 | | |
| 11060 EDIT | TFL | WORD+8,ZFROS | 12030 | 06 11763 12962 | | |
| 11070 | SF | WORD+7 | 12042 | 32 11762 00000 | | |
| 11080 | TNS | -IN,WORD+8 | 12054 | 72 1295K 11763 | | |
| 11090 | SM | IN,5 | 12066 | 12 12952 -0005 | | |
| 11100 | SF | -IN | 12078 | 32 1295K 00000 | | |
| 11110 | AM | IN,1 | 12090 | 11 12952 -0001 | | |
| 11120 | CM | -IN,20,10 | 12102 | 14 1295K 000KQ | | |
| 11130 | BNE | *+24 | 12114 | 47 12138 01200 | | |
| 11140 | SF | WORD+8 | 12126 | 32 11763 00000 | | |

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| | | | | | | | |
|-------|--------|-----------------|-------------|-------|----|-------|-------|
| 11150 | SM | IN,4 | | 12138 | 12 | 12952 | -0004 |
| 11160 | SF | WORD | | 12150 | 32 | 11755 | 00000 |
| 11170 | TNS | -IN,WORD+6 | | 12162 | 72 | 1295K | 11761 |
| 11180 | CF | WORD | | 12174 | 33 | 11755 | 00000 |
| 11190 | SM | IN,16 | | 12186 | 12 | 12952 | -0016 |
| 11200 | TD | WORD+1,-IN | | 12198 | 25 | 11754 | 1295K |
| 11210 | SF | WORD-1 | | 12210 | 32 | 11754 | 00000 |
| 11220 | SM | IN,3 | | 12222 | 12 | 12952 | -0003 |
| 11230 | SF | -IN | | 12234 | 32 | 1295K | 00000 |
| 11240 | AM | IN,1 | | 12246 | 11 | 12952 | -0001 |
| 11250 | CM | -IN,20,10 | | 12258 | 14 | 1295K | 000K0 |
| 11260 | BNZ | *+24 | | 12270 | 47 | 12294 | 01200 |
| 11270 | SF | WORD+6 | | 12282 | 32 | 11761 | 00000 |
| 11271 | AM | WORD+8,1,10 | | 12294 | 11 | 11763 | 000-1 |
| 11280 | LAST | B7 | | 12306 | 49 | 00000 | 00000 |
| 11290 | PUNCH | WACD IO | | 12314 | 39 | 05503 | 00400 |
| 11300 | TFM | *+18,IO-1 | | 12326 | 16 | 12344 | -5502 |
| 12010 | TDM | | | 12338 | 15 | 00000 | 00000 |
| 12020 | AM | *-6,1 | | 12350 | 11 | 12344 | -0001 |
| 12030 | CM | *-18,10+158 | | 12362 | 14 | 12344 | -5661 |
| 12040 | BNH | *-36 | | 12374 | 47 | 12338 | 01100 |
| 12050 | BB | | | 12386 | 42 | 00000 | 00000 |
| 12060 | DORG | *+10 | | 12407 | | | |
| 12070 | DONNA | TFM | *+30,WORD-2 | 12408 | 16 | 12438 | J1753 |
| 12080 | AM | *+18,1 | | 12420 | 11 | 12438 | -0001 |
| 12090 | TDM | | | 12432 | 15 | 00000 | 00000 |
| 12100 | CM | *-6,WORD+46 | | 12444 | 14 | 12438 | J1801 |
| 12110 | BL | *-36 | | 12456 | 47 | 12420 | 01300 |
| 12111 | CM | DONNA-1,-99,10 | | 12468 | 14 | 12407 | 000RR |
| 12112 | BE | *+24 | | 12480 | 46 | 12504 | 01200 |
| 12113 | SM | DONNA-1,1,10 | | 12492 | 12 | 12407 | 000-1 |
| 12114 | TFM | WORD+22,10,10 | | 12504 | 16 | 11777 | 000J0 |
| 12120 | BNF | *+24,DONNA-1 | | 12516 | 44 | 12540 | 12407 |
| 12130 | TFM | WORD+22,20,10 | | 12528 | 16 | 11777 | 000K0 |
| 12131 | CF | WORD+21 | | 12540 | 33 | 11776 | 00000 |
| 12140 | CF | DONNA-1 | | 12552 | 33 | 12407 | 00000 |
| 12141 | TFM | WORD+20,45,10 | | 12564 | 16 | 11775 | 000M5 |
| 12142 | CF | WORD+19 | | 12576 | 33 | 11774 | 00000 |
| 12150 | TNF | WORD+26,DONNA-1 | | 12588 | 73 | 11781 | 12407 |
| 12151 | CF | WORD+23 | | 12600 | 33 | 11778 | 00000 |
| 12160 | SF | DONNA-9 | | 12612 | 32 | 12399 | 00000 |
| 12170 | BNF | *+36,DONNA-3 | | 12624 | 44 | 12660 | 12405 |
| 12180 | TFM | WORD,20,10 | | 12636 | 16 | 11755 | 000K0 |
| 12190 | CF | DONNA-3 | | 12648 | 33 | 12405 | 00000 |
| 12191 | SF | WORD-1 | | 12660 | 32 | 11754 | 00000 |
| | | | 18 | | | | |
| 12200 | TNF | WORD+18,DONNA-3 | | 12672 | 73 | 11773 | 12405 |
| 12201 | CF | WORD+5 | | 12684 | 33 | 11760 | 00000 |
| 12210 | TFM | WORD+4,3,10 | | 12696 | 16 | 11759 | 000-3 |
| 12211 | CF | WORD+3 | | 12708 | 33 | 11758 | 00000 |
| 12220 | TD | WORD+2,DONNA-10 | | 12720 | 25 | 11757 | 12398 |
| 12230 | TDM | WORD+1,7 | | 12732 | 15 | 11756 | 00007 |
| 12235 | CF | WORD+2 | | 12744 | 33 | 11757 | 00000 |
| 12240 | BB | | | 12756 | 42 | 00000 | 00000 |
| 12250 | KDONNA | SF | KDONNA-4 | 12768 | 32 | 12764 | 00000 |
| 12260 | TFM | *+18,WORD-1 | | 12780 | 16 | 12798 | J1754 |
| 12270 | TDM | | | 12792 | 15 | 00000 | 00000 |
| 12280 | AM | *-6,1 | | 12804 | 11 | 12798 | -0001 |
| 12290 | CM | *-18,WORD+46 | | 12816 | 14 | 12798 | J1801 |
| 12300 | BNH | *-36 | | 12828 | 47 | 12792 | 01100 |
| 13010 | TFM | IN,KDONNA-4 | | 12840 | 16 | 12952 | J2764 |
| 13020 | BD | *+48,-IN | | 12852 | 43 | 12900 | 1295K |
| 13030 | AM | IN,1 | | 12864 | 11 | 12952 | -0001 |
| 13040 | CM | IN,KDONNA-3 | | 12876 | 14 | 12952 | J2765 |
| 13050 | BNH | *-36 | | 12888 | 47 | 12852 | 01100 |
| 13060 | SF | -IN | | 12900 | 32 | 1295K | 00000 |
| 13070 | TNF | WORD+6,KDONNA-1 | | 12912 | 73 | 11761 | 12767 |
| 13075 | SF | WORD-1 | | 12924 | 32 | 11754 | 00000 |
| 13080 | BB | | | 12936 | 42 | 00000 | 00000 |
| 13090 | IN | DS | 5 | 12952 | | | |
| 13100 | ZEROS | DC | 10.0 | 12962 | | | |
| 13101 | I | DS | 5 | 12967 | | | |
| 13200 | DEND | START | | 02402 | | | |

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| SAMPLE PROBLEM OUTPUT | | | | | |
|-----------------------|----------------|-----------------|-----------------|----------------|--|
| ROW 01 | | | | | |
| 1.4663088E+03 | 6.4575447E+02 | -3.7460682E+02 | 7.4650562E+01 | -1.7415282E+02 | |
| -1.0352652E+02 | -3.7460671E+02 | 7.4649988E+01 | -1.9078022E+02 | -1.0279811E+02 | |
| -6.6636106E+01 | -1.4405735E+02 | -1.7415323E+02 | -1.0352619E+02 | -6.6636326E+01 | |
| -1.4405730E+02 | -2.4905622E+01 | -1.2756122E+02 | | | |
| ROW 02 | | | | | |
| -6.4575471E+02 | 1.4663081E+03 | -7.4650132E+01 | -3.7460676E+02 | 1.0352640E+02 | |
| -1.7415280E+02 | -7.4649721E+01 | -3.7460666E+02 | 1.0279783E+02 | -1.9078033E+02 | |
| 1.4405717E+02 | -6.6636169E+01 | 1.0352602E+02 | -1.7415317E+02 | 1.4405717E+02 | |
| -6.6636074E+01 | 1.2756163E+02 | -2.4905419E+01 | | | |
| ROW 03 | | | | | |
| -3.7460681E+02 | 7.4650122E+01 | 1.5711990E+03 | 5.3158088E+02 | -3.7460658E+02 | |
| 7.4650309E+01 | -1.9842538E+02 | -9.1783324E+01 | -2.4531693E+02 | 9.9868300E-01 | |
| -1.9842532E+02 | -9.1782920E+01 | -6.6636404E+01 | -1.4405733E+02 | -5.2650675E+01 | |
| -1.4754309E+02 | -6.6636040E+01 | -1.4405724E+02 | | | |
| ROW 04 | | | | | |
| -7.4650461E+01 | -3.7460686E+02 | -5.3158137E+02 | 1.5711986E+03 | -7.4650360E+01 | |
| -3.7460661E+02 | 9.1783166E+01 | -1.9842558E+02 | -9.9850790E-01 | -2.4531696E+02 | |
| 9.1783322E+01 | -1.9842512E+02 | 1.4405749E+02 | -6.6636314E+01 | 1.4754307E+02 | |
| -5.2650584E+01 | 1.4405755E+02 | -6.6635884E+01 | | | |
| ROW 05 | | | | | |
| -1.7415292E+02 | -1.0352619E+02 | -3.7460669E+02 | 7.4650445E+01 | 1.4663088E+03 | |
| 6.4575518E+02 | -6.6636011E+01 | -1.4405764E+02 | -1.9077998E+02 | -1.0279795E+02 | |
| -3.7460646E+02 | 7.4650378E+01 | -2.4905406E+01 | -1.2756134E+02 | -6.6636140E+01 | |
| -1.4405719E+02 | -1.7415260E+02 | -1.0352591E+02 | | | |
| ROW 06 | | | | | |
| 1.0352616E+02 | -1.7415296E+02 | -7.4650439E+01 | -3.7460671E+02 | -6.4575552E+02 | |
| 1.4663088E+03 | 1.4405748E+02 | -6.6636039E+01 | 1.0279829E+02 | -1.9078010E+02 | |
| -7.4650154E+01 | -3.7460650E+02 | 1.2756138E+02 | -2.4905321E+01 | 1.4405729E+02 | |
| -6.6636070E+01 | 1.0352571E+02 | -1.7415255E+02 | | | |
| ROW 07 | | | | | |
| -3.7460671E+02 | 7.4649902E+01 | -1.9842536E+02 | -9.1783295E+01 | -6.6636318E+01 | |
| -1.4405726E+02 | 1.5711990E+03 | 5.3158069E+02 | -2.4531715E+02 | 9.9876500E-01 | |
| -5.2650722E+01 | -1.4754312E+02 | -3.7460684E+02 | 7.4650184E+01 | -1.9842552E+02 | |
| -9.1783250E+01 | -6.6636270E+01 | -1.4405735E+02 | | | |
| ROW 08 | | | | | |
| -7.4650069E+01 | -3.7460695E+02 | 9.1783092E+01 | -1.9842557E+02 | 1.4405716E+02 | |
| -6.6636439E+01 | -5.3158119E+02 | 1.5711986E+03 | -9.9867610E-01 | -2.4531720E+02 | |
| 1.4754326E+02 | -5.2650556E+01 | -7.4649847E+01 | -3.7460674E+02 | 9.1783371E+01 | |
| -1.9842532E+02 | 1.4405762E+02 | -6.6635987E+01 | | | |
| ROW 09 | | | | | |
| -1.9078043E+02 | -1.0279786E+02 | -2.4531705E+02 | 9.9865530E-01 | -1.9078013E+02 | |
| -1.0279773E+02 | -2.4531715E+02 | 9.9871160E-01 | 1.7090600E+03 | 4.5992369E+02 | |
| -2.4531696E+02 | 9.9889500E-01 | -1.9078038E+02 | -1.0279791E+02 | -2.4531690E+02 | |
| 9.9856500E-01 | -1.9078006E+02 | -1.0279789E+02 | | | |
| 24 | | | | | |
| ROW 10 | | | | | |
| 1.0279799E+02 | -1.9078048E+02 | -9.9853900E-01 | -2.4531700E+02 | 1.0279769E+02 | |
| -1.9078006E+02 | -9.9848400E-01 | -2.4531709E+02 | -4.5992412E+02 | 1.7090599E+03 | |
| -9.9883000E-01 | -2.4531697E+02 | 1.0279773E+02 | -1.9078034E+02 | -9.9844900E-01 | |
| -2.4531695E+02 | 1.0279788E+02 | -1.9078012E+02 | | | |
| ROW 11 | | | | | |
| -6.6636208E+01 | -1.4405735E+02 | -1.9842539E+02 | -9.1783212E+01 | -3.7460651E+02 | |
| 7.4650295E+01 | -5.2650751E+01 | -1.4754308E+02 | -2.4531727E+02 | 9.9929000E-01 | |
| 1.5711988E+03 | 5.3158152E+02 | -6.6635904E+01 | -1.4405770E+02 | -1.9842502E+02 | |
| -9.1783235E+01 | -3.7460622E+02 | 7.4650304E+01 | | | |
| ROW 12 | | | | | |
| 1.4405748E+02 | -6.6636059E+01 | 9.1782980E+01 | -1.9842528E+02 | -7.4650240E+01 | |
| -3.7460648E+02 | 1.4754315E+02 | -5.2650645E+01 | -9.9896500E-01 | -2.4531733E+02 | |
| -5.3158175E+02 | 1.5711989E+03 | 1.4405751E+02 | -6.6636000E+01 | 9.1783167E+01 | |
| -1.9842520E+02 | -7.4650220E+01 | -3.7460642E+02 | | | |
| ROW 13 | | | | | |
| -1.7415305E+02 | -1.0352627E+02 | -6.6636157E+01 | -1.4405742E+02 | -2.4905349E+01 | |
| -1.2756150E+02 | -3.7460688E+02 | 7.4650094E+01 | -1.9078033E+02 | -1.0279804E+02 | |
| -6.6636266E+01 | -1.4405721E+02 | 1.4663086E+03 | 6.44575474E+02 | -3.7460701E+02 | |
| 7.4650331E+01 | -1.7415290E+02 | -1.0352640E+02 | | | |
| ROW 14 | | | | | |
| 1.0352633E+02 | -1.7415331E+02 | 1.4405762E+02 | -6.6636246E+01 | 1.2756160E+02 | |
| -2.4905331E+01 | -7.4650053E+01 | -3.7460692E+02 | 1.0279782E+02 | -1.9078025E+02 | |
| 1.4405739E+02 | -6.6636280E+01 | -6.44575497E+02 | 1.4663087E+03 | -7.4650269E+01 | |
| -3.7460682E+02 | 1.0352623E+02 | -1.7415284E+02 | | | |
| ROW 15 | | | | | |
| -6.6636448E+01 | -1.4405744E+02 | -5.2650617E+01 | -1.4754318E+02 | -6.6636081E+01 | |
| -1.4405719E+02 | -1.9842575E+02 | -9.1782889E+01 | -2.4531698E+02 | 9.9858700E-01 | |
| -1.9842514E+02 | -9.1783117E+01 | -3.7460697E+02 | 7.4650370E+01 | 1.5711991E+03 | |
| 5.3158078E+02 | -3.7460642E+02 | 7.4650187E+01 | | | |
| ROW 16 | | | | | |
| 1.4405741E+02 | -6.6635963E+01 | 1.4754329E+02 | -5.26506464E+01 | 1.4405728E+02 | |
| -6.6636120E+01 | 9.1783150E+01 | -1.9842575E+02 | -9.9848600E-01 | -2.4531693E+02 | |
| 9.1783044E+01 | -1.9842511E+02 | -7.4650249E+01 | -3.7460705E+02 | -5.3158132E+02 | |
| 1.5711989E+03 | -7.4650180E+01 | -3.7460667E+02 | | | |
| ROW 17 | | | | | |
| -2.4905246E+01 | -1.2756135E+02 | -6.6635970E+01 | -1.4405744E+02 | -1.7415252E+02 | |
| -1.0352599E+02 | -6.6636280E+01 | -1.4405766E+02 | -1.9078030E+02 | -1.0279773E+02 | |
| -3.7460657E+02 | 7.4650430E+01 | -1.7415299E+02 | -1.0352592E+02 | -3.7460661E+02 | |
| 7.4650420E+01 | 1.4663090E+03 | 6.4575500E+02 | | | |
| ROW 18 | | | | | |
| 1.2756157E+02 | -2.4905077E+01 | 1.4405743E+02 | -6.6635999E+01 | 1.0352625E+02 | |
| -1.7415264E+02 | 1.4405735E+02 | -6.6636260E+01 | 1.0279760E+02 | -1.9078034E+02 | |
| -7.4650438E+01 | -3.7460659E+02 | 1.0352623E+02 | -1.7415307E+02 | -7.4650306E+01 | |
| -3.7460659E+02 | -6.4575543E+02 | 1.4663090E+03 | | | |

| VARIABLE | SOLUTION |
|----------|----------------|
| 01 | 1.9830998E+01 |
| 02 | -6.9528340E+01 |
| 03 | -6.1050400E+00 |
| 04 | -6.2656100E+01 |
| 05 | 1.9832610E+01 |
| 06 | -6.9529790E+01 |
| 07 | -6.1058000E+00 |
| 08 | -6.2655270E+01 |
| 09 | -3.5329000E+01 |
| 10 | -5.2727110E+01 |
| 11 | -6.1044400E+00 |
| 12 | -6.2656883E+01 |
| 13 | 1.9830690E+01 |
| 14 | -6.9528290E+01 |
| 15 | -6.1052200E+00 |
| 16 | -6.2656050E+01 |
| 17 | 1.9832600E+01 |
| 18 | -6.9529730E+01 |