MASSACHUSETTS INSTITUTE OF TECHNOLOGY

PROJECT MAC

Artificial Intelligence Memo. No. 177

August 1969

Preprocessor for Programs which

Recognize Scenes

H. N. Mahabala

A visual scene is transformed from a very simple and convenient format, to an internal format which describes the same scene, but is more akin to complex manipulations. This format is compatible with programs like "SEE".

The entire analysis is done using a basic primitive which gives the orientation of a point with respect to a directed line. A novel handling of inaccuracies in the scene is achieved by considering the lines to be strips of small but not negligible width. The criterion is very general and easy to modify.

Visiting Professor from Indian Institute of Technology, Kanpur, India.

Preprocessor For Programs Which Recognize Scenes

H. N. Mahabala (Visiting Professor from Indian Institute of Technology, Kanpur, India)

The output of a program which processes the data from a vidisector is often a graph (list of vertices, their location and list of neighbors). This graph has to be checked for consistancy such as all intersection of links are labelled as vertices, etc.. Further the regions have to be labeled and property lists which organize the ingormation in very specialized forms for programs like "SEE" have to be prepared. A preprocessor called "SETUP" has been written in basic LISP. SETUP includes the following features.

- (a) Entire analysis is performed using a basic primitive which gives the orientation of a point with respect to a directed line. Orientation is expressed as to the left, or to the right or in the direction of the line or away from the directed line. Since inaccuracies in the location of a vertex is unavoidable the directed line is in fact interpreted as a strip of variable width. Criterion used is very general but the organization is such that only one function has to be changed if a new criterion is to be used.
- (b) Since advice from lower level programs deal with only points (for example: points X and Y are on the same body) appropriate region names can be determined using available functions.

(c) Main background is determined without additional information.

It is interesting that the following can be achieved using only the "orient" primitive.

- (i) Determine whether a given point is inside or outside a general region (with holes).
- (ii) Determine whether a given boundary encloses a region with bounded or unbounded area.
- (iii)Determine whether a given line segment intersects the boundary of a region.
- (iv) Determine the connectivity of a graph and relative location of the various subgraphs.

Introduction

Programs which recognize or understand scenes work with line diagrams of a scene. It is preferable for the data of the scene to be presented in a pseudo canonical form. This requires ordering of the neighbors of a vertex (for example, anticlockwise) and including the names of regions in describing the neighborhood of a vertex.

Since one has to test a program (in turn a heuristic) for a large

variety of scenes of considerable complexity preparation of data in the pseudo canonical form can be very time consuming (see Figure 'HARD'). So it is desirable to have a preprocessor which can accept the scene in a simple format such as the incidence matrix. Further the output of programs that process the output of a vidisector is often in the simplified format. Thus the preprocessor can act as a link between the lower level programs and higher level programs. It is very desirable, why even necessary, for work on recognition programs to be able to use as data a line diagram (in black on white) of a scene to be analyzed. Thus one can test a program on a wide variety of scenes without too much trouble and facilitate answering the most often asked question of a recognition program: "What will the program do on this scene?".

Instead of treating the preprocessor as merely a program (or hack)
it would be nice if recognition primitives and computational techniques
involved are carefully selected so that one can view the preprocessing
as the computation of an automaton with certain capabilities. Such
a view point can help in arriving at a hierarchy of automaton for
understanding scenes.

Objectives

2.1 General

- (a) The output of the program should be compatible with input for existing recognition programs. However better organization of output wherever desirable should also be considered.
- (b) Program should be in LISP and LISP features used should be general enough to run on almost any version of LISP. Compilation if desired should also be straight forward.
- (c) All functions defined should be prefixed by a special character to facilitate easy change of a name (M% is used) in case of conflict that might arise when the program is made part of another program.
- (d) Remprop all unnecessary functions and variables at the end of the preprocessing.
- (e) The output will usually be in the form of property lists.
 Hence it should be possible to print out the output of the program in a format easy for human understanding.
- (f) All error processing should be centralized in a single routine (M% ERROR) so that handling of an error can be altered very

easily. This requirement is mandatory if the whole recognition system should somehow procede in case of certain errors and not just hangup. (At present the preprocessor quits after printing a suitable message.)

2.2 Particulars

- (a) The input of the graph of a scene should be as simple as possible. The data includes name of scene, and list of vertices, their location and unordered list of neighbors.
- (b) The output is in the form of property lists and a subset of the property lists is compatible with "SEE" of Guzman.
- (c) It is sometimes necessary to handle more than one scene with perhaps same vertex names at the same time. This is made possible by including a feature by which names of vertices, regions and subgraphs can be prefixed by the name of the scene. All global properties are on the name of the scene.

(d) Check for certain types of constancies in the input such as:

(i) Each link of the graph appears in two places, i.e. if B appears as a neighbor of A then A should appear as neighbor of B. The urge to relax this requirement (since finally a lower level program prepares input) and update suitably in case of error was curbed so that human errors in preparation of data is not misinterpreted.

- (ii) Intersection or meeting place of any two links should be at a vertex.
- (iii) Two or more neighbors of a vertex should not be collinear on the same side. (See also section 4.2).
- (e) Since input data and in particular location of a vertex is subject to hardware inaccuracies, not to forget truncation errors, certain decisions such as the following should not be based on pure geometric theorems. (See also section 3.1.3).
 - Whether two links are in the same line.
 - (ii) Whether three points are collinear.
- (f) Find the connectivity of the input graph. Separate the scene into subgraphs and find their relative location. This is desirable since each subgraph can be a body or a hole.
- (g) Find the main background (the only unbounded region which extends to infinity around the graph). The background of each subgraph (the region in which the subgraph is situated) should also be determined. The information on each subgraph should be organized in such a way that recursive analysis of the scene can be facilitated. Matching T's cannot be found satisfactorily with the available information, however, matching T's with respect to the main background should be determined. There should be facility for updating matching T's as and when more is known about the scene.

- (h) It should be possible to change the name of a vertex, region or subgraph in a scene even after the preprocessing is complete.
 (Such as identifying vertex A on LEFT scene is same as vertex X in RIGHT scene of a stereo pair.)
- (i) Advice from lower level programs or between higher level programs such as
 - Point X (XCOR, YCOR) is in the background.
 - (ii) Points X and Y are on the same body.
 - (iii) Region which has KV* (ordered boundary) is
- (iv) Region with A and B (two ordered adjacent points on the boundary) on the boundary is....... should be updated by substituting internally generated names (for subgraphs or regions). This is facilitated by making available some utility functions which are retained even after unnecessary ones are removed.

Interesting Features

3.1 "Orient" Primitive

In conforming with the intention to use simple recognition primitives it was felt that all the work involved in the preprocessor, referred to as SETUP, can be done by using a primitive which answers the question: "What is the orientation of a point with respect to an oriented half line." The answer will be in the form: to the left, to the right, ahead or behind. This recognition ability is more basic than evaluating magnitude of angles. Further one always makes approximations in judging orientation and hence similar facility for
approximating should be incorporated in this primitive. This approximation is all the more necessary in the computer program since
location of vertices are subject to hardware errors. Truncation
aggravates the problem.

3.1.1 Strict Mathematical Rule Such as:

0° - ahead

0° < θ < 180° left

180° behind

180° < θ < 360° right

where 0 is the angle between the line and the line joining the starting point of the oriented line and the given point (angle (AB) in Figure 1).

This criterion is rejected because there is no room for approximation and if this criterion is used no T's will be found in real scenes!

3.1.2. This incorporates an approximation to criterion 3.1.1.

$$-10^6 \le \theta \le 10^6$$
 ahead

170° ≤ 0 ≤ 190° behind

190° < 0 < 350 right

this works fine except that very large error results if the point distance from the origin of the directed line is large. In general one can expect that all vertices shift by about the same amount irrespective of their location due to hardware inaccuracies, (barring edge effects). Hence moving a vertex by large distance in order to consider it collinear with a line is not in general justified.

3.1.3. The line is viewed as a strip of finite width for deciding collinearity. This in itself will not suffice because orientation of C with respect to AB may not be collinear whereas A is collinear with respect to BC (See Figure 1(b)). Even though successive logical extensions cannot be allowed in approximate techniques at least three points should be judged collinear no matter which two of the three points is used for the directed line. So three points are judged collinear if any one point is collinear with respect to the strip along the other two points, i.e. A, B and C are considered if:

C lies in a strip of width ±EPS along AB or B lies in a strip of width ±EPS along AC or A lies in a strip of width ±EPS along BC

It looks at the outset that taking the strip parallel to one of the three sides of the triangle is not general enough. In fact one would like to fit a line which minimizes the sum of the squares of the distance from each point to the line. And the three points are collinear if they lie within a strip of width ±EPS about this line. It is not easy to find such a line. (This is not the regular least square fit line). Further, it can be easily shown that, if three points are collinear from the best fit line criterion, it will also be collinear with respect to our three strip criterion.

Figure 2(a) shows the criterion used in the present preprocessor (MMSETUP). The organization of the preprocessor is such that one easily can use any other criterion by rewriting MMORNT. Figure 2(b) illustrates the case where EPS is larger than distance between A and B. Obviously greater reliance is put in direction of AC or BC than that of AB.

It is reasonable to use a value for the half width of the strip

(EPS) which is commensurate with the hardware inaccuracies. In
creasing EPS beyond reason (half of minimum distance between any two
neighbors) will cause trouble which is understandable. All attempts
to adjust value of EPS dynamically by studying only the neighborhood
of a vertex should be considered carefully. One of the dangers
of such an adjustment is that many vertices will end up being T's!

One interesting technique of analysis of a scene would be analyze it at more than one value of EPS and reconcile the discrepancy if any.

It should be noted that MXORNT only shows conclusions about the orientation and does not adjust the coordinates of the vertices to fit the orientation geometrically (according to 3.1.1). It is feared that any attempt to adjust data recursively will ruin the features.

3.2 "SECT" Function

A primitive derived from orient finds whether two line segments intersect or not (Figure 3).

3.3 "Inside" Function

It is interesting that we can determine whether a point is internal to a region (given by ordered vertices on the boundary) by using the orient primitive. A point is inside if the number of intersections of the boundary with the infinite half line joining the point to a vertex on the boundary is odd, otherwise outside.

3.4 "Bounded" Function

Often we need to find if a region given by an ordered set of vertices has bounded area. The technique first finds the vertex with the minimum X coordinate. Then if the region is to the left of this point it is unbounded (Figure 2).

Overall Technique (MXSETUPX)

The names referred to in this memo (prefixed by M%) are names of LISP functions.

4.1 M% SETUP1

Input data is separated after appending a prefix (NIL if M%SETUP is used and NAME if M%SETUP* is used).

4.2 M%ARRANGE

The neighbors of each vertex are arranged in counter clockwise order. This is achieved by successively adding a neighbor to the ordered list. If EPS2 (square of the half width EPS for M%ORNT) is large two vertices will fall in the same direction which is an error.

4.3 M% TYPE

The TYPE* (see section 5) of each vertex is found.

4.4 M%FREGION

Regions associated with each boundary is labeled. The technique is: start with a vertex A (Figure TEST) and choose a neighbor (say H) connected to a A by an unused link (i.e. AH has not yet been identified as a boundary of a region). Mark AH as used. At H pick the vertex (K1) which is before A in the ordered list of neighbors of H. HK1 should also be unused which will not be the case if data is not consistent. So we

have AHK1 as a partial boundary of a region :4. Proceed as before from K1 until we reach A. There make sure that the next link (after MA) is indeed AH. This will not be the case if we had started from H instead of A. So proceed until the first link used is obtained again. It should be noted that a vertex can appear more than once on its boundary (:4 has as K vertices H,K1,L1,J,I,H,G,F,E,D,C,B,M,A). At this stage the region names and their boundaries are not final for those regions which have holes. For example: entire area within A2 A7 A6 A3 (Figure CRAZY) will be:3 and entire area outside D1 D4 D3 D2 will have a separate number. Later the extra name is eliminated and the boundary of:3 is adjusted.

4.5 M % SUBGRAPH

Connectivity of the total graph is found. The technique is that each subgraph is constituted by a minimal subset of vertices whose neighbors are also in the subset. For example, G1, G2 and G3 (Figure CRAZY) form a subgraph.

4.6 MY SEPARATE

The relative location (structure) of the various subgraphs are determined. The technique is: the background (unbounded region associated with a subgraph) of a subgraph is determined (Section 3.4). Pick the subgraph which has the vertex with the minimum X coordinate of all the vertices (Al of SUBGRAF10 in Figure CRAZY). The background of all the vertices (Al of SUBGRAF10 in Figure CRAZY). The background of the scene is the background of Subgraf 10 (:2). Separate the other subgraphs according as OUTSG if one point on them is in :2 (i.e. outside SUBGRAG10 and INSG if one point in them is not in :2. For example subgraphs 7, 4 and 6 will be in OUTSG and 3.2.5 and 1 in INSGµ Separate INSG into subsets within each region of SUBGRAF10. Proceed with OUTSG and various subsets of INSG from beginning (recursively) except that the background in each case is to be merged with a region of SUBGRAF10. For example background of OUTSG (associated with C1 C2 C3) will have to be merged with :2 and background of 1,2 and 5 (associated with F1 F2 F3 F4) is to be merged with :1. The structure information is organized as a list and is explained in Figure CRAZY.

A note about finding the background (M%BGROUND). Any cardinal point (i.e. a vertex with minimum x or y coordinates or with maximum X or Y coordinates) can be used for finding the background. The region name in each case should be the same. However, if the intersection of two links is not identified as a vertex the region names will be different causing an error exit.

4.7 M %ADJUST1

Merging information of multiple region names are gathered and information about the subgraphs in each region is collected.

4.8 M%REDUND

If there is more than one name possible for a region one with a lower number is retained. The property list of region names are updated (take care of multiple boundaries) and property lists of unused region names are deleted. However, the occurrences of region names eliminated have yet to be replaced by corresponding names. A list (M LIST) of substitutions necessary is prepared.

4.9 M%REPLACE

M LIST is used to make the substitutions in all property lists associated with M%SETUP (or M%SETUP*).

4.10 M%SEEDATA

Since one main requirement of M%.SETUP was to be compatible with
"SEE" appropriate new properties are created. NAME is given a value
which is compatible for using "PREPARA" (a preprocessor for SEE).
However, PREPARA can be bypassed. Value of NAME can be used to plot
the scene using a package written by Guzmán.

4.11 M%MATCHT

A pair of T's in a scene are matching T's if

- (i) they face eachother with their tails collinear and are the closest possible.
- (ii) the base region (one which subtends an angle of 180° at the vertex) of each T should not be a background, and
- (iii) the line joining them does not intersect any region identified as background.

M%SETUP finds the matching T's only with respect to the main background (i.e. 35 in Figure HARD). However, M%MATCHT is so organized that further updating can be done very easily. For example, M%MATCHT can be called using 36 and 34 as background and operating on only those T's which already have mates. In this case it well not make an alteration in the set of matching T's. M%MATCHT was tested on HARD by identyfying 26 (rather illogical) as background. Then vertices a, fa and b, fb were eliminated from the set of matching T's.

The technique used is to make sure that each T(of a matching pair) accepts the other as a mate, when all T's are available for matching. Since M %ORNT uses a strip for matching collinearily sometimes, cycle can arise which is an error.

Property Lists

M%SETUP (or M%SETUP*) sets up a number of property lists whose description follows.

5.1 NAME

Its value is data suitable for PREPARA.

PREFIX Explode list of characters in NAME if M % SETUP*

is used, otherwise NIL.

ACCURACY Half width of the strip for M%ORNT.

ERROR Error message in case M% MATCHT had to delete vertices

from matching because of cyclicity. [Such as B is

mate of A, C is mate of B, and A is mate of C.]

VERTICES List of vertices in the scene.

REGIONS List of regions in the scene.

CONNECTIVITY Number of subgraphs in the scene.

SUBGRAPHS List of subgraphs in the scene.

MAXMIN List of cardinal points (Min X, Max X, Min Y, Max Y).

BACKGROUND List of backgrounds (only one initially).

STRUCTURE Structural information as explained in Figure CRAZY.

5.2 Nth Subgraph (SGRAFN)

MAXMIN VERTICES REGIONS BACKGROUND

Same as in case of Name (5.1).

5.3 VERTEX

XCOR X-Coordinate YCOR Y-Coordinate

TYPE Type information. See references to GUZMAN for

details.

KIND List of counter-clockwise neighboring vertices and

regions (alternately).

N VERTICES List of neighboring vertices.

N REGIONS List of regions having VERTEX on the boundary.

NEXTE Name of matching T, otherwise NIL.

COOR List of XCOR and YCOR.

TYPE* Classification of the vertex. Types L, ARROW, PEAK, X, T,

MULTI, K, FORK are the same as GUZMAN new types.

KK One straight line and more than two branches on one

side (vertex G in Figure TEST).

SL Straight line (I in TEST).

CROSS Two straight lines cross at the vertex (B in TEST).

KK becomes MULTI, CROSS becomes X in TYPE. However, SL continues to be SL which may cause error in SEE. However, SEE as it stands does not expect SL type of vertices.

OVERTICES List of elements each of which is a list of a neighbor and an orientation. Orientation gives a measure of the angle to be rotated (anticlockwise) from the neighbor to reach the next neighbor. For example at A in TEST MAB<180 is denoted L, HAM>180 (R) and at G FGH=180 (CA).

5.4 REGION

FOOP See GUZMAN

NEIGHBORS List of adjoining regions.

KVERTICES List of all vertices on the boundary. No separation

even if there are multiple boundaries.

BACKGROUND Has BACKGROUND if region is a background, otherwise NIL

(:4 in TEST).

BOUNDARY List of elements. Each element is a list of links

in one branch of the boundary. Each link is a list of ordered (counter-clockwise) neighbors on a seg-

ment of the boundary (:1 and :2 in TEST).

OTRAVERSE List of elements. Each element is a list of subelements

in one branch of the boundary. Each subelement is a list of a vertex on the boundary and a measure of the angle subtended by the region at that vertex.

NEIGHBORS* List of elements. Each element is the ordered NEIGHBORS

of one branch of the boundary.

KVERTICES* List of elements. Each element is the ordered KVERTICES

of one branch of the boundary.

INSUBGRAPH List of subgraphs located in the region.

can be done once the two OTRAVERSE'S are compatible. OVERTICES can also be used similarly to vertices.

- (viii) Choose accuracy very carefully.
- (ix) Since each subgraph can be a hole or a body, separate analysis of a subgraph is facilitated by the properties on each subgraph.
 - (x) STRUCTURE can be used to match scenes at a gross level.

REFERENCES

- Guzman, A. Decomposition of a visual scene into three-dimensional bodies. Prodeedings of the AFIPS Fall Joint Computer Conference, Vol. 33, Part One, pp 291-304, December 1968. Review 17,227; Computer Reviews 10, 8. August 1969. Also available as Project MAC Memorandum MAC-M-391, A.I. Memo. No. 171.
- Guzman, A. Computer Recognition of three-dimensional objects in a visual scene. Ph.D. Thesis, Electrical Engineering Dept. M.I.T. December 1968. Also available as a Project MAC Technical Report MAC-TR-59.

Use of M%SETUP

- Use M%SETUP* if more than one scene with same vertex names have to be handled simultaneously.
- (ii) Even if very little information is changed in the scene it will have to be set up again.
- (iii) The property lists created by M%SETUP can be printed out by using M%ANSWER.
- (iv) The property lists can be stored on disk on disk in a suitable internal format so that the property lists can be reestablished by reading the file. Consult GUZMAN for the program.
- (v) Since M%SETUP finds matching T's only with respect to the main background updating is necessary every time background information is altered. This should be all right since one may not analyze scenes with holes in the main background. Hence in general matching T's will be a subset of the matching T's found by M% SETUP.
- (vi) Advice from the lower level programs can be updated by using the special functions available (See SETUP Comment).
- (vii)Matching models of regions is facilitated by the property
 OTRAVERSE. Exact comparison of lengths of sides and magnitude of angles

SRIEF MANUAL FOR USING THE FILE VISION SETUP.

THE PACKAGE PREPARES A DATA GIVEN IN THE FORM (SETO DATA COUDTE (MANE (VERTEX) (X1 Y1) (MEIGHODRS1)) (VERTEX2

IN AFORM COMPATIBLE WITH "SEE". ADDITIONAL PROPERTIES ARE ALSO INCLUDED.

EXECUTE (MESETUP DATA ACURRACY)

THE VALUE OF ADURRACY IS HALF THE MIDTH OF A STRIP MITHIN MHICH THREE POINTS SHOULD LIE-FOR MEINE CONSIDERED COLLINEAR. IF ACURRACY IS ZERO DEDMETRICAL COLLINEARITY MILL BE USED.

THE PROGRAM TERMINATES ATTH "DOME".

THE PROPERTY LISTS ON MANE. VERTICES, REGIONS AND BUBGRAPHS CAN BE PRINTED OUT

1. LOAD THE FILE VISION ANSHER 2. EXECUTE (MEANSHER SCENE NIL).

SCENE EPDS PREFIX REPREFIX SCPREFIX

THE VALUE OF SCENE IS "MARE".

VALUE OF "MAME" IS GATA IN A FORMAT COMPATIBLE WITH THE INPUT REQUIRED BY PREFARA OF "SEE".

ALL FUNCTIONS ARE EXPRE AND THERE MAKE BEGINS HITH MX.

THE REGIONS ARE NUMBERED CONSECUTIVELY FROM 11 WHEN A NAME IS USED FOR THE FIRST Time after Loading a List. Mundering Continues even if the Bata is rescrip. Modever the numbering can be started from any value by resetting the property RNAME on NAME to Starting munder required.

CAUTION IF THE VALUE OF ACCURACY IS TOO BIG ERROR MILL OCCUR IN MEAREANGE.
MAKIMUM VALUE FOR ACCURACY IS ABOUT ONE MALF OF OF THE MINIMUM DISTANCE
BETMEEN ANY MEIGHBORS.

"MARE" DAM SE APPENENDED TO MAMES OF VERTICES REDIONS AND SUBGRAPHS BY EXECUTING (MESETUPE DATA ACCURACY)
PROSENT TERMINATES MITH "DONE".
EXECUTING (MEANSHER SCENE PREFIX) PRINTS DUT THE PROPERT LISTS WITHOUT THE PREFIX.
EXECUTING (MEANSHER SCENE MIL) PRINTS THE INTERNAL FORMAT (WITH PREFIX).

THE EXECUTION OF MESETUP OR MESETUP AUTOMATICALLY REMPROPS ALL FUNCTIONS EXCEPT A FEW UTILITY PROGRAMS TESTUP DAM BE USED BY READING IN THE FILE VISION SETUP AGAIN.

1F YOU DON'T LIKE THIS REMOVE THE LAST S-EXPRESSION IN MESETUPX.

IF 40 PUNCTION IS TO BE RETAINED EXECUTE IMEA_GLEAR)
SRIEF DESCRIPTION OF FUNCTIONS RECOMMENDED FOR USE

NOTE KY- IS THE ANTICLOCKHISE TRAVERSE OF THE BOUNDARY OF ARECION AND IS ALIST OF LISTS. FOR EG KY- OF A TRIANGULAR REGION IS ((A B C)) WHERE A B & C AR VERTICES.

IF THERE IS AN IMMER TRIANGLE X Y Z THEN KY- OF THE ANNULAR REGION IS ((A B C) (F E D)).

NOTE THAT NO VERTEX IS REPEATED.

OUGULE LETTER (SAY AA) MEANS THE VARIABLE IS ALIST OF XCOR AND YCOR (OF A).

FUNCTIONS MISDOUNDED HXINGIDE. AND MISBEST. REQUIRE THE PROPERTY

COOR (LIST OF XCOR YCOR) ON THE VERTICES MENTIONED IN KY-IMEGRAT EPEZ AA BB CC) RETURNS THE ORIENTATION OF CO WITH RESPECT TO THE DIRECTED LINE AA 88.
THE THREE POINTS ARE COLLINEAR IF THEY ALL LIE WITHIN A STRIP OF WIDTH 24(SERT EPS2).
THIS CRITERION IS SAME AS FITTING THE LEAST SQUARE FIT LINE TO THE POINTS AND MAKING SURE
THAT DISTANCE FROM ANY POINT TO THE LINE IS LESS THAN (SORT EPS2). IF DC IS COLLINEARRETURNED VALUE IS

CT IF CC IS IN SAME DIRECTION AS BE (41TH RESPOT TO AA)

CA IF CC IS IN A DIRECTION OPPOSITE TO THAT OF BE

CO IF CC IS HITHIN EPSE OF AA IF DO IS NOT COLLINEAR WITH AN US THEN
L IF CO IS IN THE LEFT MALF PLANE OF THE DIRECTED LINE AN US
R IF CO IS IN THE RIGHT HALF PLANE OF THE DIRECTED LINE AN US (HXQ18T3 AA 88)
RETJRMS THE SQUARE OF THE SISTANCE BETHEEM AA AND 86 (HESECT AA 80 CC DD)

FINDS IF THELINE: SEGMENTS AA 88 AND CC DD INTERSECT AND RETURNS
ON IF PUINT OF INTERSECTION IS ONE OF AS 80 CC DD

(CDINCIDENCE) NEANS MITHIN AGISTANCE OF (SORT EPS2))
TES IF PUINT OF INTERSECTION IS OTHER THAN AS 80 CC DD
ND IF THEY DO NOT INTERSECT (HXBOUNGEU- KV-)
FINDS IF THE REGION SIVEN BY CV-MAS FINITE OR INFINITE AREA AND RETURNS
SOUNDED FINITE:
UNBOUNDED INFINITE:

(HX[MBIDE+ KV+ XA)
FINDS IF THE POINT XX IS INSIDE (INCLUDING ON) OR DUTSIDERETURNS I N

(MIRGSECT+ KY+ XX TY)

FINDS IF THE LINE SEGMENT IX TY CUTS INE SOUNDARY OF REGION GIVEN BY KY+ AND RETURNS
ON IF POINT OF INTERSECTION IS XX OR TY

YES IF POINT OF INTERSECTION IS OTHER THAN XX OR YY

NO IF THERE IS NO INTERSECTION

INTRESIDANT SCENE XX)

RETURNS THE MANE OPPERSION OF THE SCENE IN MHICH THE POINT XX LIES. ON THE SOUNDARY IS CONSIDERED AS IN AND HENCE ONE OF THE TWO POSSIBLE RESIONS ALL BE PICKED ARBITRATILY.

(MX46TU SCENE TU)

TJ IS A DIRECTED SEGMENT OF THE BOUNDARY DIVEN BY (A B) RETURNS THE REGION OF SCENE HAICH HAS TU AS PART OF THE BOUNDARY NIL IF THERE IS NO SUCH REGION

(NERGAY* SCENE KY*)
RETJENS THE REGION MHICH MAS AY* AS THE AVERTICES*
NIL IF THERE IS NO SUCH REGION

IMIGATEME SCENE VS 801 802)
VS LIST OF VERTICES TO BE MATCHED
801 LIST OF REDIONS
802 LIST OF REDIONS

FOR LISE OF REGIONS

LEARS THE MEXTE OF T VERTICES OF VS

PUTS PROPER MATES ON MATCHING THE THAT COMPORT TO FOLLOWING

1. DO NOT MAVE MEMBERS OF 801 AS THE REGION CONTAINING THE STRIGHT LINE AT THE T.

2. THE LINE JOINING THE MATCHING THE DOES NOT INTERSECT BOUNDARY OF HEMBERS OF 802.

USUALLY 801 AND 802 ARE SACKSROUNDS.

802 IS MIL IF CONDITION 2 IS NOT REQUIRED.

MILETUP OR MISSETUP MILLIFINU MATCHING THE OF SCENE USING THE DRE OPEN REGION FOR 801

AND 802.

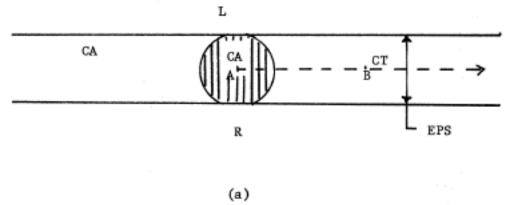
AND \$92.

AND RESIGNS ARE SECLARED AS BACKGROUND NATCHING I'S CAN BE UPDATED USING MEN RESIGNS FOR BEI AND B

(MEREPLACE SCENE HLIST)

MLIST ((FORT HITHE) (FORE HITHE) (FORJ HITHE))

UPDATES THE PROPERTY LISTS OF SCENE (AS PRODUCED BY MESETUP OR MESETUP») BY REPLACING ALL: JODURENCES OF FORE BY HITHE THE ELEMENTS REPLACED DAY BE MANES OF VERTICES OR REGIONS OR SURAFS.



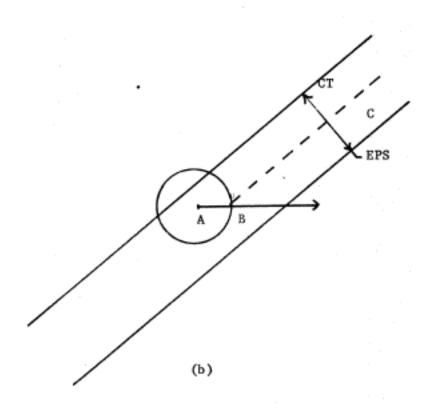


Fig. 1 Orientation of C with respect to AB

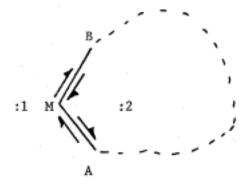


Fig. 2:1 Unbounded and :2 Bounded.

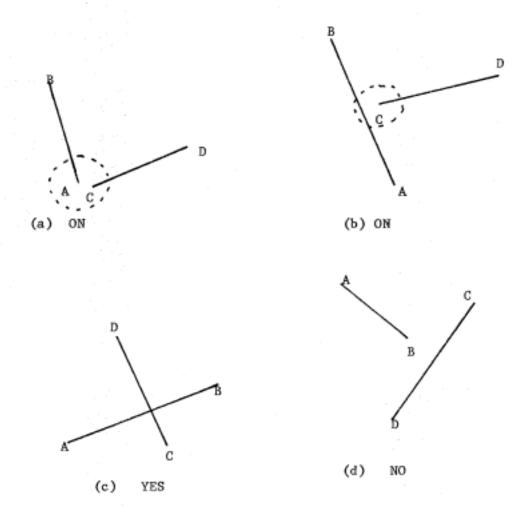


Fig.3 Return of M/SECT

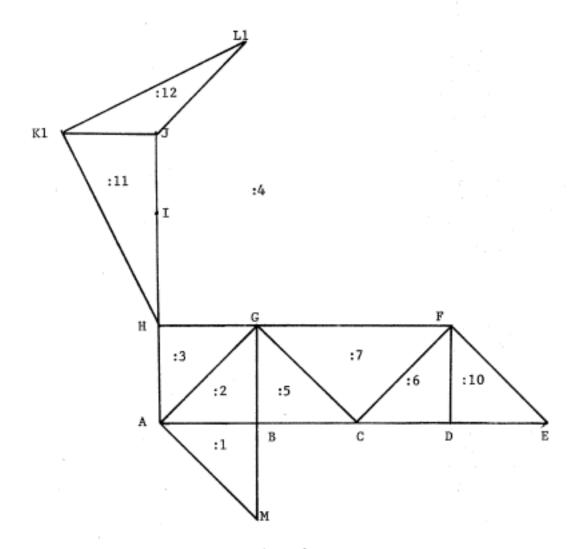


Fig. 'TEST'

(10 (INSIDE 10) (OUTSIDE 10))

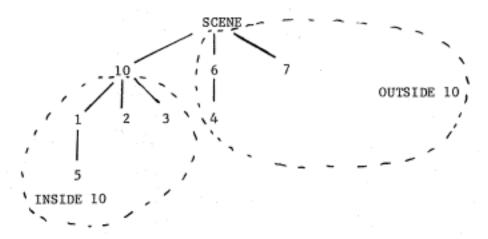
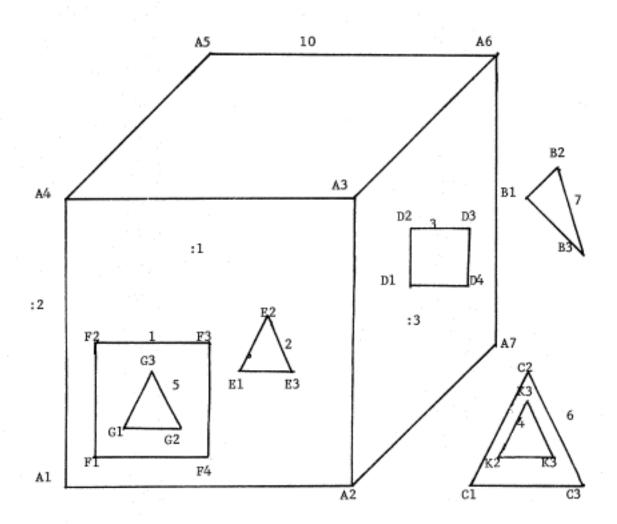


Fig. 'CRAZY'



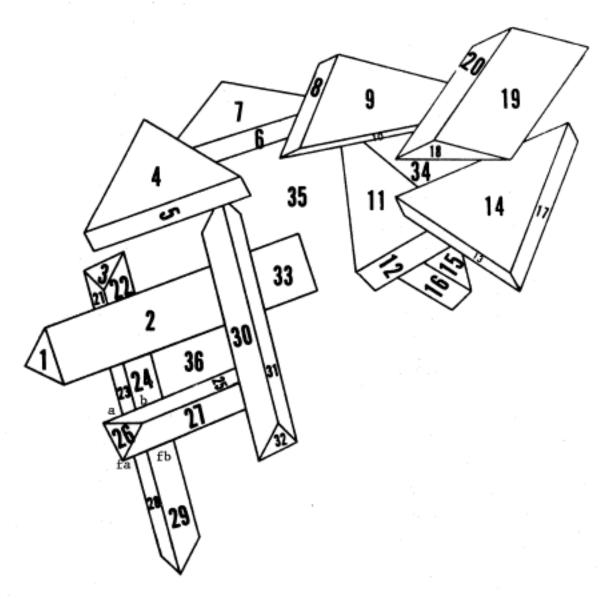


Fig. 'HARD'

SCENE TEST PREFIX NIL

DATA (TEST (A (10 0) (0 m 0 m)) (0 (11 0) (A 0 0 m)) (0 (12 0) '0 0 7 0)) (0 (13 0) (0 F 5)) (5 (
14 0) (0 7)) (7 (13 1) (0 0 0 5)) (0 (11 1) (m 7 0 0 0)) (m (10 1) (A 0 1 (1)) (1 (10 2) (m J)) (J (
10 3) (I K1 L1)) (K1 (7 3) (M J L1)) (L1 (11 4) (J K1)) (M (11 -1) (B A)))

1531

ACCURACY

0.09999999

THE SCREE

VERTICES

(A 3 0 0 E F G M 1 J K1 L1 M)

REGIONS

(*12 *11 *10 *7 *6 *8 *4 *3 *2 *1)

COMMECTIVITY

SJESTAPHS

PHS (SGRAF1)

MAXMEN (KE E M LE)

BACKGROUND

(54)

STRUCTURE

(SGRAFI NIL NIL)

SSRAF1

HAXMINICAL E H L1)

VERTICES(H & B B C E F D I H L1 K1 J)

REGIONS(#12 #11 #10 #7 #0 #5 #4 #1 #2 #3)

BACKGROJND(14)

CODE FOR VERTICES

VERTEX

XCQ₹

Y004

TYPE

K140

NVERTICES

NREGIONS

```
TYPE.
         OVERTICES
         10
         (PEAK (+ 14 4))
         (14 4 11 8 12 6 13 4)
         (4 3 2 4)
         (14 11 12 13)
         MIL
         (10 0)
         PEAK
         ((# L) (# L) (# L) (# R))
        11
         (X (G 15 12 4 11 141)
        (#$ G #2 4 #1 # #4 C)
        (# A 4 2)
        (15 12 11 14)
        NIL
        (11 0)
        CROSS
        ((G L) (A L) (A L) (C L))
¢
        12
```

NEXTE

0004

0

```
(4 (17 14 D 16 7 B 15 B))
        (17 0 15 8 14 0 16 7)
        .....
        (17 15 14 15)
       ((G L) (8 C4) (G L) (F L))
0
       13
       (T (F D E C #10 #6 #4))
       (#10 F 16 C 14 E)
       (F C E)
       (*10 #6 #4)
       WIL.
       (13 0)
       ((F L) (C CA) (E L))
       14
       t. (*10,14))
       (*10 D *4 F)
       (0 F)
       (#10 #4)
```

(14 0)

```
(PEAK (E 14 GI)
        (110 E 14 G 17 G 16 D)
        (E 2 C 0)
        (310 14 17 16)
        HIL
        (13 1)
        ((E R) (8 L) (C L) (8 L))
.
        11
        (MULTE 3)
        (17 F 14 H 13 A 12 8 15 G)
        (F + 4 0 C)
        (17 14 13 12 15)
        NIL
        (11 1)
        (IF CA) (# _0 (A L) (B L) (C L))
        10
        (X (4 14 13 ] 14 111))
        (*11 <1 *4 4 *3 0 *4 1)
        (K1 A 2 1)
        (*11 14 13 14)
        MIL
```

((0 %) (F L))

```
(10 1)
        ((KI L) (A L0 (6 L) (I L))
ı
        2
        (SL (+11 +4))
        (411 + 14 3)
        (H J)
        (*11 14)
        MIL
        (10 2)
        SL
        ((# DA) (J 2A))
Į
        3
        (FORK J)
        (#12 K1 #11 I #4 L1)
        (41 I L1)
        (*12 *11 *4)
        WIL
        (10 3)
        FORK
        ((6) 4) (1 4) (41 43)
51
        (ARROW (J K1 H L1 +11 +12 +4))
```

(412 L1 44 4 411 J)

```
(61 # 3)
(*12 *4 *11)
(7 3)
ARROH
COLUMN CHI JA CA LID
(6 (812 84))
(*12 4 44 51)
(3 (1)
(*12 14)
NIL
(11 4)
(() 4) (41 .0)
(1 (11 14))
(*4 B *1 A)
(*4 *1)
(11 -1)
((8 L) (4 P))
```

j

CODE FOR RESIDUS

```
RETCHESONS
        KVERTICES
        BACKGROUND
        POUNDARY
        OTRAVERSE
        *EFFEREZEM
        KVERTISES.
        INSUBSTATE
*12
        ((#4 L1 #4 (1 H11 J1)
        (** ** *11)
        (L4 K1 J)
        NIL
        (((J L4) (L1 K1) (K1 J));
        (((L1 L) (K] L) (J L)))
        ((84 44 *11))
        ((L1 K1 J))
*11
        (144 | 14 J 112 K1 14 H))
        (14 14 112 14)
        0.741.40
        MIL.
        (((4 I) (I J) (J K1) (K1 H)))
        ((() CA) (J L) (K1 L) (H L)))
        ((14 14 112 14))
```

PCIGSP

FOGP

```
(() J <1 41)
       NIL
*10
        (484 E 84 F 86 D))
       (84 14 15)
        12 . 01
       414
        (((D E) (E *) (# D)))
        (((E L) (F _# (0 L)))
        ((## ## #6))
        ((E F D))
        MIL
17
        ((16 F 14 G 15 C))
        (16 14 15)
        (F & C)
        NIL
        ((4C F) (F 2) (8 C)))
        (((* _) (6 _) (6 _)))
        ((46 14 15))
        (4F & C1)
        (444 D 410 * 47 CF)
        (#4 #10 #7)
        (0 # 0)
        416
        (((C D) (D #9 (F C)))
```

(((0 4) (7 4) (2 4)))

```
((*4 *10 *7))
        ((0 F 0))
        NIL
15
        ((#4 C 17 G 12 B))
        (14 17 12)
        (8 6 3)
        MIL
        (((8 0) (0 3) (8 8)))
        (((0 4) (0 4) (0 4)))
        ((14 17 12))
        ((C S B))
        NIL
14
        ((#3 H #11 <1 #12 L1 #12 J #11 I #11 H #3 & #7 F #10 E #10 @ #6 C #5 8 #1 H #1 A))
        (#3 #11 #12 #12 #11 #11 #3 #7 #10 #10 #6 #5 #1 #1)
        (4 41 L1 J 1 4 8 F E D C B M A)
        8404680340
        CCCA H3 CH CL) (K1 L1) CL1 J) CJ 1) CI H3 CH D) CD F3 CF E3 CE D) CD C) CO B3 CB H3 CH A333
       (CCM L3 (K) R) (L1 R) (J L) (1 CA) (H L) (8 CA) (F R) (E R) (8 CA) (8 C) (8 L) (H R) (A R))
        ((#3 *11 *12 *12 *11 *11 *3 *7 *10 *10 *6 *5 *1 *11)
       CONTRACTOR SESSIONAL
        (SGRAF1)
13
       [[12 0 14 H 14 A]]
       152 56 567
       (6 4 A)
       NIL
```

```
(((A B) (B 4) (M A)))
       (((& L) (H _0 (A L))))
       ((12 14 14))
       ((A H A))
       MIL
12
       (411 B 15 G 13 A))
       (*1 *5 +3)
        (8 2 A)
       MIL
        CCCA B) (8 23 19 A)))
        (((8 L) (8 J) (4 L)))
        ((*1 #5 #31)
        (18 G 41)
        MIL
**
        1:14 H 14 B 12 A1)
        (14 14 12)
        (A & A)
        CCC4 40 (N 83 CB A)))
        (((4 L) (8 L) (A L)))
        ((14 14 12))
        ((# # A))
        WIL
```

ŧ

SOEME CRAEY

DATA (CRAZY (A1 (0 0) (A2 A4)) (A2 (12 0) (A1 A3 A7)) (A3 (12 12) (A4 A6 A2)) (A4 (0 12) (A1 A5 A 3)) (A5 (5 17) (A4 A5)) (A6 (17 17) (A5 A3 A7)) (A7 (17 5) (A5 A2)) (31 (20 12) (32 63)) (32 63)) (32 (21 13) (31 33)) (33 (22 13) (31 32)) (31 32)) (31 32)) (32 (32 13) (31 32)) (31 32)) (32 (32 13)) (32 (32 3)) (33 (32 3)) (33 (33 4) (31 32)) (41 (17 1) (42 (3))) (42 (21 1) (41 43)) (43 (20 3)) (41 (21 1) (41 47) (32 34)) (32 (14 1)) (31 33)) (33 (16 1)) (32 (34)) (34 (16 7) (33 31)) (41 (37 3))

TEAPS

ACCJ\$ACY 0.00999999

ERROR NIL

VERTICES (A1 A2 A3 A4 A5 A6 A7 B1 B2 B3 C1 C2 C3 C1 G2 33 K1 K2 K3 D1 D2 D3 D4 E1 E2 E3 F1 F2

F3 F4)

9EG1048 (#20 #16 #13 #12 #11 #10 #6 ## #3 #2 #1)

CONNECTIVITY 10

SUBERAPHS (SCRAFIC SCRAFF SCRAFS SCRAF4 SCRAF3 SERAFE SCRAFE)

MAXMIN (A4 C3 C3 A5)

BAC<240UND (#2)

STRUCTURE (SERAF10 (SERAF1 (SERAF5 WIL WIL) (SERAF2 WIL (SERAF3 WIL WIL))) (SERAF6 (SERAF4 WIL WIL))

SURAFIO

MAXMINEAS AS AS AS)

VERTICES(A1 A7 A2 A6 A5 A4 A3)

REGIONS(14 13 12 11)

BACKERGJND(+2)

528A*7

MAX4[4(#1 83 83 82)

VERTICES(83 92 81)

REG1048(+6 12)

BACKGROJND(12)

SGRAFS

MAX414(31 C3 C1 C2)

```
VERTICES(C3 C2 C1)
       REGIO48(#10 #2)
       BASKBR0J40(12)
8384F5
       MAX414(91 02 81 03)
        VERTICES(63 62 61)
        RESIGNS(#12 #11)
        BACKGROJ40(+12)
9984*4
        MAININ(41 K2 K4 K3)
        VERTICES(KS KE KI)
        RESIDUS(#10 #13)
        BACKGROJND(#101
 959473
        MAX414(01 D3 01 D2)
         VERTICES(04 D3 D2 01)
         RESIDUS(116 13)
         BACKSROJND(±3)
 5584*2
         MAX4144E1 E3 E1 E2)
         VERTISERIES ER ELI
         9EG1045(120 11)
         BASKSRDJADI:17
 528451
         MAX414(#1 F3 F1 F2)
         VERTICES(F4 F3 F2 F1)
         RES1048(112 81)
          8424883J4D(111
```

```
12
       ((1) A4 *4 45 *4 A6 13 A7 13 A2 11 A1) (16 82 16 83 15 81) (10 C2 10 C3 10 C1))
        (*) *4 *4 *3 *3 *1 *6 *6 *6 *10 *10 *10)
        (A4 A5 A6 A7 A2 A1 B2 B3 B1 C2 38 C1)
(((A1 A4) (44 A5) (A5 A5) (A6 A7) (A7 A2) (A2 A1)) ((31 B2) (82 B3) (83 B1)) ((C1 C2) (C2 C3 ) (C3 C1)))
        (((A4 R) (A5 R) (A6 R) (A7 R) (A2 R) (A1 R)) ((02 R) (03 R) (01 R)) ((C2 R) (C3 R) (C1 R)))
        ((*1 *4 *4 *3 *3 *1) (*6 *6 *6) (*10 *10 *10))
        ((A4 A5 A6 A7 A2 A1) (B2 B3 B1) (C2 C3 C1))
        (SERAFF SERAFS SERAFIC)
*1
        ((02 A2 03 A3 04 A4 02 A1) (020 E2 020 E3 020 E1) (012 F2 012 F3 012 F4 012 F1))
        (12 13 14 12 120 120 120 112 112 112 112)
        (A2 A3 A6 A1 E2 E3 E1 F2 F3 F4 FE)
        NIL
        (((A1 A2) (A2 A3) (A3 A4) (A4 A1)) ((E1 E2) (E2 E3) (E3 E1)) ((F1 F2) (F2 F3) (F3 F4) (F4 F1
111
        (((A2 L) (A3 L) (A4 L) (A1 L0) ((E2 R) (E3 R) (E1 R)) ((F2 R) (F3 R) (F4 R) (F1 R)))
        ((#2 #3 #4 #2) (#20 #20 #20) (#12 #12 #12 #12))
        ((A2 A3 A4 A1) (E2 E3 E1) (F2 F3 F4 F1))
```

(SGRAFZ SGRAF1)