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B.S., Rensselser Polytechnic Institute

SUBMITTED IN PARTIAL FULFILIMENT OF THE REQUIREMENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY

at the

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

September, 1964

Signature	Department of Mathematics, June 3, 1964
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Acknowledgements

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The work reported berein was supported in part by the MIT Computation Center, and in part by Project MAC, an MIT research program sponsored by the Advanced Research Projects Agency, Department of Defense, under Office of Newel Research Contract number Nonr-4102(01). Reproduction in whole or in part is permitted for any purpose of the United States Government. Associated preliminary research was supported in mental by Bolt, Beranek and Newman, Inc., Cambridge, Massachusetts, and in part by System Development Corporation, Santa Monica, California.

The author expresses him and to Marvin Minsky for his supervision of this thesis; to Victor Yngve and Murray Eden for their critical reading ref-sthermanuscript; M. To Herbert Simon, Noam Chomsky and Seymour Papert for and to his wife Eilean for her patience, encouragement and unfailing confidence without which this thesis could not have been completed.

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NATURAL LANGUAGE INPUT FOR A COMPUTER PROBLEM SOLVING SYSTEM

by

DANIEL G. BOBROW

Submitted to the Department of Mathematics on June 3, 1964 in partial fulfillment of the requirements for the degree of Doctor of Philosophy.

ABSTRACT

The STUDENT problem solving system, programmed in LISP, accepts as input a comfortable but restricted subset of English which can express a wide variety of algebra story problems. STUDENT finds the solution to a large class of these problems. STUDENT can utilize a store of global information not specific to any one problem, and may make assumptions about the interpretation of ambiguities in the wording of the problem being solved. If it uses such information, or makes any assumptions, STUDENT communicates this fact to the user.

The thesis includes a summary of other English language question-answering systems. All these systems, and STUDENT, are evaluated according to four standard criteria.

The linguistic analysis in STUDENT is a first approximation to the analytic portion of a semantic theory of discourse outlined in the thesis. STUDENT finds the set of kernel sentences which are the base of the input discourse, and transforms this sequence of kernel sentences into a set of simultaneous equations which form the semantic base of the STUDENT system. STUDENT then tries to solve this set of equations for the values of requested unknowns. If it is successful it gives the answers in English. If not, STUDENT asks the user for more information, and indicates the nature of the desired information. The STUDENT system is a first step toward natural language communication with computers. Further work on the semantic theory proposed should result in much more sophisticated systems.

Thesis Supervisor: Marvin L. Minsky

Title: Professor of Electrical Engineering

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CHAPTER I: INTRODUCTION

The aim of the research reported here was to discover how one could build a computer program which could communicate with people in a natural language within some restricted problem domain. In the course of this investigation, I wrote a set of computer programs, the STUDENT system, which accepts as input a comformable but restricted subset of English which can be used to express a wide variety of algebra story problems. The problems shown in Figure 1 illustrate some of the communication and problem solving capabilities of this system.

In the following discussion, I shall use phrases such as "the computer understands English". In all such cases, the "English" is just the restricted subset of English which is allowable as input for the computer program under discussion. In addition, for purposes of this report I have adopted the following operational definition of understanding. A computer understands a subset of English if it accepts input sentences which are members of this subset, and answers questions based on information contained in the input. The STUDENT system understands English in this sense.

A. The Problem Context of the STUDEST System.

In constructing a question-answering system, many problems are greatly simplified if the problem context is restricted. The simplification resulting from the restrictions embodied in the STU-DENT system, and the reasons these simplifications arise, will be discussed in detail in the body of this report.

The STUDENT system is designed to answer questions embedded

```
(THE PROBLEM TO BE SOLVED IS)
(THE DISTANCE FROM NEW YORK TO LOS ANGELES IS 3000 MILES.
IF THE AVERAGE SPEED OF A JET PLANE IS 600 MILES PER MOUR.)
FIND THE TIME IT TAKES TO TRAVEL FROM NEW YORK TO LOS ANGELES.
 BY JET 35
 (THE EQUATIONS TO BE SOLVED ARE)
 (EQUAL 68252) (TIME (IT / PRO) TAKES TO TRAVEL FROM NEW YORK TO LOS AMBELES BY JET))
 (EQUAL (AVERAGE SPEED OF JET PLANE) (QUOTIENT (THREE 600 (MILES))
 (EQUAL (MISTANCE FROM NEW YORK TO LOS ARBELES) (TIMES 3000
 (MILES) >>
 THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION
(USANG THE FOLLOWING RHOME RELATIONSHIPS)
((EGRAL EDISTANCE) (TIMES ESPEED) (TIME))) (RQUAL (DISTANCE)
(TIMES (MAS COMMUNITION) ENUMBER OF GALLONS OF GAR USED))))
 (ASSEMINE THAT)
 ((TIME) DE EQUAL TO (TIME GIT / PRO) TARES TO TRAVEL FROM NEW
YORK TO SEE ARGELES BY JETT)
 (ASSIMINE TRATT)
((DISTANCE) ME BOUAL TO (DESTANCE FROM NEW
 (THE TIME IT TAKES TO TRAVEL FROM HEN YORK TO LOS ANDELES BY
(THE PROBLEM TO BE SOLVED LE)

(THE PRICE OF A RADIO 28 M. 70 DOLLARS 2 IF THIS PRICE IS
15 PRICENT LESS THAN THE MARKED PRICE , RIND THE MARKED PRICE
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL GO2515 (MARKED PRICE))
(EQUAL (MRICE-OF RADIO) (TIMES
(EQUAL (PRICE OF RADIO) (TIMES 69.70 (DELLARS)))
```

(THE MARKED PRICE IS 82 DOLLARS)

```
(THE PROBLEM TO BE SOLVED IS)
 (THE SUM OF TWO NUMBERS IS 111 . ONE OF THE NUMBERS IS CONSECUTIVE
 TO THE OTHER NUMBER . FIND THE TWO NUMBERS .. )
TRYING POSSIBLE IDIOMS
(THE PROBLEM WITH AN "IDIONATIC SUSSTUTION IS)
(THE SUM OF ONE OF THE NUMBERS AND THE DTHER NUMBER IS 111
. ONE OF THE NUMBERS IS CRUSECUTIVE TO THE OTHER NUMBER . FIND
THE ONE OF THE NUMBER'S AND THE OTHER NUMBER .)
 (THE EQUATIONS TO BE SOLVED ARE)
 (EDUAL GO2522 (OTHER NUMBER))
 (ECHAL 902521 (ONE OF MUMBERS))
 (ECHAL CONE OF NUMBERS) (PLUS 1 (OTHER NUMBER)))
 (EQUAL (PLUS (ONE OF NUMBERS) (OTHER NUMBER)) 111)
 (THE ONE OF THE NUMBERS IS
 (THE OTHER NUMBER 18 655)
THE PROBLEM TO BE SOLVED (S)
(BIGL S FATHER S UNCUE IS TWICE AS OLD AS BALL S FATHER . 2
YEARS FROM NOW BILL S FATHER WILL BE 3 TIMBE AS OLD AS BILL
THE SON OF THEIR AGES 18 92 T FIRD BILL S AGE .)
 (THE EGENTIONS TO BE SOLVED ARE)
 (ECHAL 002533 ((BILL 7 PERSON) & ARE))
 (EGMAL (PLUS ((BIAL / PERSON) S (FATHERS/ PERSON) S (UNCLE
Y PERSON) S AGE) (PLUS ((B) LL / PERSON) S (FATHER / PERSON)
S AGE) ((B) LL / PERSON) S AGE)) 929
(EQUAL (PLUS ((BILL / PERSON) $ (FATHER / PERSON) $ AGE) 2)
(TIMES F (PLUS ((BILL / PERSON) $ AGE) 3)))
 (EQMAL ((BILL / BERSON) S (FATHER / PERSON) S (UNCLE / PERSON)
 S AGE) (TIMES 2 ((BILL / PERSON) S (FATHER # PERSON) S AGE)))
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(BILL S AGE IS

those shown in Figure 1. STUDENT does this by constructing from the English input a corresponding set of algebraic equations of all forms of

algebra atory specience in which to develop techniques which would be well allow a computer problem solving system to accept natural language sold by input. First, we know a good type of data structure in which to store information meeded to answer questions sinct his context; and the structure in which to namely, algebraic equations. There exist will kindus algorithms to the sold by the second structure in which we have the second structure in which to store information implicit in the equations of legislic legislic values for particular variables which examples the set of legislicits and a superior of second structure in the second structure in

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ten tost meg . Ogragora bestititations o sk mesu ett bistt et

In addition, I felt that there was a medageable subset of
English in which many types of algabra story problems were expressible. A large number of these story problems are systistic
in first year high school text books, and I have transcribed some
of them into SEDENT's input English of ince this question-answering task is one penformed by humans conductines the entire process
from input to solution of the equations was programed, we can obtain a measure of comparison between the performance of STORENT and
and of a human on the same problems. Its facts this program of an edge of
IEM 7094 enswers must questions that its comparison this comparison, one should menumber the base speed of the IM 7094; which
can perform over one hundred thousand additions per second.

B. Reasons for Wenting Natural Language Input

Why should one want to talk to a computer in English? There are many tongues the computer already understands such as FORTRAN, COMIT, LISP, ALGOL, COBOL, to name just a few. These serve adequately as communication media with the computer for a large class of problems. A more pertinent question is really, when is English input to a computer desirable?

English input is desirable, for example, if it is enecessary to use the computer for retrieval of information from a text in English. If a computer could accept English input, much information now recorded only in English would be available for computer use without need for human translation.

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A computer which understood English would be more accessible to any speaker of English, whether or not he was trained in any "foreign" computer tongue. For a single shot at the computer with a question not likely to be repeated, it would not be worthwhile to train the user in a specialized language. For fact retrieval, rather than document retrieval, English is a good vehicle for stating queries. For a good description of the differences between fact and document retrieval, see Cooper (12).

Programming languages are process oriented. One cannot describe a problem, only a method for finding a solution to the problem. A natural language is a convenient vehicle for providing a description of the problem itself, leaving the choice of processing to the problem solver accepting the input. In an extreme case, one would like to talk to the computer about a problem, with appropriate questions and interjections by the computer on assumptions it finds necessary, until the computer claims that the problem is now well formed, and an attempt at solution can be made.

factor in his intelligence, and if we can tearn how to make a computer understand a natural language, we will have taken a big step toward creating an "artificially intelligent" computer (32).

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C. Criteria for Evaluating Question-Answering Systems.

We have defined understanding in terms of an ability to answer questions in English. A number of question enswering systems have been built, and will be described in the next section. In this section, we shall give a number of criteria for evaluating question answering systems.

In many systems there is a separation of data input and question input. For all systems under consideration, the input questions are in English. The input data may be either invEnglish of in a prestructured format, e.g. a tree or milerarchy. The English data input may be used as a data base as is your mapped into a structured information store. Simmons, in his compedent survey of English question-answering systems (40), calls those systems using a structured information store "data base question-answerers", as opposed to "text-based question-answerers" which retrieve facts from the original text.

The extent of understanding of a quantion answering system can be measured along three different dimensions, syntactic, semantic and deductive. Along the syntactic dimension one can measure the grammatical complexity allowable in imput sentences. This may differ for the data input and question input. In the simplest case, one or some small number of fixed formet sentences are allowable inputs. Less restricted inputs may allow any sentences which can be parsed by a fixed grammar. The nearer this grammar is to a grammar

of all of English, the less restricted is the input. Because textbased question enswerers accept as input any string of words, without further processing, they have no syntactic limitation on input. However, the fact-retrieval program may only be able to abstract information from those portions of a text with less than some maximum syntactic complexity.

In data base question-answering systems, only certain relationships between words, or objects, may be representable in the information may be discarded or ignored.

This is a limitation in the sementic dimension of understanding.

In order to obtain answers to questions not explicitly given in the input, a question-answering system must have the power to perform some deductions. The structure of the information store may facilitate such deductive ability. The range of deductive ability is measured along the deductive dimension of sunderstanding. The structure of the information store may also aid in selecting only relevant material for use in the deductive question answering process, thus improving the efficiency of the system.

Another criteria closely related to the extent of numberstanding, is the facility with which the syntactic, semantic, or
deductive abilities of a question-answering system can be extended.

In the best case one could improve the system sliens any mimension
by talking to it in English. Alternatively, one might have to add
some new programs to the system, or at worst, any change might imply
complete reprograming of the entire system.

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An important additional consideration for means of a question-answering system is the amount of knowledge of the internal structure of the system that is necessary to use its Atbest one need not be aware of the information storage structure used at all.

At worst, as thorough knowledge of the daternal structure may be necessary to construct suitable input. To accommod adaption as accommod as a second construct.

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Another measure of the usefulness of a question-answering system is its ability to interact with the mear. In the worst case, a question is asked and sometime later an answer or report of failure is given. When the question cannot be answered, no indication is given of the cause of failure, nor does the system allow the person to give any help. This is typical of the operation of a number of Air Force query systems (Jay Keyser, personal communication). In the best case, the system will ask the user for specific help and accept suggestions of appropriate courses of action.

In this section we have given four criteria for evaluating question-answering systems. They may be summarized as follows:

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e rock a com la company of Association (Company) and a company of the company of

- 2) Facility for extending abilities (syntactic, semantic, deductive)
- 3) Need by user for knowledge of internal structure of
 - (2004) Extent of interaction with user the comment of the comment

D. English Language Question-Answering Systems

In this section, I shall give a critical summary of a number of English language question answering systems, butilizing the criteria outlined in the previous section. This discussion will provide a context for the section of the concluding chapter which summarizes the capabilities of the STUDENT system. For a description of the different syntactic analysis schemes mentioned below, see the survey by Bobrow (4).

1) Phillips. One of the earliest question answering systems was written in 1960 at MIT by Anthony Phillips (36) attains and at a way to base system which accepts sentences which can be parsed by a very simple context-free phrase structure grammar, of the type defined by Chomsky (8). Additional syntactic restrictions require that each word must be in only one grammatical class, and that a sentence has been exactly one parsing.

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A parsed sentence is transformed into a list of five elements, the subject, verb, object, time phrase, and place phrase in
the sentence. All other information in the sentence is disregarded.

Questions are answered by matching the list from the transformed
question against the list for each input sentence. When a match is
found, the corresponding sentence is given as an answer.

abilities would require repregramming the system. A questioner must be aware that the system utilizes a matching process which does not recognize synonyms, and therefore the sentence "The teacher eats lunch at noon." will not be recognized as an answer to the question "What does the teacher do at twelve o'clock?" When Phillips' system cannot find an answer, it reports only "(THE ORACLE DOES NOT KNOW)".

It provides for no further interaction with the user.

2) Green. Baseball is a question answering system designed and programmed at Lincoln Leberatories by Green; Welf; Chomsky and Laughery (19). It is a data base system in which the data is placed in memory in a prestructured tree format. The data consists of the dates, location, opposing teams and accres of some American League baseball games. Only questions to the system can be given in English.

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Questions must be simple sentences, with no relative clauses, logical or coordinate connectives. With these restrictions, the program will accept any question couched in words contained in a vocabulary list quite adequate for asking questions about baseball statistics. In addition, the parsing routine, based on techniques developed by Harris (21), must find a parsing for the question.

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a. අදහු රාජ්ජ වර මට මට පුද්ගුව මදුර <mark>මිහි මහ</mark>ම ්නවේ වීම හරවි ස්වර මණ්ර

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The questions must pertain to statistics about baseball games found in the information store. One cannot ask questions about extrema, such as "highest" score or "fewest" number of games won. The parsed question is transformed into a standard specification (or spec) list, and the question answering routine utilizes this canonical form for the meaning of the question. For example, the question "Who beat the Yankees on July 4?" would be transformed into the "spec list":

. Pa Team (Posing) = New York & Except of the Europe Continue of the Position of the Position

Because Baseball does not utilize English for data input, we cannot talk about deductions made from information implicit in several sentences. However, Baseball can perform operations such as counting (the number of games played by Boston, for example) and thus in the sense that it is utilizing several separate data units in its store, it is performing deductions.

Baseball's abilities can only be extended by extensive reprogramming, though the techniques utilized have some general applicability. Because the parsing program has a very complete grammar,
and the vocabulary list is quite comprehensive for the problem domain,
the user needs no knowledge of the internal structure of the Baseball program. No provision for interaction with the user was made.

3) Simmons. The SYNTHKY system is a text-based question answering system designed and programmed at SDC by Simmons, Klein and McConologue (41). The entire contents of anchildren's encyclopedia has been transcribed to magnetic tape for use as the information use store. An index has been prepared listing the location of all the content words in the text, i.e. including words like "worm," "est," and "birds," while excluding function words like "and," "the," and "of." All the content words of a question are extracted, and information rich sections of the text are retrieved, i.e. sections that are locally dense in content words contained in the question. For example, if the question were "What do worms eat?", with content words "worms" and "eat", the two sentences "Birds eat worms on the grass." and "Most worms quaually est grass." might be retrieved. At this time, the pregram performs a syntectic analysis of the quest and tion and of the sentences that may contain the answer A comparison of the dependency trees of the question and various sentences may eliminate some irrelevant sentences. In the example, "Birds eat worms on the grass" is eliminated because "worms" is the object of the verb "eats" instead of the subject as in the question. In the general case, the remaining sentences are given in some ranked order as possibly answering the question. The above and tubbed denote along the record

SYNTHEX is limited syntactically by its grammar to the extent that the syntactic analysis eliminates irrelevant statements. It makes no use of the meaning of any statements or words, and cannot deduce answers from information implicit in two or more sentences. Because the grammar is independent of the program, the syntactic ability of SYNTHEX can be extended relatively easily. However, before it can become a good question-answering system, some semantic abilities will have to be added.

SYNTHEX does not explicitly provide for interaction with the

with the few police two and the contract

user, but because it is implemented in the SDC time-sharing system

(9), a user may modify a previous question if the sentences re
trieved were not suitable. The mechanism for selection of sentences

must be kept in mind to get best results.

week cracitate his queries to questions on

acr⇔rue bruare alio edi .Tim ro (80) 4) Lindsay. While at the Carnegie Institute of Technology, Robert Lindsay (28) programmed the SAD SAM question-answering system. The input to the system is a set of sentences in Basic English, a subset of English devised by C.K. Ogden (35), which has a vocabulary of about 1500 words and a simple subset of the full English gram-The SAD part (Syntactic Appraiser and Diagrammer) of SAD SAM parses the sentence using a predictive analysis scheme. The Semantic Analyzing Machine (SAM) extracts from these parsed sentences information about the family relationships of people mentioned; it stores this information on a computer representation of the family tree, and ignores all other information in the sentence. For example, from the parsing of "Tom, Mary's brother, went to the store." Lindsay's program would extract the sibling relationship of Tom and Mary, place them on the family tree as descendants of the same mother and father, and ignore the information about where Tom went.

The information storage structure utilized by SAD SAM, namely, the family tree, facilitates deductions from information implicit in many sentences. Because a family relationship is defined in terms of the relative position (no pun intended) of two people in their family tree, computation of the relationship is independent of the number of sentences required to place in the tree the path between the individuals.

Extending the abilities of the SAD SAM system would require reprogramming. No provision is made for interaction with the user. No internal knowledge of the program structure is necessary if the

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user restricts his queries to questions of family relationships, and his language to Basic English.

5) Raphael. The SIR question-answering system (mnemonic for Semantic Information Retrieval) was designed by Bertram Raphael (38) at MIT. The SIR system accepts simple sentences in any of about 20 fixed formats useful for expressing certain relationships between objects. The semantic relationships extracted from these sentences are those of set membership, set inclusion, subpart, left-to-right position and ownership.

The information about the relationships between various objects is stored in a semantic network, where the nodes of the network are objects and the relationships are indicated by directed labeled links between nodes. For example, if the three sentences "John is a boy," "A boy is a person," and "Two hands are part of any person" were an input to SIR, four nodes labeled John, boy, person and hand would be created. Included in the network would be a link indicating set membership between John and boy, another with a label indicating set inclusion between boy and person, and a link indicating hand is a subpart of person, with the number of parts equal to 2.

Separate question-answering routines are used for questions involving different relationships. Each routine takes cognizance of the interaction of various relationships, and can deduce answers from the linked structure of the network, independent of the number of sentences which were necessary to set up these links. For example, by tracing the links from "John" to "hand," SIR would answer "YES" to the question "Is a hand part of John?"

The SIR system can interact with the user. For example, if

told that "A finger is part of a hand" and asked "How many fingers does John have?" it would reply "How many fingers per hand?" Then if it is told "Every hand has five fingers," it would ensuer the question with "The ensuer is 10".

Any extensions of the SIR system necessitate additional programming effort, though it is considerably easier to add new syntactic forms than new semantic relationships. Within the input limits of the 20 fixed format statements, the user need act know snything of the internal structure of the information storage structure.

E. Other Related Work.

In addition to those question-answering systems described above, a number of programs have been written to translate English statements into a logical notation to check the consistency of a set of statements, and the validity of logical enguments. In the sense that, given a corpus transformed to some logical potation, and another statement, a logic-based system can answer the question "Is this statement (or its negation) implied by the corpus?", such logic-based systems are question-answering systems.

Cooper (12) and Darlington (14) both have programs which translate a subset of English into the propositional calculus. Darlington is also working on programs which can translate English into the first order and second order predicate calculiant A difficult problem being considered by Darlington, in trying to handle implications of English statements in terms of their logical translation, is the determination of the proper level of enalysis for a particular problem - that is, whether to translate the input into second order predicate calculus where proofs are very difficulty or to try to use first order predicate or propositional calculus to prove the

theorem; and perhaps wind it logically insufficient at regal at dair than

At the National Bureau of Standards, Rirsch (22), Gohan (10) and Sillars (39) have designed a system in which pictures and Ringhish and language statements are converted to expressions in the first order predicate calculus products than check to see differ English language statements consistent with a given picture?

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English input; would make an excellent base for a question answering system. Fischer Black (2) has programmed a system which can do all of McCarthy's Advice-Taker problems, and can be adapted to accept a very limited subset of English. The deductive system in Black's section is program is equivalent to accept a program and accept a program and accept a program accept a program and accept a program accept a prog

Michael Goleman (11), at MIT, whote autermapaper describing and a program of his which sets up the equations for some types of algebra to bra story problems (also handled by STUDENE). To Some of the special and heuristics Truse for "age problems" were imprired by techniques he above invented. At the case we have an assume as a series a series as

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In his thesis, David Rucki (24) Identified Wintideas on how to construct this type of program, but again did not implement these ideas. He suggests methods for transformation of Anglish inputs ton aquations which would require much more information abpublished than its smedies size in the STUDENT program, and therefore were not applicable on this work to the STUDENT program considers words aspayabods, and diskers to without mention as little knowledge about the meaning of words as its compatible. One notify with the goal of finding a solution to the particular problems aga. 1887 and 1887 and 1888 an

A. Lawrege as Communication.

Language is an encoding used for road or one of words and the second of the second of

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CHAPTER II: SEMANTIC CENERATION AND ANALYSIS OF DISCOURSE

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The purpose of this chapter is to put the techniques of analysis embedded in the STUDENT program into a wider context, and indicate how they would fit into a more general language processing system. We will describe in this chapter a theory of sementic generation and analysis of discourse. STUDENT can then be considered a first approximation to a computer implementation of the analytic portion of the theory, with certain restrictions on the interpretation of a discourse to be analyzed. It will be evident from the theory why analysis is so greatly simplified by the imposed restrictions.

A. Language as Communication.

Language is an encoding used for communication between a speaker and a listener (or writer and reader). To transmit an "idea", the speaker must first encode it in a message, as a string in the transmission language. In order to understand this message, a listener must decode it, and extract its meaning. The coding of a particular message, M, is a function of both its global context and local context. The global context of a message is the background knowledge of the speaker and the listener, including some knowledge of possible universes of discourse, and codings for some simple ideas.

The local context of a message, M, is the set of messages temporally adjacent to M. M may refer back to earlier messages. M may even be just a modification of a previous message, and only understandable in this context. For example, consider the second sentence of the following discourse: "How many chaptains are in the U.S. Army? How many are in the navy?"

In order for communication to take place, the information map

of both the listener and the speaker must be approximately the same, at least for the universe of discourse; also the decoding process of the listener must be an approximate inverse of the encoding process of the speaker. Education in language is, in large part, an attempt to force the language processors of different people into a uniform mold to facilitate successful communication. We are not proposing that identity in detail is achieved, but as Quine so nicely put it (37):

"Different persons growing up in the same language are like different bushes triumed and trained to take the shape of identical elephants. The anatomical details of twigs and branches will fulfill the elephantine form differently from bush to bush, but the overall outward results are alike."

As a speaker transmits successive messages concerning some portion of his information map, the listener who understands the messages constructs a model of a "situation". The relation between the listener's model and the speaker's information map is that from each can be extracted the transmitted information relevant to the universe of discourse, including information deductible from the entire set of messages. The internal structure of the listener's model need bear no resemblance to that of the speaker, and may in general contain far less detail.

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B. Theories of Language.

According to Morris' theory of signs (33), the encoding and decoding of language can be stratified into three levels. The first level is the syntactic which deals with the relationships of signs to other signs. A syntactic analysis, treating words as members of classes of words, can yield structurings of messages which indicate common processing features. The second level, sementic analysis, is concerned with the relationships of signs to the things they denote.

A third level, pragmatic analysis, is concerned with the relationships between signs and their interpretations in terms of actions required.

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Our theory will deal with all three levels of analysis, with a primary emphasis on the relation of the semantic aspect of language to the generation of discourse.

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Many theories of syntax have been developed to describe the structure of English, and many of these have served as bases for computer programs which perform syntactic analysis. For a complete survey of such systems see the paper by Mobius (4) and Most all of these theories ignore the concepts of meaning and semantics. Because they ignore such an important sepact of language programs based on such theories often yield many possible structurings for a single sentence which is unambiguous to a person. With some use of meaning, many of the meaningless subiguous interpretations could be eliminated.

For a good discussion of why ambiguities arise in syntactic analysis as see Kuno and Octringen (25).

ទាំងការសារិយា (2000 នៅ នោះ នោះ នោះ និង និងសម្រាជិញ្ញា នៅ និងការសារិយា នៅ និងការបាន នៅ នៅ នៅ និងការបាន នៅ មានប

programs have been written which generate syntactically correct English sentences. In most cases, the sentences penerated are predominately meaningless nonsense. The coherent discourse generator of Klein (23) is the one exception I know. Klein utilizes an input text from which he extracts certain structural dependencies of the words in the input. He then generates sentences and before they are relieved for output, a postprodessor shocks to see if the words in the generated sentence satisfy structural dependencies consistent with those found in the input texts. However, even in Klein's program no attempt is made to use the denotive meaning of any word, except in so far as this meaning is reflected in its concentrances with other words in the input text.

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Misjeranos bus sesigare a aud in Some theories which do consider the problem of semantics are being developed now. Pendegraft (27) states that the programs being avoid developed at the Linguistic Research Center of the University of Texas are an explication of Morris' theory of signs. Though not yet implemented, the semantic analysis program will make use of a preliminary phrase structure syntactic analysis. A number of syntactic structures, with appropriate vocabulary items, will map onto single semantic constants, essentially indicating that these structures all have the same meaning. This gives a type of canonical form for structures in terms of their meanings, but does not utilize any explicit model of the world. No provision is made in the theory for deduction of information implicit in a set of sentences.

sapsa a di semerador buit year, sicomo di Lamb (26) also has proposed a stratificational theory of grammar, not yet implemented on a computer, in which successive levels of analysis are performed, with a final mapping of the input into structures in a "sememic" stratum of the language. In this sememic stratum tum are bundles of "sememes" or meanings, and indications of the relationships between different bundles. Different septences which mean the same thing should map into the same structure in this sememic stratum. Sememic structures are thus canonical representations of meaning. កស ស្គម ទីស ១៦១ **ស្រែកស្នាក់ស្នាប់ ស្គាល់ស** ការសំណើ

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The theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and analysis which we shall the theory of language generation and the shall the theory of language generation and the shall the shall be also the shall the shall be also the shal describe below is designed to handle what we call coherent discourse. A discourse is a sequence of sentences such that the meaning of the discourse-cannot be determined by intempleting each sentence independently, disregarding the other sentences in the discourse, interpretation of each sentence may be dependent on the local context, in the sense defined previously. A discourse is coherent if

it has a complete and consistent interpretation. Completeness implies that there is no substring within the discourse that does not have some interpretation in the model of the situation being built by the listener.

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A listener's ability to build a model of a situation from a discourse is dependent on information available to him from his general store of knowledge. Therefore it is quite possible for a discourse to seem coherent to one listener and not another. A writer, reading his own writing, may feel that he has generated a coherent sequence of sentences, but in fact, it is incoherent to all other readers. This is, unfortunately, not a rare occurrence in the scientific literature. Conversely, a listener who is a psychiatrist, for example, may find coherence in a sequence of remarks which a patient thinks are entirely unrelated.

The STUDENT system utilizes an expandable store of general knowledge to build a model of a situation described in a member of a limited class of discourses. The form of this model of a situation built by STUDENT will be discussed in detail in a later section of this chapter. As far as I know, STUDENT is the only computer implementation of a theory of discourse analysis now extant that maps a discourse into some representation of its meaning. When the theories of Lamb and Pendegraft are implemented, they should also be able to analyze this class of discourse (and others). Harris also talks about "discourse analysis," (20) but in his use of this term he specifically excludes the use of meaning, stating:

"The method [of discourse analysis] is formal, depending only on the occurrence of morphemes as distinguishable elements, and not upon the analyst's knowledge of the particular meaning of each morpheme."

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D. The Use of Kernel Sentences in Our Theory.

A basic postulate of our theory of language analysis is that a listener understands a discourse by transforming It into an equivalent (in meaning) sequence of simpler kernel sentences. A kernel sentence is one which the listener can understand directly; that is, one for which he knows a transformation into his information store. Conversely, a speaker generates a set of kernel sentences from his information map, and utilizes a sequence of transformations on this set to yield his spoken discourse. This set of kernel sentences is not invariant from person to person, and even varies for a single individual as he learns.

The use of kernel sentences in this way is controversial. However, the theory is proposed as a good framework for understanding and implementing language processing on a computer, not necessarily as a model for human behaviour. The usefulness of this theory as a psychological model is an empirical question. Skinner (42) has given some psychological justification for assuming the existence of a set of base sentences, and Chomsky (7) has discussed the linguistic merits of the use of the concept of kernel sentences. Despite this common concept of kernel sentences, in practice, our use of kernel sentences is different than that of Skinner or Chomsky. Our use of kernel sentences as a basis of a language is analogous to the use of generators in defining a group.

Although we are not proposing our theory as a basis for a psychological model, it has been useful, to avoid circumlocutions, to describe the theory in terms of the properties and actions of a hypothetical speaker and listener. All statements about speakers and listeners should be interpreted as referring to computer programs which respectively, generate and analyze coherent discourse.

E. Generation of Coherent Discourses as a server and iscourse is not and and

1) The Speaker's Model of the World. We assume that a speaker has some model of the world in his information store. We shall not be concerned here with how this model was built, or its exact form. Different forms for the model will be useful for different language tasks, but they must all have the properties described below.

The basic components of the model are a set of objects, $\{0_1\}$, a set of functions $\{P_1^n\}$, a set of relations $\{P_1^n\}$, a set of propositions $\{P_1^n\}$, and a set of semantic deductive rules. A function $\{P_1^n\}$ is a mapping from ordered sets of n objects, called the arguments of $\{P_1^n\}$, into the set of objects. The mapping may be multivalued and is defined only if the arguments satisfy a set of conditions associated with $\{P_1^n\}$. A condition is essentially membership in a class of objects, but is defined more precisely below. A relation $\{P_1^n\}$ is a special type of object in the model, and consists of a label (a unique identifier), and an ordered set of n conditions, called the argument conditions for the relation. Functions of relations are again relations.

An elementary proposition consists of a label associated with some relation, R₁ⁿ, and an ordered set of n objects satisfying the argument conditions for this relation. One may think of these propositions as the beliefs of a speaker about what relationships between objects he has noticed are true in the world. Complex propositions are logical combinations (in the usual sense) of elementary propositions.

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The semantic deductive rules give procedures for adding new propositions to the model based on the propositions now in the model. In addition to the ordinary rules of logic, these rules include axioms about the relationships of the relations in the model. The semantic

example, one such deductive rule for adding a proposition to the model might be (loosely speaking) "Look in the real world and see if it is true." These rules essentially determine how the model is to be expanded, and are the most complex part of a complete system. However, from our present point of view, we need only consider these rules as a black box which can extend the set of propositions in the model.

A closed question is a relational label for some R₁ and an ordered set of n objects. The answer to this quantion is affirmative if the proposition, consisting of this label and the n objects, is in the model (or can be added to it). If the negation of this proposition is in the model (or can be added), the enswer is negative.

Otherwise the answer is undefined.

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An open question consists of a relational label for an n-argument relation, \mathbb{R}^n_1 , and a set of objects corresponding to n-k of these arguments, where n-k-1. An answer to an open question is an ordered set of k objects, such that if these objects are associated with the k unspecified arguments of \mathbb{R}^n_1 , the resulting proposition is in the model or can be added to it. An open question may have no answers, or may have one or more answers. A condition is an open question with k-1, and an object satisfies a condition if it is an answer to the question.

2) Generation of Kernel Sentences. We have described the logical properties of the speaker's model of the world. We shall now consider how strings in a language, words, phrases, and sentences, are associated with the model. Corresponding to the set of objects

O₁ there is a set N₁ of strings (in English in our case), called the names of the objects. There is a many-one mapping from

[Nij] onto [0]. It is many-one because one object may have more than one name pleas. Frankfurter and hot dog both map back into the same object. in the model.

Recall that functions map n-tuples of objects into objects. Thus a function name and an in-tuple can specify an object. We can derive a name for this object from the function name and the 😘 🤲 💛 names of its m arguments. Associated with each function is at least one linguistic form, a string of words with blanks in which names of arguments of the function must be inserted. Examples of linguistic forms associated with a model are "number of a line", "father of ______, and "the child of _____and ____". There is a many-one mapping from the set of linguistic forms (1) onto the set of functions. Two examples of multiple linguistic forms for the same function are: "father of ______ tand the ____ tacher"; and "____plus ____" and "the sum of ____ and ___". Thus, if objects x and y have names "the first number" and "the second number! and associated with the function ! *! is the linguistic form "the product of ____ and ____", then the name of the object produced by applying the function " * " to x and y is "the product of the first number and the second number . A parsing of a name thus must decompose it into the part which is the linguistic form, and the parts which are names of arguments of the corresponding funcation tion. We shall call objects defined in terms of a function and an n-tuple of objects a functionally defined object, and those which are not functionally defined we shall call simple objects. Simple objects have simple names and functionally defined objects have composite names.

In addition to linguistic forms associated with functions, there are linguistic forms associated with relations. For an <u>n</u> argument relation there are <u>n</u> blanks in the linguistic form. Examples

of	relational	linguistic	forms are:	11	equals	",	
"_	gave	to _	" and	11	speaks".	It is	this
set	of linguis	stic forms,	correspondin	ng to the	relations	in the	model,
tha	at serve as	frames for	the kernel s	entences	តិស្តាទស្ត្រ L•	and Alberta	

In a manner similar to the way composite names are built, a kernel sentence corresponding to an elementary proposition is constructed by inserting names corresponding to each argument in the appropriate blank. Names may be simple or composite. An example of a kernel sentence for a proposition built from such a relational linguistic form is "John's father gave .3 times the salary of Bill to Jack." which contains the simple names "John", ".3", "Bill", and "Jack". It contains the functional linguistic forms "____'s father", "____times ____' and "salary of ____' and the relational linguistic form "____ gave _____ to ___'.

A kernel sentence corresponding to a complex proposition is constructed recursively from the kernel sentences corresponding to its elementary propositional constituents by placing them in the corresponding places in the linguistic forms " and ", " or ", "not " etc.

The kernel sentence corresponding to a closed question is constructed from the kernel of the corresponding proposition by placing it in the linguistic form "Is it true that ____?" For an open question, dummy objects are placed in the open argument positions to complete a propositional form. These dummy arguments have names "who", "what", "where", etc., and which dummy objects are used depends on the condition on that argument position. A question mark is placed at the end of the kernel sentence constructed in the usual way from the relational linguistic form and the names of the arguments.

In generating a coherent discourse, a speaker chooses a number of propositions in his model and/or some open or closed questions. He then uses linguistic information associated with the model to construct the set of kernel sentences corresponding to this set of chosen propositions. In the next section we will discuss how he generates his discourse from this set of kernels.

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3) Transformations on Kernel Sentences. The set of kernel sentences is the base of the coherent discourse. The meaning of a kernel sentence is the proposition into which it mans, and similarly, the meaning of any name is the object which is its image under the mapping. To this set of kernels we apply a sequence of meaning preserving transformations to get the final discourse. We use the word "transformation" in its broad general sense, not in the narrow technical sense defined by Chomsky (7).

There are two distinct types of transformations, structural and definitional. A structural or syntactic transformation is only dependent on the structure of the kernel string(s) on which it operates.

For example, one syntactic transformation takes a kernel in the active voice to one in the passive voice. Another combines two sentences into a single complex coordinate sentence.

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Stitute pronominal phrases for names. Pronominal phrases may be ordinary pronouns such as "he", "she", or "it". They may be referential phrases such as "the latter", "the former" or "this quantity".

They may also be truncations of a full name such as "the distance" of the distance between New York and Los Angeles". In cases where such pronominal reference is made, the coherence of the final discourse is dependent on the order in which the resultant strings appear.

The second type of transformation will definitionally like the second volves substitutions of linguistic strings and formation open appearance of a log pearing in the kernel destences. I for example sofor any appearance of a log "2 times" we may substitute "twice" sand for "hipstimes" substitute on a significant benefit and the string substitutions are transformations perform form substitution and meaningment of for example soof for a kernel sentence of the form " is y more than z" swhere z yell of and z are any names, some definitional transformation ican substitute.

Some transformations are optional, and some may be mandatory of if certain forms are present in the kernel setter Certain transformations are used by a speaker for atylistic purposes plan maximple, and also to emphasize certain objects; other syntactic transformations such any of as those which perform pronominal substitutions are used because consequent they decrease the depth of a construction distributions decrease defined by a construction distributions are defined by a construction distributions are defined by a construction distributions are said and account of the same defined by a construction distributions are said and construction distributions.

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Let us review the steps in the generation of a coherent discourse. The speaker chooses a set of propositions, the "ideas" he wishes to transmit to He then encodes them as clanguage strongs called kernel sentences in the manner described above. He then chooses are for sequence of structural and definitional transformations which are real and defined on this set of kernels or on the ordered set of sentences which result from applications of the first transformations of The discourse to a serve listener if he knows all the definitional transformations applied to a listener if he knows all the definitional transformations applied to a serve back into the same object, the listener must also map into a single object.

In order to clarify this theory, we show, in Appendix Equation is sample semantic generative grammar which will generate coherent dis-

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jects are numbers and the functions are the arithmetic operations of sum, difference, product and quotient. The only relation in the model is numerical equality. The transformations are described informally; further linguistic investigation is necessary before a formal notation for transformations can be decided upon Parallel to the grammar is a sample problem generated by utiliting this grammar. This problem is solvable by the STUDINT system.

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F. Analysis of Coherent Discourse 1000 sta confidence of the continued of

Generation of coherent discourse consists of two distinguishable steps. From propositions in the speaker's model of the world, he generates an ordered set of kernel sentences. He then applies a sequence of transformations to this kernel set. The resulting discourse is a coded message which is to be analyzed and decoded by a listener. The listener's problem can be loosely characterized as an attempt to answer the question, "What would I have meant if I said that?"

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To analyze a discourse the listener must find the set of kernel sentences from which it was generated; one way to do this is to find a set of inverse transformations which when applied to the input discourse yield a sequence of kernel sentences. The listener must then transform these kernel sentences to an appropriate representation in his information store. The appropriateness of a representation is a function of what later use the listener expects to make of the information contained in the discourse. The listener may simultaneously transform a given kernel sentence into a number of different representations in his information store. On a level of pragmatic analysis, statements require only storage of information. Questions and imperatives require appropriate responses from the

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listener. The difficulties in analysis dickotomize fato those at associated with finding the kernel sentences which are the base of 199891 the discourse, and those associated with transferring the kernel of the base of 199891 tences into representations in the discourse that we representations in the discourse of 1921 decreases and those associated with transferring the kernel of the base of 1921 decreases and the second of the discourse of the base of 1921 decreases and the second of the base of 1921 decreases and the second of the base of 1921 decreases and the second of the base of 1921 decreases and the second of the base of 1921 decreases and the second of the base of 1921 decreases and 1921 decreases

those wilth are part of a name. This diffifult tocause out

Mathews (29) has suggested that analysis can be performed by synthesis. A sequence of kernel sentences; and a sequence of kernel sentences; and the transformations are chosen; and the transformations are applied to the kernel nel sentences. The resulting discourse is matched against the input.

If they are the same, these kernel sentences and transformations give the required analysis of the input. Sifenot, a change is made so that the resulting discourse becomes more like the imput.

If the kernel sentences and transformations were chosen randomly, this method would obviously be too inefficient to work in any practical sense. However, by utilizing class within the impuration discourse with a choice of kernels and transformations can be greatly restricted. This technique of sentence analysis is being implemented in a program being written at MITRE by walker and Bartlett (43). This technique has the advantage that exactly the same grammar can be utilized for both analysis and generation of Discourse.

verse analytic transformations. If This a transformation that may be used in generating a discourse, and P₁(S) = S, where S and S are been sets of sentences, then the analytic transformation T₁. Is the in- a set verse of T₁ if and only if T₁(S) = S. The choice of which In- a set verse transformations to apply and the order of their application may again be restricted by utilizing heuristics tenterned with the section of the imputation of the imputation and the order of the interned with the section of the imputation of t

Once the base set of kernel sentences for a given dis-

course is determined, there remains the problem of tenterine representations of these semberces in the lifetener's determine at the representation and the major problem in accomplishing this steps involves the separation and of those words which are part of a name. This is difficult because the same word (lexicographic symbol) emay have munitiple uses in (ex language). Having separated the relational form from the arguments of this relations some can analyze the arguments of this relations some can analyze the representation terms of components which are functional displaying the terms of components which are functional linguistic forms and others and tinguistic forms a functional linguistic canonical separates for intermediations to the listener.

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imply that the representation of the discourse which information of the discourse which information of the discourse which information of the discourse which is information of the discourse of the sequentially described to the sequential of the sequential of the sequential of the discourse of the listenetic energy and the sequential of the listenetic energy and the sequential of the listenetic energy and the sequential of the sequential of

If the listener is only interested in certain sepects of the discourse, he need only preserve information or lemant to this tinteresty of and discourse the restain Within his area of interest the third his imade of is is properly to the specker's model in the measure that allowed as a second vant deductions which can be made by the speaker on the hasis of the second discourse can also be made by the listener of Quitaide chite area and second interest, the listener will be smaller to make any questions. We go yet call such restricted information stores limited deductive midels appeared.

The question-enswering programs of Lindesy and Raphael pand

the STUDENT system, said autilize limited deductive models. For the area of interest in each of these programs there was as "natural" and the representation for the information in the allowable input; of these are representations were natural in that they facilitated the deduction of implicit information. For example, Lindsay's family tree representation made it easy to compute the relationship of any two in- area dividuals in the tree; independent of the number of sentences necessary to build the tree.

Because the number of relations and functions expressible in the models in all three systems is very limited, there is a corresponding limitation on the number of linguistic forms that may appear in the input. This greatly simplifies the parsing problem discussed earlier, by restricting alternatives for words in the input text.

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H. The STUDENT Deductive Model.

The STUDENT system is an implementation of the analytic portion of our theory. STUDENT performs tertain inverse transformations to obtain a set of kernel sentences and then transforms these kernel sentences to expressions in a limited deductive model. Utilizing the power of this deductive model, within its limited domain of understanding, it is able to answer questions based on information implicit in the input information.

The analytic and transformational techniques utilized in STUDENT are described in detail in Chapter IV. We shall describe here the canonical representation of objects, relations and functions within the model. STUDENT is restricted to answering questions framed in the context of algebra story problems. Algebraic equations are a natural representation for information in the input.

The objects in the model are numbers, or numbers with an associated dimension. The only relation in the models is equality, and the only functions represented directly in the model are the arithment metic operations of addition, negation; multiplication; division and a and exponentiation. Other functions are defined in terms of these basic functions, by compostion, and/or substitutions of constants in the constant in the const for arguments of these functions. For example of the operation of the continued squaring is defined as exponentiation with "2" as the second argu- was an ment of the exponential function; subtraction is a composition of addition and negation. THE STATE OF THE PARTY OF THE PARTY OF THE PARTY.

Within the computer, a parenthesized prefix motation is used for a standard representation of the equations implicated the En- page glish input. The arithmetic coperation to be expressed is made the control of first element of a list, and the arguments of the function are succeeding list elements. The exact notation is given in Figure 2 below.

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Operation of	Infix Notation	Prefix Notation
Bquality	a: A r≢) B awrelinog TW	ES(EQUAL, A.B.)
		(PLUS A B C)
		(MINUS A)
		(PLUS A (MINUS B))
Multiplication		(TIMES A B) (TIMES A B C)
Division	A / B	(QUOTIENT A B)
Exponentiation	i jara <mark>k</mark> Barrias (h. 1966). 1944 - Barrias (h. 1966).	ri <mark>(REPTATB)</mark> Bosc Bydrosenic (18810) Es

Figure 2: Notation Within the STUDENT Deductive Model Fires within the model. STUDER) is restructed to restricted the

In the figure, A, B, and C are any representations of objects in the model, either composite or simple names. The usual infix notation for

these functional expressions is given for comparison. Because this is a fully parenthesized notation, no ambiguity of operational order arises, as it does, for example, for the unparenthesized infix notation expression A*B+C or its corresponding natural language expression "A times B plus C". Note also that in this prefix notation plus and times are not strictly binary operators. Indeed, in the model they may have any finite number of arguments, e.g. (TIMES A B C D) is a legitimate expression in the STUDENT model.

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Representations of objects in the STUDENT deductive model are taken from the input. Any string of words not containing a linguistic form associated with the arithmetic functions expressible in the model are considered simple names for objects. Thus, "the age of the child of John and Jane" is considered a simple name because it contains no functional linguistic forms associated with functions represented in STUDENT's limited deductive model. In a more general model it would be considered a composite name, and the functional forms "age of ____ " and "child of ____ and __ " would be mapped into their corresponding functions in the model.

Because such complex strings are considered simple names in the model, and objects are distinguished only by their names, it is important to determine when two distinct names actually refer to the same object. In fact, answers to questions in the STUDENT system are statements of the identity of the object referenced by two names. However, one of the names (the desired one) must satisfy certain lexical conditions. Most often this condition is just that the name be a numeral. For a more general model this restriction could be stated as requiring a simple name corresponding to some functionally defined name — because, for example, "number of _____" would be a functional linguistic form in the general model, and the only simple name for such an object would be the numeral corres-

ponding to this number of answer consists of a statement, of much and identity e.g. "The number of customers Ton sets is 162-"

The other lexical restriction on answers sometimes used in the STUDENT system is insistence that a certain unit (corresponding to a dimension associated with a number) appear in the demonstrated answer. For example, spans is the unit specified by the question "How many spans equals 1 fathom?", and the answer given by STUDENT is "1 fathom is 8 spans".

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ကြောင်းကြသည့် ကာသော ပြာလက်များခဲ့တယ်။ အသမားမှ အာရီကျွန်းခဲ့များသောတွင် ကြောင်းလေးသည်။ ကြောင်းကြောင်းသည်။ မြောင်းသည်များသည် အမျိုးသည် သည် သည်သည်။ သည်များသည်။

The deductive model described here is useful for enswering questions because we know how to extract implicit information from expressions in this model; that is, we know how to solve sets of algebraic equations to find numerical values which satisfy these equations. The solution process used in STIDENT is described in detail in Chapter VI. The transformation process, based on the theory described earlier, which STUDENT uses to go from an English input to this deductive model, is described in Chapter IV.

CHAPTER III: PROGRAMMING FORMALISMS AND LANGUAGE MANIPULATION

Almost any programming language is universal in the sense that with enough time, space, and work at the implementation, any computable function may be programmed. However, the task of programming can be made much easier by the proper choice of a higher level problem oriented programming language. The data to be manipulated by the STU-DENT system is symbolic, and of indefinite length and complexity. For this reason, a list-processing language was the most appropriate type of programming for this task. There are a number of such languages available, each having its own set of advantages and disadvantages. For a description of the general properties of list-processing languages, with a detailed comparison of four of the better known list-processing languages, see Bobrow and Raphael (5). Mostly because I knew it so well, I chose LISP (31) as the basic language for the STU-DENT system.

The LISP formalism is very convenient for programming recursive tasks such as the solving of a set of simultaneous equations. However, LISP does not provide any natural mechanisms for representing manipulation of strings of English words, another very important subtask in the STUDENT system. For this type of manipulation one would like to perform a sequence of steps involving operations such as recognizing a sentence format which fits a particular pattern, finding certain elements in a sentence by their context, rearranging a string of words, deleting, inserting, and duplicating parts of strings, and others.

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The LISP formalism cannot easily express such string manipulations, though each could be individually programmed. However, a formalism for just this sort of manipulation is the basis of the COMIT (45) programming system. Rules in this formalism can easily express very

complex string manipulations, and are easy to read and write. However, COMIT and LISP cannot be used simultaneously, and the problem context necessitates going back and forth between LISP-oriented tasks and COMIT-oriented tasks. Therefore, I adapted the COMIT rule notation for use in LISP, and constructed a LISP program called METROR which would interpret string transformation rules in this notation.

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In constructing the METEOR interpreter, I effectively extended the eloquence of the LISP programming language; that is, operations which could be done previously, but were askward to invoke could now be expressed easily. An extended language embodying the best features of COMIT and LISP could have been built from scratch, but it is much more economical to achieve such extensions by embedding. The advantages and disadvantages of language extension by embedding are discussed in detail by Bobrow and Weizenbaum (6).

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A. Specifying a Desired String Format.

METEOR has been described in detail elsewhere (3), but we include here a brief summary of its features. We do this because use of the notation makes later explication of the transformation process easier. In addition, if any ambiguity becomes apparent in the explanation of the operation of STUDENT, it may be resolved by consulting the listing of the STUDENT program in Appendix B. In this latter case, it may be necessary to consult the more complete specification of METEOR referenced above.

A METEOR program consists of a sequence of rules each specifying a string transformation and giving some control information. Let us first consider how a string transformation is specified. We shall call the string to be transformed the workspace. The workspace will be transformed by a rule only if it matches a pattern or format given

in the "left half" of the rule. This left half is a list of elementary patterns which specifies a sequence of items that must be matched in the workspace. For example, if the left half were "(THE BOY)" then a match would be found only if the workspace contained a "THE" immediately followed by "BOY". In addition to known constituents, one can match unknown constituents. The element \$1 in a left half will match any one workspace constituent. The left half "(A \$1 B \$2 C)" will match a contiguous substring of the workspace which consists of an A followed by exactly one constituent (specified by the marker "\$1") followed by a B followed by exactly 2 constituents (matching the "\$2") followed by an occurrence of a C.

Thus \$1 will match an element of the workspace with a specified context. If a left half would match more than one substring in the matching process.

We have discussed elementary patterns which match a fixed number of unknown constituents (e.g., "\$3" matches 3 unknown constituents). METEOR also has an elementary pattern element "\$" which matches an arbitrary number of unknown constituents. For example, the left half (THE \$ BOY) will match a substring of the workspace which starts with an occurrence of "THE" followed by any number of constituents (including zero) followed by an occurrence of "BOY". It would, for example, match a substring of the workspace "(GIVE THE GOOD BOY)" or of the workspace "(THE BOY HERE)". If the left half (\$ GLITCH \$3) matches a substring from the beginning of the workspace up to but not including the first occurrence of "GLITCH"; the pattern "GLITCH" matches this occurrence of "GLITCH"; in the workspace; and the elementary pattern "\$3" matches the 3 elements or constituents of the workspace immediately following GLITCH.

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Elements in the workspace may be tagged or subscripted to indicate special properties of this element; for example, one might have (HAVE/VERB) or (BOY/NOUN) as elements of the workspace. Such elements can be matched by name (using HAVE or BOY as pattern elements), or identified just by their subscripts (or by both). The elementary pattern (\$1/VERB) will match any single constituent which is a verb; that is, one which has the subscript "VERB", even if this constituent has other subscripts. Thus the left half (ALFRED (\$1/VERB) BOOKS) will match the substring (ALFRED (READS/VERB) BOOKS) in the workspace (NOW ALFRED (READS/VERB) BOOKS IN THE LIBRARY).

Other elementary pattern elements are provided, and new pattern elements can be defined and easily used within the METEOR system.

B. Specifying a Transformed Workspace.

We have discussed how a desired format can be specified through a prototype pattern, called a left half. If we try to match the workspace to a left half, but it is not in the format specified, we say the match has failed. If a substring of the workspace is in the specified format, the match is successful. When there is a successful match, we may wish to transform or manipulate the substring matched, or place in a temporary storage location, called a shelf, copies of segments of the matching substring. We shall now discuss the notation used for specifying such transformations, and storage of material.

A left half is a sequence of elementary patterns, and we associate with each elementary pattern a number indicating its position in this left half sequence. For example, in the left half (\$2 D \$ E), the first elementary pattern, \$2, would be associated with the number 1, the second, D, with 2, \$ with 3, and E with 4. If a match is successful, each elementary pattern element in the left half matches a

part of the substring of the workspace matched by this left half. The part matched by an elementary pattern can then be referenced by the number associated with this elementary pattern. For the left half given above, and the workspace (A B C D B A E G), the left-half match succeeds, and the substring (B C) may then be referenced with the number 1, the substring (D) by 2, (B A) by 3, and (E) by 4.

The transformed workspace is specified by the "right half" of a METEOR rule. This right half may be just the numeral 0, in which case the matched portion of the workspace is deleted. Otherwise this right half must be a list of elements specifying a replacement for the matched substring. Any numbers in this right-half list reference (specify) the appropriate part of the matched substring. Other items in the list may reference themselves, or strings in temporary storage, or functions of any referenceable substrings. In the example discussed above, if the right half were (3 2 M 2 H), then the matched portion of the workspace would be replaced by (B A D M D H), and the workspace would become (A B A D M D H G). Note that 1 and 4 were not mentioned in this right half and were therefore deleted from the workspace. Also 3 and 2 were in reverse order, and thus these referenced parts were inserted in the workspace in an order opposite to that in which they had appeared. 2 is referenced twice in this right half and therefore two copies of this referenced substring, "(D)" appear in the workspace. The elements M and H in this right half reference only themselves, and are therefore inserted directly into the ក់រាសរា<u>មលាក់ ១៩៩៦បាយ **១៧**លី (រញ្ញាពិ</u>សេវាឌ ១០០០១៩ភាពម workspace.

Using the right-half elements described, that is, numbers referencing matched substrings and constants (elements referencing themselves), one can express transformations of the workspace in which elements have been added to, deleted from, duplicated in, and rearranged in the workspace. Elements to be added to the workspace

thus far can only be constants. Let us consider some other possible right-half elements. They are all indicated by lists which start with special flags.

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The contents of any shelf (temporary storage list) can be referenced by a two element list with first element either *A (for All) or *N (for Next), and a second element, the shelf name. For example, (*A EQT) references the entire contents of a shelf named EQT. If this element appeared in a right half, the entire contents of that shelf would be placed in the corresponding place in the workspace. The first element of a shelf named SENTENCES could be put into the workspace by using the element (*N SENTENCES) in a right half.

The flag FN as the first member of a list serving as a right-half element indicates that the next member of this list is a function name, and the following ones are the arguments of this function. The value of the function for this set of arguments is placed in the workspace. In this way, any LISP function can be used within a METEOR rule.

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The flag *K indicates that the rest of the list following is to be evaluated as a right-half rule, and then is to be "compressed" into a list which will be a single element of the workspace. Thus, chunks which are longer, and have more complex structure than a single word can be treated as a single unit within the METEOR workspace string. The inverse operation is the expansion of a chunk so that all its components appear as individual constituents in the workspace. Expansion is indicated by a *E flag at the beginning of a right-half element list.

We have thus far discussed how the transformation of a string, here has been presented by the transformation of a string, here has been aliquidated by the beauty many the called the workspace, can be expressed in terms of a left half which have an expressed in terms of a left half which

pattern for a desired input format, and salright half which is a pattern for the desired output format. There is no reason to limit to one the number of outputs from a single left half match. In fact, a third section of a METEOR rule; called the Prouting section of for historinal reasons), allows the programmer to give any numbers of other er right halves, and place these referenced distance the beginning or end of any shelf (temporary storage list). The storage of such a "right half" is indicated in the routing section (by a list estarting with a *S or a *Q, followed by the shelf name, and followed by a right half pattern. The *S indicates that the preferenced material is to be Stored on the beginning of the named shalf a *Qoindicates that it should be Queued on the end of the shelfs a weed with a *N for retrieval, a shelf built up by a *Site a pushdown list; (a last-in-first-out list), and a shelf built up by a *Site a pushdown list; (a last-in-first-out list).

The only other significant sequence of a METEOR program that we have not yet touched on is the control setucture in section in Greinarily sife and the state has a name yeard has a sequence section in Greinarily sife and the section and the sequence set of the section and the sequence set of the section and the sequence set if the sette has season the sequence set in the sequence in the sequence of the sequence of the sequence of the sequence in the sequence of the sequence

Routing control can also be changed by a list of the form
"(*D namel name2)" in the routing section of a rule. After this list
is interpreted, any occurrence of namel in a "go-to" will be intered.

preted as a "go-to" containing "name2" is This datter feature allows
easy return from subroutines. The use of oleft-half-success or failure.

as a switch for the transfer of control makes it possible to write significant one rule loops.

A METEOR program is a sequence (list) of rules. Each rule is a list of up to six elements. The following is an example of a METEOR rule containing all six elements:

We shall briefly review the function of each of these six elements.

The first element of a METEOR rule is a name, and must be present in any rule. If no name is needed, the dummy name "*" can be used.

The second element is a "*" and is optional. When it is present it reverses the switch on flow of centrol, and transfer of control to the rule named in the "go-to" is made on left-half failure.

The third element is mandatory, and is a left-half pattern which is to be matched in the workspace. The fourth element is optional, and is a right-half pattern specifying the result in the workspace of the string transformation desired. The fifth (optional) element is called the routing section, and is a list flagged with a "/" as a first element. The remainder of the routing section is a sequence of lists which specify operations which place items on shelves or set "go-to" values. The final element is called the "go-to" and specifies where control is to be passed if a match succeeds (in the normal case). A "*" in this position specifies the next rule in sequence.

C. Summary.

In this chapter, we have briefly summarized the features of a language for string manipulation which has been embedded (by building

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the METEOR interpreter) in the general list-processing language LISP.

The ability to describe easily in METEOR the string transformations needed to process English sentences, and also use, where appropriate, the functional notation of the general list-processing language, LISP, was a great advantage in the programming effort involved in this study.

As a final illustration of the power of the combined METEOR-LISP language, we include a program for Wang's algorithm for proving theorems in the propositional calculus. This algorithm is described on pages 44-45 of the LISP manual (31), and a LISP program for the algorithm appears on pages 48-50. Figure 3 below contains the complete METEOR program for the algorithm, including definitions of four small auxiliary LISP functions used within the METEOR program.

In addition, the figure contains a trace of the program as it proves the theorem given after the first line containing "(THEOREM)". The other lines give the theorems that are proven by the algorithm as steps in the proof of this theorem. This METEOR program compares quite favorably in both size and understandability to the one given in the LISP manual, and to the one COMIT program which I have seen which performs the Wang algorithm.

Figure

for

Wang Algorithm

Definition of WANG in METEOR

```
DEFINE((
(WANG (LAMBDA (X) (METEOR (QUOTE (
       ((#P THEBREND)
(TOP
                                                     END)
(*
        (ARROW S (FN MAINCON NOT)) ((EN ARGONE (+16,3)) 1
(A2
       ((FN MAINCEN NET) S ARREST)
                                    (2 3 (FN ARSONE (4) 1
(B2
                                                  à. 19)
                                      CCEN AIR CEN WANG
(43
       (S ARROW S (FN MAINCON AND) S)
            (4K 1 2 3 (FN ARGINE (4K 4)) 5)) (FN WAR CHK
            1 2 3 (FN ARGTWS (+K 4)) 573)) 🗀
       ((FN MAINCON AND) S ARROW) ((FN ARGONE (+K 1))
(83
           FN ARGTHS (+K 1)) 2 3)
        (ARREN $ (FN MAINCEN ER)) (1 2 (FIE ARGENE CAK 3)
CAA
                                                  @ TOP)
           ) (FN ARGTWS (+K 3)))
       ($ (FN MAINCHN GR) $ ARROW $) - C(FN-ANC-CFN WANG
(B4
           (水 1 (FN ARGINE (水 2)) 3 4-5)) (FN NA NG (本
           1 (FN ARGTHS (4K 2)) 3 4 5)320
        CARROW & CFN MAINCON IMPLIESD) (CEN ARRONE CHE 3
(A5
           )) 1 2 (FN ARGTMB (+K-3)))
        CS CFN MAINCHN IMPLIESD S ARROW SO ECCEN AND CFN
(B5
           WANG COK 1 (FN ARGTHE COK 27) 3 4 539 (FN WANG
            (+K 1 3 4 5 (FN ARGONE (+K 2)))) 3 3 END)
        (S ARROW S (FN MAINCON EQUITO SE) (SFN AND TEFN
(A6
           WANG CHE 1 CFN ARGONE CHE 433 2 3 CFN ARGTHS C
           4K 4)) 50) (FN WANG (4K ) (EN ARGTWE-C4K 4) & 2
        3 (FH ARGONE CHE 4)) 525)) (FH ANGONE EQUI V) $ ARROW S) (FH ANG (FN)
(86
           WANG (AK (FM ARGENE (AK 2)) I FN ARGTHE (AK 2))
            3 4 5)) (FN WANG (+K 1.3 4 5 (FN ARSONE (+E 2
           )) (FN ARGTWS (+K 2)))))
                                                    EMD)
(FAILURE
           ($\) ((#K))
)) X)))
33
```

Auxiliary Functions for WANG

```
DEFINECC
(MAINCON (LAMBDA (WS CON) COND
      ((EQ CON (CAAR WS))(CONS(LIST(CAR WS))(CDR WS)))
      (TENIL) )))
(AN2 XLAMBDA (XXY) (COND XX Y) (T NIL))))
(ARGONE LAMBDA (X) (LISTICADAR X)))
(ARGINO (LAMBDA (X) (LIST(CADDAR X1)))
))
                 Trace of a Proof by WANG
(THEOREM)
((OR A (NOT B)) ARROW (IMPLIES (AND P Q) (EQUIV P Q)))
(THEOREM)
(A ARROY (IMPLIES (AND P Q) (EQUIV P Q)))
(THECKEM)
(A_(AND P Q) ARROY (EQUIVEP Q))
(THEOREM)
(A P Q ARROW (EQUIV P Q))
(THECKEM)
(A P Q P ARROW Q)
(THEOREM)
(A P E Q ARROW P)
(THECKEM)
((NOT B) ARROW (IMPLIES (AND P Q) (EQUIV P Q)))
( THEOREM)
(ARIDE B (IMPLIES CAND P Q) (EQUIV P Q)))
(THEOREM)
((AND Q) ARROW B (EQUIV P Q))
(THECKEM)
(P Q ARRON B (EQUIV P Q))
(THECREM)
(P Q P ARROW B Q)
(THEOREM)
(PQQ ARROY B P)
```

VALUE

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The STUDENT system consists of two main subprograms, called STUDENT and REMEMBER. The program called REMEMBER accepts and processes statements which contain global information; that is, information which is not specific to any one story problem. We shall discuss the processing and information storage techniques used in REMEMBER in the next chapter. A listing of the global information given to the STUDENT system may be found in Appendix C.

In this chapter, we shall describe the techniques embedded in the STUDENT program which are used to transform an English statement of an algebra story problem to expressions in the STUDENT deductive model. By implication we are also defining the subset of English which is "understood" by the STUDENT program. A more explicit description of this input language is given at the end of the chapter.

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A. Outline of the Operation of STUDENT.

To provide perspective by which to view the detailed heuristic techniques used in the STUDENT program, we shall first give an outline of the operation of the STUDENT program when given a problem to solve. This outline is a verbal description of the flow chart of the program found in Appendix A.

STUDENT is asked to solve a particular problem. We assume that all necessary global information has been stored previously. STUDENT will now transform the English input statement of this problem into expressions in its limited deductive model, and through appropriate deductive procedures attempt to find a solution. More specifically, STUDENT finds the kernel sentences of the input discourse, and trans-

forms this sequence of kernels into a set of simultaneous equations, keeping a list of the answers required, a list of the units involved in the problem (e.g. dollars, pounds) and a list of all the variables (simple names) in the equations. Then STUDENT invokes the SOLVE program to solve this set of equations for the desired unknowns. If a solution is found, STUDENT prints the values of the unknowns requested in a fixed format, substituting in "(variable Is value)" the appropriate phrases for variable and value. If a solution cannot be found, various heuristics are used to identify two variables (i.e. find two slightly different phrases that refer to the same object in the model). If two variables, A and B, are identified, the equation A = B is added to the set of equations. In addition, the store of global information is searched to find any equations that may be useful in finding the solution to this problem. STUDENT prints out any assumptions it makes about the identity of two variables, and also any equations that it retrieves because it thinks they may be relevant. If the use of global equations or equations from identifications leads to a solution, the answers are printed out in the format described above.

If a solution was not found, and certain idions are present in the problem (a result of a definitional transformation used in the generation of the problem), a substitution is made for each of these idioms in turn and the transformation and solution process is repeated. If the substitutions for these idioms do not enable the problem to be solved by STUDENT, then STUDENT requests additional information from the questioner, showing him the variables being used in the problem. If any information is given, STUDENT tries to solve the problem again. If none is given, it reports its instillity to solve this problem and terminates. If the problem is ever solved, the solution is printed and the program terminates.

B. Categories of Words in a Transformation.

The words and phrases (strings of words) in the English input can be classified into three distinct categories on the basis of how they are handled in the transformation to the deductive model. The first category consists of strings of words which name objects in the model; I call such strings, variables. Variables are identified only by the string of words in them, and if two strings differ at all, they define distinct variables. One important problem considered below is how to determine when two distinct variables refer to the same object.

The second class of words and phrases are what I call "substitutors". Each substitutor may be replaced by another string. Some substitutions are mandatory; others are optional and are only made if the problem cannot be solved without such substitutions. An example of a mandatory substitution is "2 times" for the word "twice". "Twice" always means "2 times" in the context of the model, and therefore this substitution is mandatory. One optional "idiomatic" substitution is "twice the sum of the length and width of the rectangle" for "the perimeter of the rectangle". The use of these substitutions in the transformation process is discussed below. These substitutions are inverses of definitional transformations as defined in Chapter II.

Members of the third class of words indicate the presence of functional linguistic forms which represent functions in the deductive model. I call members of this third class "operators". Operators may indicate operations which are complex combinations of the basic functions of the deductive model. One simple operator is the word "plus", which indicates that the objects named by the two variables surrounding it are to be added. An example of a more complex operator is the phrase "percent less than", as in "10 percent less than the marked price", which indicates that the number immediately preceding

the "percent" is to be subtracted from 100, this result divided by 100, and then this quotient multiplied by the variable following the "than".

Operators may be classified according to where their arguments are found. A prefix operator, such as "the square of...." precedes its argument. An operator like "....percent" is a suffix operator, and follows its argument. Infix operators such as "....plus...." or "....less than...." appear between their two arguments. In a split prefix operator such as "difference between....and....", part of the operator precedes, and part appears between the two arguments. "The sum of....and" is a split prefix operator with an indefinite number of arguments.

Some words may act as operators conditionally, depending on their context. For example, "of" is equivalent to "times" if there is a fraction immediately preceding it; e.g., ".5 of the profit" is equivalent to ".5 times the profit"; however, "Queen of England" does not imply a multiplicative relationship between the Queen and her country.

C. Transformational Procedures.

Let us now consider in detail the transformation procedure used by STUDENT, and see how these different categories of phrases interact. To make the process more concrete, let us consider the following example which has been solved by STUDENT.

(THE PROBLEM TO BE SOLVED IS)

(IF THE NUMBER OF CUSTOMERS TOM GETS IS <u>TWICE</u> THE <u>SQUARE OF</u>
20 <u>PER CENT</u> OF THE NUMBER OF ADVERTISEMENTS HE RUNS, AND THE NUMBER OF ADVERTISEMENTS HE RUNS IS 45, WHAT IS THE NUMBER OF CUSTOMERS TOM GETS Q.)

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Shown below are copies of actual printout from the STUDENT program, illustrating stages in the transformation and the solution of the problem. The parentheses are an artifact of the LISP programming language, and "Q." is a replacement for the question mark not available on the key punch.

The first stage in the transformation is to perform all mandatory substitutions. In this problem only the three phrases underlined (by the author, not the program) are substitutors: "twice" becomes "2 times", "per cent" becomes the single word "percent", and "square of" is truncated to "square". Having made these substitutions, STUDENT prints:

(WITH MANDATORY SUBSTITUTIONS THE PROBLEM IS)

(IF THE NUMBER OF CUSTOMERS TOM GETS IS 2 TIMES THE SQUARE

20 PERCENT OF THE NUMBER OF ADVERTISEMENTS HE RUNS, AND THE

NUMBER OF ADVERTISEMENTS HE RUNS IS 45, WHAT IS THE NUMBER

OF CUSTOMERS TOM GETS Q.)

From dictionary entries for each word, the words in the problem are tagged by their function in terms of the transformation process, and STUDENT prints:

(WITH WORDS TAGGED BY FUNCTION THE PROBLEM IS)

(IF THE NUMBER (OF / OP) CUSTOMERS TOM (GETS / VERB) IS

2 (TIMES / OP 1) THE (SQUARE / OP 1) 20 (PERCENT / OP 2)(OF/OP)

THE NUMBER (OF / OP) ADVERTISEMENTS (HE / PRO) RUNS, AND THE

NUMBER (OF / OP) ADVERTISEMENTS (HE / PRO) RUNS IS 45,

(WHAT / QNORD) IS THE NUMBER (OF / OP) CUSTOMERS

TOM (GETS / VERB) (QMARK / DLM))

If a word has a tag, or tags, the word followed by "/", followed by the tags, becomes a single unit, and is enclosed in parentheses. Some typical taggings are shown above. "(OF/OP)" indicates that "OF" is an operator and other taggings show that "GETS" is a verb, "TIMES" is an operator of level 1 (operator levels will be explained below), "SQUARE" is an operator of level 1, "PERCENT" is an operator of level 2, "HE" is a pronoun, "WHAT" is a question word, and "QMARK" (replacing Q.) is a delimiter of a sentence. These tagged words will play the principal role in the remaining transformation to the set of equations implicit in this problem statement.

The next stage in the transformation is to break the input sentences into "kernel sentences". As in the example, a problem may be stated using sentences of great grammatical complexity; however, the final stage of the transformation is only defined on a set of kernel sentences. The simplification to kernel sentences as done in STUDENT depends on the recursive use of format matching. If an input sentence is of the form "IF" followed by a substring, followed by a comma, a question word and a second substring (i.e. it matches the METEOR left half "(IF \$, (\$1/ QWORD(\$)") then the first substring (between the IF and the comma) is made an independent sentence, and everything following the comma is made into a second sentence. In the example, this means that the input is resolved into the following two sentences, (where tags are omitted for the sake of brevity):

"The number of customers Tom gets is 2 times the square 20 percent of the number of advertisements he runs, and the number of advertisements he runs is 45." and "What is the number of customers Tom gets?"

This last procedure effectively resolves a problem into declarative assumptions and a question sentence. A second complexity resolved

by STUDENT is illustrated in the first sentence of this pair. A coordinate sentence consisting of two sentences joined by a comma immediately followed by an "and" (i.e., any sentence matching the
METEOR left half "(\$, AND \$)") will be resolved into these two independent sentences. The first sentence above is therefore resolved
into two simpler sentences.

Using these two inverse syntactic transformations, this problem statement is resolved into simple kernel sentences. For the
example, STUDENT prints

(THE SIMPLE SENTENCES ARE) - enof toned) social tops bus self it the

(THE NUMBER (OF/OP) CUSTOMERS TOM (GETS / VERB) IS

2 (TIMES /OP 1) THE (SQUARE / OP 1) 20 (PERCENT / OP 2)

(OF / OF) THE NUMBER (OF / OF) ADVERTISEMENTS (HE / PRO)

RUNS (PERIOD / DIM)) THE SQUARE (SQUARE SQUARE) THE SQUARE (SQUARE SQUARE) THE SQUARE S

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example. Star the reference tragation come content of the content of the land and the star that the community of the content o

THE NUMBER (OF / OP) ADVERTISEMENTS (HE / PRO) RUNS IS 45 TO SECOND PROPERTY OF A SECOND PROP

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Each simple sentence is a separate list, i.e., is enclosed in parentheses, and each ends with a delimiter (a period or question mark).

Each of these sentences can now be transformed directly to its interpretation in the model.

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D. From Kernel Septences to Equations.

The transformation from the simple kernel sentences to equations uses three levels of precedence for operators. Operators of higher precedence level are used earlier in the transformation. Before utilizing the operators, STUDENT looks for linguistic forms associated with the equality relation. These forms include the copula "is" and transitive verbs in certain contexts. In the example we are considering, only the copula "is" is used to indicate equality. The use of transitive verbs as indicators of equality, that is, as relational linguistic forms, will be discussed in connection with another example. When the relational linguistic form is identified, the names which are the arguments of the form are broken down into variables and operators (functional linguistic forms). In the present problem, the two names are those on either side of the "is" in each sentence.

The word "is" may also be used meaningfully within algebra story problems as an auxiliary verb (not meaning equality) in such verbal phrases as "is multiplied by" or "is divided by". A special check is made for the occurrence of these phrases before proceeding on to the main transformation procedure. The transformation of sentences containing these special verbal phrases will be discussed later. If "is" does not appear as an auxiliary in such a verbal phrase, a sentence of the form "P1 is P2" is interpreted as indicating the equality of the objects named by phrases P1 and P2. No equality relation will be recognized within these phrases, even if an appropriate transitive verb occurs within either of them. If P1* and P2* represent the arithmetic transformations of P1 and P2, then "P1 is P2" is transformed into the equation

"(EOUAL P1* P2*)".

The transformation of P1 and P2 to give them an interpretation in the model is performed recursively using a program equivalent to the table in Figure 4. This table shows all the operators and formats currently recognized by the STUDENT program. New operators can easily be added to the program equivalent of this table.

In performing the transformation of a phrase P, a left to right search is made for an operator of level 2 (indicated by subscripts of "OP" and 2). If there is none, a left to right search is made for a level 1 operator (indicated by subscripts "OP" and 1), and finally another left to right search is made for an operator of level 0 (indicated by a subscript "OP" and no numerical subscript). The first operator found in this ordered search determines the first step in the transformation of the phrase. This operator and its context are transformed as indicated in column 4 in the table. If no operator is present, delimiters and articless (a) an and the) are deleted, and the phrase is treated as an indivisible entity, a variable.

In the example, the first simple sentence is

(THE NUMBER (OF/OF) CUSTOMERS TON (GETS/VERS) IS

2 (TIMES/OP 1) THE CSQUARE/OF 1) 20 (PERCENT/OP 2)

(OF/OP) THE NUMBER (OF/OP) ADVERTISEMENTS

(HE/PRO) RUNS (PERIOD/DIM)

This is of the form "P1 is P2", and is transformed to (EQUAL P1* P2*). P1 is "(THE NUMBER (OF/OP) CUSTOMERS TOM (GETS/VERB))". The occurrence of the verb "gets" is ignored because of the presence of the "is" in the sentence, meaning "equals". The only operator found is "(OF/OP)". From the table we see that if "OF" is immediately preceded by a number (not the word "number") it is treated as if it were the infix "TIMES". In this case, however, "OF" is not preceded by a number; the subscript OP, indicating that "OF" is an operator, is

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PLUSS 0 P1 PLUSS P2	(PLUS P1* P2*)		
MINUS 2 P1 MINUS P2	(PLUS P1* (NINUS P2*)) (c)		
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MINUSS 0 P1 MINUSS P2	(PLUS P1* (MINUS P2*)) (b)		
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A CONTRACTOR OF THE CONTRACTOR	(P1) (N100) P2) # 35, 25, 25, 25 (E) (C)		
PIRLESS 2 P1 K PERLESS P2	(P1((100-x)/100) P2)* (f) (g)		
SUM 0 SUM P1 AND P2 AND P3	(PLUS PI* (SUM P2 AND P3)*)		
	the step in the property are the property		
DIFFERRICE TO THE TANK OF DIFFERRICH SETS AND P2	(PLUG PAS (LONG 222)) and the residual		
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P1 OF P2	(P1 OF P2)*		
i and the lands	::3 oxi , , , 		
(a) If Pl is a phrase, Pl* indicates its interpretati	on in the model.		
(b) PLUSS and MINUSE exe identice to MINUS accept for preparence level.			
(c) When two posetble contents are indicated they ar	a shacked in the order shown.		
(d) SQUARE Pl-and SUM Pl ane idiometic shortenings of	SQUARE OF P1.		
(e) * outside a parenthesised expression indicates the to be transformed.	nt(the tentered phrase is		
(f) K is a number.	· 15.5 · · · · · · · · · · · · · · · · · ·		
(g) / and - imply that the indicated erithmetic operations are setuelly performed.			

Figure 4: Operators Recognized by STUDENT

and a complete such a such a such a such and a such and a such a such as the such as the such as the such as t The such as th

and the community of the second of the secon

stripped away, and the transformation process is represed on the or phrase with CEN no longer acting as an operator, and the respective process tion, no operators are found, and Elade the warrable and bus besseld as a second of the constant of the consta

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To the right of "IS" in the sentence is P2:

(2 (TIMES/OP 1) THE (SQUARE/OP 1) 20 (PERCENT/OP 2) (OF/OP)
THE NUMBER (OF/OP) ADMERITS HORNES: (HE/PRO) RUNS: (PERCENT/DEM)

for which STUDENT is to find a value. Also, this variable

The first operator found in Prince description operator of viewelling 2. From the tablerin Figure 4, we seed that other spector has the effect of dividing the number immediately preceding divided and the transformations of impacted one theorems of the remarkable in the example, the "... 20 (PERCENT) 2) (ef/ef) wary become THEGUTS verifies the constant of the first seed of the constant of the con

Continuing the transformation, the operators found are, in order, TIMES, SQUARE, OF and OFENAREMENTS handledwell-familiabled in the table. The "OF" in the context "... .2000 (OF/OP) THE" is treated as an infix TIMES, substituted by the state of the context "... .2000 (OF/OP) THE" the operator marking functionally and the context the context of the contex

(TIME 2 (EXPT (TIMES .2 (NUMBER OF ADVERTISEMENTS
(WE/PRO) RUMB(2) \$2 SOUTH OF THE RESTRICT OF

The transformation of the second sentence of the example is

done in a similar manner; candity telds (the sequestion of the caute signification of the sequestion of the example and full signification of the second sentence of the example is a signification of the second sentence of the example is a signification of the second sentence of the example is a signification of the example is a significant of the exam

The third sentence is of the form "What is P1?". It starts with a question word and is therefore treated specially. A unique variable, a single word consisting of an X of G followed by five integers, is created, and the equation (EQUAL Xnnnnn P1*) is stored. For this example, the variable X00001 was created, and this last simple sentence is transformed to the equation:

(EQUAL X00001 (NUMBER OF CUSTOMERS TOM (GETS/VERB))

编码表面编译 (1) ** (1) * (1) ** (2) ** (2) ** (3) ** (4

In addition, the created variable is placed on the list of variables for which STUDENT is to find a value. Also, this variable is stored, paired with Plathe untransformed right side, for use in printing out the answer. If a value is found for this variable, STUDENT prints the sentence (Pl is value) with the appropriate substitution for value. Below we show the full set of equations, and the printed solution given by STUDENT for the example being considered. For ease in solution, the last equations created are put first in the list of equations.

(THE EQUATIONS TO BE SOLVED ARE)

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(EQUAL X00001 (NUMBER OF CUSTOMERS TOM (GETS/VERB)))

(EQUAL (NUMBER OF ADVERTISEMENTS (HE/PRO) RUNS) 45)

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(EQUAL (NUMBER OF CUSTOMERS TOM (GETS/VERB)) (TEMES 2 (EXPT (TIMES 2000 (NUMBER OF ADVERTISEMENTS (HE/PRO) RUNS)) 2)))

The amount of the Control of the Control

(THE NUMBER OF CUSTOMERS TON GETS 18:162)

In the example just shown, the equality relation was indicated by the copula "is". In the problem shown below, solved by STUDENT, equality is indicated by the occurrence of a transitive week in the proper context.

(THE PROBLEM TO BE SOLVED IS)

(TOM HAS TWICE AS MANY FISH AS MARY HAS GUPPIES. IF MARY HAS

3 GUPPIES, WHAT IS THE NUMBER OF FISH TOM HAS Q.)

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL X00001 (NUMBER OF FISH TOM (HAS/VERB)))

(EQUAL (NUMBER OF GUPPLES (MARY/PERSON) (HAS/VERB)) 3)

(EQUAL (NUMBER OF FISH TOM (HAS/VERB)) (TIMES 2 (NUMBER OF GUPPLES (MARY/PERSON) (HAS/VERB))))

(THE NUMBER OF FISH TOM HAS IS 6)

The verb in this case is "has". The simple sentence "Mary has 3 guppies" is transformed to the "equivalent" sentence "The number of guppies Mary has is 3" and the processing of this latter sentence is done as previously discussed.

The general format for this type of sentence, and the format of the intermediate sentence to which it is transformed is best expressed by the following METEOR rule:

(* (\$(\$1/VERB) (\$1/NUMBER) \$) (THE NUMBER OF 4 1 2 IS 3) *)

ra i naza ki azirizinti kini i ni

This rule may be read: anything (a subject) followed by a verb followed by a number followed by anything (the unit) is transformed to a sentence starting with "THE NUMBER OF" followed by the unit, followed by the subject and the verb, followed by "IS" and then the number. In "Mary has 3 guppies" the subject is "Mary", the verb "has", and the units "guppies". Similarly, the sentence "The witches of

Firth brew 3 magic potions" would be transformed to serve the real transformed transformed

"The number of magic potions the witches of Firth brew is 3."

In addition to a declaration of number, a single-object transitive verb may be used in a comparative structure, such as exhibited in the sentence "Tom has twice as many fish as Mary has guppies."

The METEOR rule which gives the effective transformation for this type of sentence structure is:

(* (\$ (\$1/VERB) \$ AS MANY \$ AS \$ (\$1/VERB) \$)

(THE NUMBER OF 6 1 2 IS 3 THE NUMBER OF 10 8 9) *)

For the example, the transformed sentence is:

"The number of fish Tom has is twice the number of guppies Mary has!"

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Transformation of new sentence formats to formats previously "understood" by the program can be easily added to the program, thus extending the subset of English "understood" by STUDENT. In the processing that actually takes place within STUDENT the intermediate sentences shown never exist. It was easier to go directly to the model from the format, utilizing subroutines previously defined in terms of the semantics of the model.

The word "is" indicates equality only if it is not used as an auxiliary. The example below shows how verbal phrases containing "is", such as "is multiplied by", and "is increased by" are handled in the transformation.

(THE PROBLEM TO BE SOLVED IS)

(A NUMBER IS MULTIPLIED BY 6. THIS PRODUCT IS INCREASED BY 44.

THIS RESULT IS 66 . FIND THE NUMBER .)

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and the expression of the Mark Mark the control of

Harriet in Touris (2004) trepend in 19 20 2000 in 19 20 20

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL X00001 (NUMBER))

(EQUAL (PLUS (TIMES (NUMBER) 6) 44) 68)

(THE NUMBER IS 4)

The sentence "A number is multiplied by 6" only indicates that two objects in the model are related multiplicatively, and does not indicate explicitly any equality relation. The interpretation of this sentence in the model is the prefix notation product:

(TIMES (NUMBER) 6)

This latter phrase is stored in a temporary location for possible later reference. In this problem, it is referenced in the next sentence, with the phrase "TRIS PRODUCT". The important word in this last phrase is "TRIS" — STUDENT ignores all other words in a variable containing the key word "TRIS". The last temporarily stored phrase is substituted for the phrase containing "TRIS". Thus, the first three sentences in the problem shown above yield only one equation, after two substitutions for "this" phrases. The last sentence "Find the number." is transformed as if it were "What is the number Q.", and yields the first equation shown.

The word "this" may occur in a context where it is not referring to a previously stored phrase. Below is an example of such a context.

(THE PROBLEM TO BE SOLVED IS)
(THE PRICE OF A RADIO IS 69.70 DOLLARS . IF THIS PRICE IS
15 PERCENT LESS THAN THE MARKED PRICE.)

BE PROBLEM DE

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL X00001 (MARKED PRICE))

(EQUAL (PRICE OF RADIO) (TIMES 8499 (MARKED PRICE)))

(EQUAL (PRICE OF RADIO) (TIMES 69.70 (DOLLARS)))

(THE MARKED PRICE IS 82 DOLLARS)

In such contexts, the phrase containing "THIS" is replaced by the left half of the last equation created. In this example, STUDENT breaks the last sentence into two simple sentences, deleting the "IF". Then the phrase "THIS PRICE" is replaced by the variable "PRICE OF RADIO", which is the left half of the previous equation.

This problem illustrates two other features of the STUDENT program. The first is the action of the complex operator "percent less than". It causes the number immediately preceding it, i.e., 15, to be subtracted from 100, this result divided by 100, to give .85 (printed as .8499 due to a rounding error in floating point conversion). Then this operator becomes the infix operator "TDMES". This is indicated in the table in Figure 4.

This problem also illustrates how units such as "dollars" are handled by the STUDENT program. Any word which immediately follows a number is labeled as a special type of variable called a unit. A number followed by a unit is treated in the equation as a product of the number and the unit, e.g., "69.70 DOLLARS" becomes "(TIMES 69.70 (DOLLARS))". Units are treated as special variables in solving the set of equations; a unit may appear in the answer though other variables cannot. If the value for a variable found by the solver is

the product of a number and a unit, STUDENT concatenates the number and the unit. For example, the solution for "(MARKED PRICE)" in the problem above was (TIMES 82 (DOLLARS)) and STUDENT printed out:

(THE MARKED PRICE IS 82 DOLLARS)

There is an exception to the fact that any unit may appear in the answer, as illustrated in the problem below.

(THE PROBLEM TO BE SOLVED IS)
(IF 1 SPAN EQUALS 9 INCHES, AND 1 FATHOM EQUALS 6 FRET,
HOW MANY SPANS EQUALS 1 FATHOM Q.)

(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL X00001 (TIMES 1 (FATHOMS)))
(EQUAL (TIMES 1 (FATHOMS)) (TIMES 6 (FEET)))
(EQUAL (TIMES 1 (SPANS)) (TIMES 9 (INCHES)))

THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

(USING THE FOLLOWING KNOWN RELATIONSHIPS)
((EQUAL (TIMES 1 (YARDS)) (TIMES 3 (FEET))) (EQUAL (TIMES 1 (FEET)) (TIMES 12 (INCHES))))

(1 FATHOM IS 8 SPANS)

If the unit of the answer is specified, in this problem by the phrase "how many spans" — then only that unit, in this problem "spans", may appear in the answer. Without this restriction, STUDENT would blithely answer this problem with "(1 FATHOM IS 1 FATHOM)".

In the transformation from the English statement of the problem to the equations, "9 INCHES" became (TIMES 9 (INCHES)). However,

"I FATHOM" became "(TIMES 1 (FATHOMS))". The plural form for fathom has been used instead of the singular form. STUDENT always uses the plural form if known, to ensure that all units appear in only one form. Since "fathom" and "fathoms" are different, if both were used STUDENT would treat them as distinct, unrelated units. The plural form is part of the global information that can be made available to STUDENT, and the plural form of a word is substituted for any singular form appearing after "1" in any phrase. The inverse operation is carried out for correct printout of the solution.

Notice that the information given in the problem was insufficient to allow solution of the set of equations to be solved. Therefore, STUDENT looked in its glossary for information concerning each of the units in this set of equations. It found the relationships "I foot equals 12 inches." and "I yard equals 3 feet." Using only the first fact, and the equation it implies, STUDENT is then able to solve the problem. Thus, in certain cases where a problem is not analytic, in the sense that it does not contain, explicitly stated, all the information needed for its solution, STUDENT is able to draw on a body of facts, picking out relevant ones, and use them to obtain a solution.

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In certain problems, the transformation process does not yield a set of solvable equations. However, within this set of equations there exists a pair of variables (or more than one pair) such that the two variables are only "slightly different"; and really name the same object in the model. When a set of equations is unselvable, STUDENT searches for relevant global equations. In addition, it uses several heuristic techniques for identifying two "slightly different" variables in the equations. The problem below illustrates the identification of two variables where in one variable a pronoun has been substituted for a noun phrase in the stiller variable. This

Identification is made by checking all variables appearing before one containing the pronoun, and finding one which is didentical to this a department pronoun phrase, with a substitution of a string of any length for white the pronoun.

(THE PROBLEM TO BE SOLVED IS)

(THE NUMBER OF SOLDIERS THE RUSSIANS HAVE IS ONE HALF OF THE NUMBER OF CURS THE HAVE TO THE NUMBER OF CURS THEY HAVE TO SOLDIERS THEY HAVE IS

37000 . WHAT IS THE NUMBER OF SOLDIERS THEY HAVE QUE

BETWEEN NEW YORK AND BUSTON G.

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL X00001 (NUMBER OF SOLDIESS (THEY FROM (HAVE / VERB)))

E (EQUAL KRIMBER OF GUMS (THE TYPHO) PRIAVE PUBLIS) I A FOCO)

(EQUAL (NUMBER OF SOLDIERS SANISACION (GREVENER)) (TIMES .5000 (EQUAL (DICCOMPANION (DRECOMPANION CRECOMPANION CRECOMPANION CRECOMPANION (HILLES)))

THE EQUATIONS WERE INSURFICIENT TO EIRO A SQLUTION

(ASSIMULE THAT)
((NUMBER OF SOLDIERS (THEY/PRO) (HAVE/VERB)) IS EQUAL TO
(NUMBER OF SOLDIERS RUSSIANS (HAVE/VERB)))

(USING THE POLLOWING PAROPE MELATIONSHIPS)

(PART DECIMIEDA)

(THE NUMBER OF SOLDIERS THEY HAVE IS 3500)

with the effected working for this or hasem fit (Scharzett))

If two variables match in this fashion, STUDENT assumes the two variables are equal, prints out a statement of TAUT ONIMUSEA, as shown, and adds an equation expressing this equality to the set to be solved. The solution procedure is translated, switch this additional equation. In the example, the additional equation was sufficient to allow determination of the solution.

(THE NUMBER OF GALLONS OF CAS USED OF A TRIF BECKERN NEW TORK ANT BOSTON IS 18.00 GALLORED

the verse when storing word of electroneriable are not a local terminal

The example below is again a "non-analytic" problem. The first set of equations developed by STUDENT is unsolvable. Therefore, STUDENT tries to find some relevant equations in its store of global information.

(THE PROBLEM TO BE SOLVED IS)
(THE GAS CONSUMPTION OF MY CAR IS 15 MILES PER GALLON.
THE DISTANCE BETWEEN BOSTON AND NEW YORK IS 250 MILES.
WHAT IS THE NUMBER OF GALLONS OF GAS USED ON A TRIP
BETWEEN NEW YORK AND BOSTON Q.)

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL X00001 (NUMBER OF GALLONS OF GAS USED ON TRIP BETWEEN NEW YORK AND BOSTON))

(EQUAL (DISTANCE BETWEEN BOSTON AND NEW YORK) (TIMES 250 (MILES)))

(EQUAL (GAS CONSUMPTION OF MY CAR) (QUOTIENT (TIMES 15 (MILES)) (TIMES 1 (GALLONS))))

THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

(USING THE FOLLOWING KNOWN RELATIONSHIPS)

((EQUAL (DISTANCE) (TIMES (SPEED) (TIME))) (EQUAL (DISTANCE) (TIMES (GAS CONSUMPTION) (NUMBER OF CALLONS OF GAS USED))))

TO SAFETHER PRATERIES CHARGO VIEW FOR REFIELD

(ASSUMING THAT)

((DISTANCE) IS EQUAL TO (DISTANCE BETWEEN BOSTON AND NEW YORK))

(ASSUMING THAT)

((GAS CONSUMPTION) IS EQUAL TO (GAS CONSUMPTION OF MY CAR))

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(ASSUMING THAT)

((NUMBER OF GALLONS OF GAS USED) IS EQUAL TO (NUMBER OF GALLONS OF GAS USED ON TRIP BETWEEN NEW YORK AND BOSTON))

(THE NUMBER OF GALLONS OF GAS USED ON A TRIP BETWEEN NEW YORK AND BOSTON IS 16.66 GALLONS)

It uses the first word of each variable string as a key to its

glossary. The one exception to this rule is that the words "number of" are ignored if they are the first two words of a variable string. Thus, in this problem, STUDENT retrieved equations which were stored under the key words distance, gallons, gas, and miles. Two facts about distance had been stored earlier: "distance equals speed times time" and "distance equals gas consumption times number of gallons of gas used". The equations implicit in these sentences were stored and retrieved now — as possibly useful for the solution of this problem. In fact, only the second is relevant.

Before any attempt is made to solve this augmented set of equations, the variables in the augmented set are matched, to identify "slightly different" variables which refer to the same object in the model. In this example "(DISTANCE)", "(GAS GONSUMPTION)" and "(NUMBER OF GALLONS OF GAS USED)", are all identified with "similar" variables. The following conditions must be satisfied for this type of identification of variables Pland P2: 38 (12 Mag 12)

1) Plamust appears later in the problem than P2.

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2) Pl is completely contained in P2 in the sense that Pl is a contiguous substring within P2.

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ការធ្វើការស្ថិត ១៥៥៦១ ខ្លួន ១គីលី១៩៩ គ្រឿង 💨

This identification reflects a syntactic phenomenon where a truncated phrase, with one or more modifying phrases dropped, is often used in place of the original phrase. For example, if the phrase "the length of a rectangle" has occurred, the phrase the length" may be used to mean the same thing. This type of identification is distinct from that made using pronoun substitution.

In the example above, a stored schema was used by identifying the variables in the schema with the variables that occur in the problem. This problem is solvable because the key phrases "distance", "gas consumption" and "number of gallons of gas used" occur as

substrings of the variables in the problem. Since STUDENT identifiles each generic key phrase of the scheme with a particular variable of the problem, any scheme can be used only once in a problem.

Because STUDENT handles scheme in this at her fashion it cannot solve problems in which a relationship such as adistance equals speed times time" is needed for two different values of distance; speed; and time.

E. Possible Idiomatic Substitutions.

There are some phrases which have a dust character, depending on the context. In the example below, the phrase perimeter of a context rectangle becomes a wartable with now reference to its meaning, or definition, in terms of the length and with of the rectangle.

This definition is unneeded for solution (CREUPAD TO EMOLICE TO A CONTEXT.)

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problem to fact, and who second to be expended

(THE PROBLEM TO BE SOLVEDGES) 9 RELEASED AND THE PERIMETER OF A RECTANGLE AND THE PERIMETER OF A TRIANGLE IS 24 INCHES. IF THE PERIMETER OF THE RECTANGLE IS TWIGETHEFER OF THE TRIANGLE, WHAT! IS THE PERIMETER OF THE TRIANGLE, WHAT! IS THE PERIMETER OF THE TRIANGLE OF TH

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(THE EQUATIONS TO BE SOLVED ARE)

- - (EQUADOXOCOO 14 (PERIMETER OF STRIANGES)) Limbit in the sale of the

(BQUALT(PERIMETERSOF TREGRANGLE) (TIMES 23(PERIMETER OF PROMITE OF PROMITE OF TREATMENT OF THE PROMITE OF THE P

្សី២ ខណ្ឌី១៩៤ ខ្មាន់ **ខេ**ងក្រុម ខណ្ឌា**ន្ទនិង១៤១** ១ ខណៈ

(EQUAL (PLUS (PERIMETER OF RECTANGLE) (PERIMETER OF TRIANGLE))

(TIMES 24 (INCHES)))

(**Control of the control of the control

្សាស៊ី ទី ១៩ ខ្លួន ១០១៩ភូឌ្គ ដូច្នេះមាន ១ ខ្លួ<mark>ងកាលពី៩ ១០១</mark>៣០១៩ **១៤៤** បារ

(THE PERIMETER OF THE TRIANGLE IS 8 INCHES)

However, the following problem is stated in terms of the perimeter, length and width of the rectangle. Transforming the English into

(THE PROBLEM TO BE SOLVED AS) A TO A THE AREA SOLVED AS SOLVED AS SOLVED AS A CTHE LENGTH OF A RECTANGLE IS 8 INCHES MORE THAN THE WIDTH
OF THE RECTANGLE COME THAT FROM THE PERIMETERS OF THE RECTANGLE OF THE RECTANGLE OF THE RECTANGLE
IS 18 INCHES. FIND THE LENGTH AND THE WIDTH OF THE RECTANGLE

.) The production of the production of the rectangle of the rectangle of the rectangle of the rectangle. Silver to a fightight loster to (THE EQUATIONS TO BE SOLVED ARE) gi sin ma gi ganiyan i bili lar (EQUAL G02516 (WIDTH OF RECTANGLE)) The restriction cases if clarents were (EQUAL G02515 (LENGTH)) 'elgisioer o inc. outsai casi tuk (EQUAL (TIMES .5000 (PERIMETER OF RECTANGLE)) (TIMES 18 (INCHES))) (EQUAL (LENGTH OF RECTANGLE) (PLUS (TIMES & (INCHES)) (WIOTH niges: Aller of the rectangle. Who a OF RECTANGUES)) THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION (USING THE FOLLOWING KNOWN RELATIONSHIPS) ((EQUAL (TIMES 1 (REET)) (TIMES 12 (INCHES)))) ((LENGTH) IS EQUAL TO (LENGTH OF RECTANGLE)) THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION gram on a specific who salt convenies were distinct TRYING POSSIBLE IDIOMS (THE PROBLEM WITH AN IDIOMATIC SUBSTUTION IS) (THE LENGTH OF A RECTANGLE IS & INCHES MORE THAN THE WIOTH OF THE RECTANGLE . ONE HALF OF TWICE THE SUM OF THE LENGTH AND WIDTH OF THE RECTANGLE IS 18 INCHES . FIND THE LENGTH AND THE WIDTH OF THE RECTANGLE .) പെടു സ്രാധരമില് ഒത്ത് പ്രത്യേത്ത് നിരിച്ചി ច្រើន ប្រាស់ស្រាស់ ១៨ ១៣១ (THE EQUATIONS TO BE SOLVED ARE) Malbury to a soli (EQUAL G02518 (WIDTH OF RECTANGLE)) Substitution with the program of the control 200 (EQUAL G02517 (LENGTH)) . Hera in**i**d liest there does bet (EQUAL (TIMES (TIMES .5000 2) (PLUS (LENGTH) (WIDTH OF RECTANGLE))) (TIMES 18 (INCHES))) (EQUAL: (LENGTH, OF RECTANGLE) (PLUS (TIMES: 40 (INCHES)) (WIDTHOU) 6141 OF RECTANGLE))) Tanga isi ma galapa TORKETTE BOTH OF BASIC OF THE HELD THE EQUATIONS, WERE INSUFFICIENTS TO SEIND, AS SOLUTION OF SOME BOTH DOSS AS A SECOND OF STATES (USING THE FOLLOWING KNOWN RELATIONSHIPS) 1955311 ((EQUAL (TIMES 1 (FEET)) (TIMES 12 (INCHES)))) July of Little Pay 180 18 had been (ASSUMING THAT) ((LENGTH) IS EQUAL TO (LENGTH OF RECTANGLE)) Secure MESCHES IN

(THE LENGTH IS 13 INCHES)

(THE WIDTH OF THE RECTANGLE IS 5 INCHES)

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equations is not sufficient for solution. Neither retrieving and using an equation about "inches", the unit in the problem, nor identifying "length" with a longer phrase serve to make the problem solvable. Therefore, STUDENT looks in its dictionary of possible idioms, and finds one which it can try in the problem. STUDENT actually had two possible idiomatic substitutions which it could have made for "perimeter of a rectangle"; one was in terms of the length and width of the rectangle and the other was in terms of the shortest and longest sides of the rectangle. When there are two possible substitutions for a given phrase, one is tried first, namely the one STUDENT has been told about most recently. In this problem, the correct one was fortunately first. If the other had been first, the revised problem would not have been any more solvable than the original, and eventually the second (correct) substitution would have been made. Only one non-mandatory idiomatic substitution is ever made at one time, although the substitution is made for all occurrences of the phrase chosen.

In this problem, the idiomatic substitution made allows the problem to be solved, after identification of the variables "length" and "length of rectangle". The retrieved equation about inches was not needed. However, its presence in the set of equations to be solved did not sidetrack the solver in any way.

This use of possible, but non-mandatory idiomatic substitutions can also be used to give STUDENT a way to solve problems in which two phrases denoting one particular variable are quite different. For example, the phrase, "students who passed the admissions test" and "successful candidates" might be describing the same set of people. However, since STUDENT knows nothing of the "real world" and its value system for success, it would never identify these two phrases. However, if told that "successful candidates" sometime means "students

who passed the admissions test", it would be able to solve a problem using these two phrases to identify the same variable. Thus, possible idiomatic substitutions serve the dual purpose of providing tentative substitutions of definitions, and identification of synonomous phrases.

F. Special Heuristics.

The methods thus far discussed have been applicable to the entire range of algebra problems. However, for special classes of problems, additional heuristics may be used which are needed for members of the class, but not applicable to other problems. An example is the class of age problems, as typified by the problem below.

(THE PROBLEM TO BE SOLVED IS)

(BILL S FATHER S UNCLE IS TWICE AS OLD AS BILL S FATHER. 2

YEARS FROM NOW BILL S FATHER WILL BE 3 TIMES AS OLD AS BILL...
THE SUM OF THEIR AGES IS 92. FIND BILL S AGE .)

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(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL X00001 ((BILL / PERSON) S AGE))

(EQUAL (PLUS ((BILL / PERSON) S (FATHER / PERSON) S (UNCLE / PERSON) S AGE) (PLUS ((BILL / PERSON) S (FATHER / PERSON) S AGE) ((BILL / PERSON) S AGE))) 92)

(EQUAL (PLUS ((BILL / PERSON) S (FATHER / PERSON) S AGE) 2) (TIMES 3 (PLUS ((BILL / PERSON) S AGE)))

(BILL S AGE IS 8)

Before the age problem heuristics are used, a problem must be identified as belonging to that class of problems. STIDENT identifies age problems by any occurrence of one of the following phrases. "as old as", "years old" and "age". This identification is made immediately after all words are looked up in the dictionary and tagged by function.

After the special heuristics are used the modified problem is transformed to equations as described previously.

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The need for special methods for age problems arises because of the conventions used for denoting the variables, all of which are ages. The word age is usually not used explicitly, but is implicit in such phrases as "as old as". People's names are used where their ages are really the implicit variables. In the example, for instance, the phrase "Bill's father's uncle" is used instead of the phrase "Bill's father's uncle's age".

STUDENT uses a special heuristic to make all these ages explicit. To do this, it must know which words are "person words" and therefore, may be associated with an age. For this problem STUDENT has been told that Bill, father, and uncle are person words. They can be seen tagged as such in the equations. The " following a word is the STUDENT representation for possessive, used instead of "apostrophe - s" for programming convenience. STUDENT inserts a "S AGE" after every person word not followed by a "S" (because this "S" indicates that the person word is being used in a possessive sense, not as an independent age variable). Thus, as indicated, the phrase "BILL S FATHER S UNCLE" becomes "BILL S FATHER S UNCLE S AGE".

In addition to changing phrases naming people to ones naming ages, STUDENT makes certain special idiomatic substitutions. For the phrase "their ages", STUDENT substitutes a conjunction of all the age variables encountered in the problem. In the example, for "THEIR AGES" STUDENT substitutes "BILL S FATHER S UNCLE S AGE AND BILL S FATHER S AGE AND BILL S AGE". The phrases "as old as" and "years old" are then deleted as dummy phrases not having any meaning, and "will be" and "was" are changed to "Is". There is no need to

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preserve the tense of the copula, since the serve of the future or past tense is preserved in such prefix phrases as 2 years from now", or "3 years ago".

The remaining special age problem heuristics are used to process the phrases "in 2 years", "5 years ago" and "now". The phrase "2 years from now" is transformed to "in 2 years" before processing.

These three time phrases may occur immediately efter the mord "age", (e.g., "Bill's age 3 years ago") or at the beginning of the sentence. If a time phrase occurs at the beginning of the sentence, it implicitly modifies all ages mentioned in the sentence, except those followed by their own time phrase. For example, "In 2 years Bill's father's age will be 3 times Bill's age" is equivalent to "Bill's father's age in 2 years will be 3 times Bill's age in 2 years". However, "3 years ago Mary's age was 2 times Ann's age now". Thus prefix time phrases are handled by distributing them over all ages not modified by another time phrase.

After these prefix phrases have been distributed, each time phrase is translated appropriately. The phrase win 5 years causes 5 to be added to the age it follows, and "7 years ago" causes 7 to be subtracted from the age preceding this phrase. The word "now" is deleted.

Only the special heuristics described thus far were necessary to solve the first age problem. The second age problem, given below, requires one additional heuristic not previously mentioned. This is a substitution for the phrase "was when" which effectively decouples the two facts combined in the first sentence. For "was when", STUDENT substitutes "was K years ago" where K is a new variable created for this purpose.

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(THE PROBLEM TO BE SOLVED IS)
(MARY IS TWICE AS OLD AS ANN WAS WHEN MARY WAS AS OLD AS ANN IS NOW . IF MARY IS 24 YEARS OLD, HOW OLD IS ANN Q.)

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL X00008 ((ANN / PERSON) S AGE))

(EQUAL ((MARY / PERSON) S AGE) 24)

(EQUAL (PLUS ((MARY / PERSON) S AGE) (MINUS (X00007))) ((ANN / PERSON) S AGE))

(EQUAL ((MARY / PERSON) S AGE) (TIMES 2 (PLUS ((ANN / PERSON) S AGE) (MINUS (X00007)))))

(ANN S AGE IS 18)

In the example, the first sentence becomes the two sentences:
"Mary is twice as old as Ann X00007 years ago. X00007 years ago
Mary was as old as Ann is now." These two occurrences of time
phrases are handled as discussed previously. Similarly the phrase
"will be when" would be transformed to "in K years".

These decoupling heuristics are useful not only for the STUDENT program but for people trying to solve age problems. The classic age problem about Mary and Ann, given above, took an MIT graduate student over 5 minutes to solve because he did not know this heuristic. With the heuristic he was able to set up the appropriate equations much more rapidly. As a crude measure of STUDENT's relative speed, note that STUDENT took less than one minute to solve this problem.

G. When All Else Fails.

For all the problems discussed thus far, STUDENT was able to find a solution eventually. In some cases, however, necessary global information is missing from its store of information, or variables which name the same object cannot be identified by the heuris-

tics of the program. Whenever STUDENT cannot find a solution for any reason, it turns to the questioner for help. As in the problem below, it prints out "(DO YOU KNOW ANY MORE RELATIONSHIPS BETWEEN THESE VARIABLES)" followed by a list of the variables in the problem. The questioner can answer "yes" or "no". If he says "yes", STUDENT says "TELL ME", and the questioner can append another sentence to the statement of the problem.

(THE PROBLEM TO BE SOLVED IS)
(THE GROSS WEIGHT OF A SHIP IS 20000 TONS . IF ITS NET
WEIGHT IS 15000 TONS , WHAT IS THE WEIGHT OF THE SHIPS
CARGO Q.)

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THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

TRYING POSSIBLE IDIOMS

(DO YOU KNOW ANY MORE RELATIONSHIPS AMONG THESE VARIABLES)
(GROSS WEIGHT OF SHIP)
(TONS)
(ITS NET WEIGHT)
(WEIGHT OF SHIPS CARGO)

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4、多点等等(2**18)。 6.6**6年,**3**86.1998 6 (11.13年 86.13年 78.88年 78.884年 78.88年 78.88年 78.88年 78.88年 78.88年 78.88年 78.88年 78.88年 78.884年 78.8844 78.8844 78.8844 78.8845 78.8

yes TELL ME

(the weight of a ships cargo is the difference between the gross weight and the net weight)

THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

(ASSUMING THAT)

((NET WEIGHT) IS EQUAL TO (ITS NET WEIGHT))

(ASSUMING THAT)

((GROSS WEIGHT) IS EQUAL TO (GROSS WEIGHT OF SHIP))

(THE WEIGHT OF THE SHIPS CARGO IS 5000 TONS)

In this problem, the additional information typed in (in lower case letters) was sufficient to solve the problem. If it was not, the question would be repeated until the questioner said "no", or provides sufficient information for solution of the problem.

tions involves solving a quadratic equation; which is beyond the mathematical ability of the present STUDENT system. Note that in this case STUDENT reports that the equations were unsolvable, not simply insufficient for solution. STUDENT still requests additional information from the questioner. In the example, the questioner says "no", and STUDENT states that "I CANT SOLVE THIS PROBLEM" and terminates.

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(THE PROBLEM TO BE SOLVED IS)
(THE SQUARE OF THE DIFFERENCE BETWEEN THE NUMBER OF
APPLES AND THE NUMBER OF ORANGES ON THE TABLE IS EQUAL
TO 9. IF THE NUMBER OF APPLES IS 7, FIND THE NUMBER
OF ORANGES ON THE TABLE 30 OF THE

ានក្រស^កា នេះ ខែន^{ុស្ស} ពេទ្ធខ្លួន ពេល ពេ**វពេ**ធនៅសម្រេច សេវ

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL GO2515 (NUMBER OF ORANGES ON TABLE))

(EQUAL (NUMBER OF APPLES) 7) AREA (AND AREA OF APPLES)

(EQUAL (EXPT (PLUS (NUMBER OF APPLES) (MINUS (NUMBER OF ORANGES ON TABLE))) 2) 9)

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UNABLE TO SOLVE THIS SET OF EQUATIONS

TRYING POSSIBLE IDIOMS

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(NUMBER OF APPLES)

(NUMBER OF ORANGES ON TABLE)

((compared to the second of the second of the second (compared to the second of the se

I CANT SOLVE THIS PROBLEM

H. Summary of the STUDENT Subset of English.

The subset of English understandable by STUDENT is built around a core of sentence and phrase formats, which can be transformed into expressions in the STUDENT deductive model. On this basic core is built a larger set of formats. Each of these are first transformed into a string built on formats in this basic set and then this string is transformed into an expression in the deductive model. For example, the format (\$ IS EQUAL TO \$) is changed to the basic format (\$ IS \$), and the phrase "IS CONSECUTIVE TO" is changed to "IS 1 PLUS". The constructions discussed earlier involving single object transitive verbs could have been handled this way, though for programming convenience they were not.

The complete list of the basic formats accepted by the present STUDENT system can be determined by examining (in the pregram listing in the Appendix) the rules from the one labeled OPFORM to the one labeled QSET. The METEOR rules of the STUDENT program precisely specify the acceptable formats, and their translations to the model, but I shall try to summarize the basic and extended formats here. Implicitly assumed in the syntax is that any operator appears only within one of the contexts specified in the table given in Chapter II, and only the operators given in the table appear. The listing of STUDENT starting at the rule labeled IDIOMS gives translations of additional operators to those in the table.

The basic linguistic form which is transformed into an equation is one containing "is" as a copula. The phrases "is equal to" and "equals" are both changed to the copula "is". The auxiliary verbal constructions "is multiplied by", "is divided by" and "is increased by" are also acceptable as principal verbs in a sentence. As discussed in detail earlier, a sentence with no occurrence of "is" can have as a main verb a transitive verb immedi-

phrase which is the direct object of the verb, as in "Mary has three guppies". This type of transitive verb can also have a comparative structure as direct object, e.g., "Mary has twice as many guppies as Tom has fish".

This completes the repertoire of declarative sentence formats. Any number of declarative sentences may be conjoined, with ", and" between each pair, to form a new (complex) declarative sentence. A declarative sentence (even a complex declarative) can be made a presupposition for a question by preceding it with "IF" and following it with a comma and the question.

Questions, that is, requests for information from STUDENT, will be understood if they match any of the patterns:

(WHAT ARE \$ AND \$)

(FIND \$ AND \$)

(HOW MANY \$ DO \$ HAVE)

(HOW MANY \$1 IS \$)

This completes the summary of the set of input formats presently understood by STUDENT. This set can be enlarged in two distinct ways. One is to enlarge the set of basic formats, using standard subroutines to aid in defining, for each new basic format, its interpretation in the deductive model. The other method of extending the range of STUDENT input is to define transformations from new input formats to previously understood basic or extension formats. In the next chapter we discuss how this latter type of extension can be performed at run time, using the STUDENT global information storage facility. A combination of English and METEOR elementary pattern

elements can be used to define the input format and transformation, well

Even if a story problem is stated within the subset of English acceptable to STUDENT, this is not a guarantee that this problem can be solved by STUDENT (assuming it to be solvable). Two phrases designed cribing the object must be at worst only "slightly different" by the criteria prescribed earlier. Appropriate global information must be available to STUDENT, and the algebra involved must not extinct ceed the abilities of the solver. However, though most algebra story as problems found in the standard texts cannot be solved by STUDENT exactly as written, the author has usually been able to find some maraphrase of almost all such problems, which is solvable by STUDENT. Appendix Descentains a fair sample of the range of problems that can be handled by the STUDENT system.

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I. Limitations of the STIDENT Subset of Englished to the state of the

be used to enable a computer program to accept and penderstand a discontinuous fairly extensive subset of English for a fixed semantic base. However, the current STUDENT system is experimental and has a number of limitations.

matching. If each format is used to express the meaning understood by STUDENT, no misinterpretation will occur. However, these formats occur in English discourse even in algebra story problems, in semantic contexts not consistent with STEDENT's interpretation of these formats mats. For example, a sentence matching the format "(\$, AND \$)" is always interpreted by STEDENT as the conjunction of two declarative statements. Therefore, the sentence "You has 2 applies; I beneaus, and 4 pears." would be incorrectly divided into the two declarative

"Tom has 2 apples, 3 bananas." and "4 pears."

Each of the operator words shown in Figure 4 must be used as an operator in the context as shown or a misinterpretation will result. For example, the phrase "the number of times I went to the movies" which should be interpreted as a variable string will be interpreted incorrectly as the product of the two variables "number of" and "I went to the movies", because "times" is always considered to be an operator. Similarly, in the current implementation of STUDENT, "of" is considered to be an operator if it is preceded by any number. However, the phrase "2 of the boys who passed" will be misinterpreted as the product of "2" and "the boys who passed".

These examples obviously do not constitute a complete list of misinterpretations and errors STUDENT will make, but it should give the reader an idea of limitations on the STUDENT subset of English. In principle, all of these restrictions could be removed. However, removing some of them would require only minor changes to the program, while others would require techniques not used in the current system.

For example, to correct the error in interpreting "2 of the boys who passed", one can simply check to see if the number before the "of" is less than 1, and if so, only then interpret "of" as an operator "times". However, a much more sophisticated grammar and parsing program would be necessary to distinguish different occurrences of the format "(\$, AND \$)", and correctly extract simpler sentences from complex coordinate and subordinate sentences.

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Because of limitations of the sort described above, and the fact that the STUDENT system currently occupies almost all of the computer memory, STUDENT serves principally as a demonstration of

the power of the techniques utilized in its construction. However, I believe that on a larger computer one could use these techniques to construct a system of practical value which would communicate well with people in English over the limited range of material understood by the program.

CHAPTER V: STORAGE OF GLOBAL INFORMATION

This algebra problem-solving system contains two programs which process English input. One is the problem thus far discussed. STUDENT, which accepts the statement of an algebra story problem and attempts to find the solution to the particular problem. STUDENT does not store any information, nor "remember" anything from problem to problem. The information obtained by STUDENT is the local context of the question.

The other program is called REMEMBER and it processes and stores facts not specific to any one problem. These facts make up STUDENT's store of "global information" as opposed to "local information" specific to the problem. This information is accepted in a subset of English which overlaps but is different from the subset of English accepted by STUDENT. REMEMBER accepts statements in certain fixed formats, and for each format the information is stored in a way that makes it convenient for retrieval and use within the STUDENT program. Some information is stored by actually adding METEOR rules to the STUDENT program, and other information is stored on property lists of individual words, which are unique atoms in the LISP system.

The following are the formats currently understood by REMEMBER, and the processing and information storage techniques used for each one:

1. Format: P1 EQUALS P2.

Example: DISTANCE EQUALS SPEED TIMES TIME

Processing: The sentence is transformed into an equation in the same way it is done in STUDENT. This equation is stored on the property lists of the atoms which are the first words in each variable. In the example, the equation with the second of the second of

"(EQUAL (DISTANCE) (TIMES (SPEED) (TIME)))"

is stored on the property lists of "DISTANCE", "SPEED" and "TIME".

If any one of these words appears as the initial word of a variable in a problem, and global equations are needed to solve this problem, this equation will be retrieved.

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2. Format: P1 IS AN OPERATOR OF LEVEL K
Example: TIMES IS AN OPERATOR OF LEVEL 1

Processing: A dictionary entry for Pl is created, with subscripts of OP and K. For TIMES, the dictionary entry (TIMES / OP I) is created. The dictionary entry for any word is placed on the property list of that word (atom), and is retrieved and used in place of any occurrence of that word in a problem.

3. Format: P1 IS AN OPERATOR
Example: OF IS AN OPERATOR

Processing: A dictionary entry is created for Pl with the subscript OP. The entry for OF is (OF/OF).

4. Format: Pl IS A P2
Example: BILL IS A PERSON

Processing: A dictionary entry is created for Pl with subscript P2. The entry for BILL is (BILL/PERSON).

5. Format: Pl IS THE PLURAL OF P2

Example: FEET IS THE PLURAL OF FOOT

Processing: P2 is stored on the property list of P1, after the flag SING; the word P1 is stored on the property list of P2 after the flag PLURAL. Thus FEET is stored after PLURAL on the

property list of the atom FOOT. The state of the state of

6. Format: P1 SOMETIMES MEANS P2 HA, Add to the second

Example: TWO NUMBERS SOMETIMES MEANS ONE NUMBER AND THE OTHER NUMBER.

Processing: The STUDENT program is modified so that an idiomatic substitution of P2 for P1 will be made in a problem if it is otherwise unsolvable. All such "possible idiomatic substitutions" are tried when necessary, with the last one entered being the first one tried. The STUDENT program is modified by the addition of four new METEOR rules. Since P1 and P2 are inserted as left and right halves of a METEOR rule, they need not contain only words, but can use the METEOR elementary patterns to specify a format change instead of just a phrase change. For the example shown, the rules added to the STUDENT program, as listed in Appendix B, are the rule labeled CO2510, the rule following that one, the rule labeled GO2511 and the rule following it.

7. Format: P1 ALWAYS MEANS P2

Example: ONE HALF ALWAYS MEANS 0.5

Processing: The program STUDENT is modified so that if Pl occurs, a mandatory substitution of P2 for Pl will be made in any problem. The <u>last</u> sentence in this format processed by REMEMBER will be the <u>first</u> mandatory substitution made. Thus "one always means 1" <u>followed</u> by "one half always means 0.5" will cause the desired substitutions to be made; if these sentences were reversed no occurrence of "one half" would ever be found since it would have been changed to "l half", by mandatory substitution of l for one.

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For each sentence in this format processed by REMEMBER, a new METEOR rule is added to the STUDENT program, immediately following the rule named IDIOMS. The format of the METEOR rule added

is (* (P1) (P2) IDIOMS) where P1 and P2 are the strings In the sentence processed. Thus by using a combination of English and METEOR elementary patterns and reference numbers in P1 and P2, one can add a new format of sentence to the STODAY repertoire? For example, the following statement was processed by manuals to willow STODAY to be "understand" (properly transform) a sentence in which the main verb was "exceeds":

Prophed to al LISEE MARTO MICHOLOGIC REMAIN SYAUTA & YE STEEDER \$) be through a cothe more knowledgeable.

This permanently extended the STUDENT input subset of English,
while avoiding the necessity of actually editing and changing the
STUDENT program. The subset of modifications and at TOS befords, one can assure and one can assure the contract of the subset of the subset

The global information stored for STUDENT ranged from equations to format changes to plural forms. Again, elle compatible use as of the general list of the general list of processing processing operations in TISP facilitated programming of processing, and storage and retrieval of this wide range of information. It is Appendix of the STUDENT system.

The engine of SOLVE is dependent on western the term of some transfer grown real and solved ion the variables and real form of the second became the solution from the contract product of the value USSOLVARUE. If an intension is present the formula with the value USSOLVARUE. If an intension is present the not energy a solution in family state of a transfer of paths. The however, a solution in family state of a transfer element of whose value is a variable of paths. It is a variable whose value as family and a second of equals of the first element of the family of the second of equals of the first element of the first of the second of each of the second of the first element of the second of each of the second of the first element of the second of the first of the second of the se

CHAPTER VI: SOLUTION OF SIMULTANEOUS EQUATIONS

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This chapter contains a description of the LISP program used by STUDENT to solve sets of simultaneous equations. The definitions of the three top level functions SOLVE, SOLVER and SOLVEl are shown in the figure at the end of this chapter. This description of these functions is essentially independent of a detailed knowledge of LISP, akthough occasional parenthetical comments will be directed to the more knowledgeable.

The top level function, SOLVE, is a function of three arguments. One, labeled EQT in the definition of SOLVE, is the set of equations to be solved. The argument labeled WANTED in the definition is a list of variables whose values are wanted. The third argument, labeled TERMS, is another list of variables which is disjoint from WANTED. SOLVE will find the value of any variable which is wanted in terms of any or all of the variables on the list TERMS. In use, the list TERMS is a list of units, such as pounds, or feet, which may appear in the answer.

The output of SOLVE is dependent on whether the set of equations given can be solved for the variables wanted. If no solution can be found because the solution involves nonlinear processes, SOLVE returns with the value UNSOLVABLE. If no solution is found because not enough equations are given, SOLVE returns with the value INSUFFICIENT. If however, a solution is found, SOLVE returns with a list of pairs. The first element of each pair is a variable, either on the wanted list, or a variable whose value was found while solving for the desired unknowns. The second element of each pair is an arithmetic expression (in the prefix notation shown in Figure 2), which contains only numbers and variables on the list TERMS. Thus, the answer found

by SOLVE is an "association list" of variables, and their values To the way of the is , 思格蒙 test of the said of in the proper terms.

For example, let us consider the set of seven simultaneous equations shown below, and suppose SOLVE were asked to solve this set of equations for x and z. These are given in infix notation The goal acception costate mentioners on the Addition for ease of reading. o ama primosiony i sidi kilib off i molifeticky

(2)
$$\mathbf{x}^2 - \mathbf{c} = \mathbf{D}$$
 . Let \mathbf{x} the \mathbf{x} to \mathbf{x} \mathbf{y} \mathbf{z} \mathbf{z} \mathbf{z} \mathbf{z} \mathbf{z}

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(3)
$$^{\circ}$$
 C $^{\circ}$ 3D = 6 for the second order of (7) $^{\circ}$ 4x $^{\circ}$ $^{\circ}$

(4)
$$2C - D = 5$$

The list TERMS is empty, and thus the values must all be numbers. In this case SOLVE would return with the fist of pairs "((y, 1)(x, 2)(z, 0))," which indicates that the values x = 2 and z = 0 satisfy this set of equations (or those members of this set which were used to determine the values). The value you live was found during the solving process. the prepare to section of a section of a section

Most of the work of SOLVE is done by the function SOLVER. SOLVE transmits to Solver the list of WANTED variables, the list of TERMS, and a null association list (called ALIS) which is recursively built up to give the answer. The value of SOLVER is this association list of pairs, with the first element of each pair being a variable whose value has been found. The second element of each is an arithmetic expression which may contain any variable 8913.123 on the list TERMS (as was the case for the ALIS of SOLVE) However, it may also contain variables which are first elements of pairs 137.108 later on the association list. If values for variables given by GIGNET A later pairs are substituted into this arithmetic expression, one

yariables on the list TREMS. In the example, SOLVER would return with the association list ((y, (4x-7)) (x,2) (z,0)) which gives y in terms of x. SOLVE makes the substitutions and simplification on the association list returned by SOLVER.

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variables. It does this by choosing one of these variables, adding the others to the list of terms and calling SOLVEL to solve for this one variable in terms of the other wanted variables and the original TERMS. If SOLVEL succeeds in solving for this variable, SOLVER pairs this one variable with the expression found, puts this pair on the end of the ALIS, and using this substitution in every equation it tries to solve, attempts to solve for the remaining wanted variables. If there are no more, SOLVER is finished and returns the association list built up.

equation containing this variable, after all substitutions of values for variables listed on the ALIS have been made. It then makes a list of all the other variables in the equation, and checks to see if there are any not on the list TERMS. If so it calls SOLVER to solve for these new variables in terms of the wanted variable and the variables in TERMS. If SOLVER is unsuccessful, SOLVEI tries to find another equation containing the wanted variable, and repeats the process. If there is none, SOLVEI has the value INSUFFICIENT. If SOLVER is successful, and values for these new variables are found, or if there were no new variables, SOLVEI finally calls SOLVEQ which attempts to solve this equation for the wanted variable. If the equation is linear in this variable, SOLVEQ will be successful and give a solution. SOLVEI will add a pair consisting of the wanted variable and this value to the end

of ALIS, and return with this sugmented ALISOSSELTS value FIRE (0.0000) SOLVEQ is unsuccessfully SOLVEL tries and this Requisition, but then if soldw no solution sean befound SOLVEL returns the by side (MISCLVARIE) - x45 (0.00)

This descriptions has been a srather laugewinded attempt to a notice of explain the cone spage of LISP programmet this and so foth to be chapter. How to work to make it more specific filetous adonated what shappens when SOLVER ideas tries to solve the set of equations (below it the same (one shown all galls) and earlier); and all ((3,0),(2,0),(10,0)) ((3,0),(2),0).

o gaise d'AVA de dimention SHONE (CACOLE de la gaise d'AVA). Corres **(1) l'x.+}w,=.9** idigment bon dotse**-(5).** ce**t-02y = 4**de de do d'alèq

of g. Haveny found g in terms of a. \$25,758 will now tell theory

(2) $x^2 - C = D$

(6) (**(\$²; s-) (3y ×\$• (2 ; ₹) à** 2007 (4d °

(3) C + 3D = 5

(7) 4x - y = 7

a. ... **(4)**... **2C.→ D.⊕**:5.: Model 1-33 kodás medá pymáz michakk sidő kide a ... Makkak ek yak a közöt a Mak**to jes to jes z nyi**en, ad ako togid∃mæð

solve for x in terms of z and Olive for x and z althouse solve for was and a new variable, when appeared and asks SCLARN to solve for was and a new variable, when appeared and asks SCLARN to solve for was and a new variable, when appeared and asks SCLARN to solve for was and a new variable, and z as Since there is no other occurrence of w in a large of this set, SOLVER is unsuccessful and SOLVED absolute equation (1), and and goes to equation (2). Here it calls solve to solve for the action two new variables C and D in terms of x and z. In this case

SOLVER is successful, using equations (3) and (4) point when these values are substituted an equation (2), SOLVED cannot solve for x and z are substituted an equation (2), SOLVED cannot solve for x and z are substituted an equation (2), SOLVED cannot solve for x and z are substituted an equation (2), SOLVED cannot solve for x and z are substituted an equation (2), SOLVED cannot solve for x are a substituted an equation (2), SOLVED cannot solve for x are a substituted an equation (2), SOLVED cannot solve for x are a solve for x ar

SOLVEL now abandons equation (2) and the results it obtained of the as subgoals for solving (2) on It finds an occurrence of x lagsing abandons in (3). Again it calls on SOLVER, to solve for the new variable (2000) y in terms of x and x 901VER tries to use (6) by but SOLVEQ cannot with solve this equation for y 1 Using (7) SOLVER fetures with an ALIS of ((y, (4x - 7))). Using this ALIS, substituting this value for y 1.

which it does, and finally SQLVEL returns to SOLVER the ALIS

((y, (4x - 71), (x,2)) which does give the value of x in terms
of z. Having found x in terms of z, SOLVER will now call SOLVEl

to find the value of z. SOLVEl finds an occurrence of z in

equation (6), and after substitution of terms on the ALIS, SOLVEQ

is able to colve this equation for x, because it is linear in z.

Adding the pair (z,0) to the ALIS, SOLVEL returns it to SOLVER,

which passes on this ALIS ((y, (4x - 7)), (x,2), (z,0)) to SOLVE.

SOLVE, using the function SUBORD, which substitutes in order

pairs on an ALIS into an expression and simplifies, finally returns

the ALIS ((y,1)(x,2)(z,0)).

This example shows the rather tortuous recursions that these functions use to solve a set of equations. Why should we use this type of solving program instead of a more straightforward matrix method? The principal reason is that, as shown nonkinear equations may appear in the set. In this case, if appropriate values can be found from other equations which when substituted into this nonlinear equation make it linear in the variable for which we want to solve, then SOLVE will find the value of this variable.

The method of operation of SOLVER requires that if n variables appear in any equation, and that equation is used, then at least n-1 other independent equations containing these variables must be in the set of equations, or the actual mechanics of solving will not be started. This eliminates much work if there are extraneous equations in the set which contain one or two of the wanted variables. However, it precludes solving a set of equations which is homogeneous in one unwanted variable, and would therefore cancel out in the solution process. This is the principal reason why problems such as:

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"Spigot A fills a tub in 1 hour, and spigot B in 2 hours. How long do they take together?"

cannot be solved by STUDENT.

This solving subroutine set is an independent package in the STUDENT program. Therefore, improvements can be made to it without disturbing the rest of the processing. The routine described here was designed to handle most of the problems that can be found in first year algebra texts.

```
(SOLYE
Figure
           (LAMBDA (WANTED EQT TERMS ALIS) (PROG (A B)
                    (SETQ A (SOLVER WANTED TERMS ALIS))
              START (COND
                       ((NULL A) (RETURN B))
                       ((MULL (CDR A)) (RETURN (CONS (CAR A) B)))
                       ((ATOM A) (RETURN A)))
5
                    (SETQ B (CONS (CONS (CAAR A) (SUBGRD (CDAR A) (
        CDR A))) B))
                    (SETQ A (CDR A))
                    (60 START))))
        (SOLVER
           (LAMBDA (WANTED TERMS ALIS) (PROG (A B C D E G H J)
                    (SETQ A WANTED)
                    (SETQ J (QUOTE INSUFFICIENT))
              START (COND
Progr
                       ((NULL A) (RETURN J)))
                    (SETQ B (CAR A))
                    (SETQ C (CDR A))
                    (SETQ E (SOLVE) B (APPEND C (APPEND D TERMS)) ALIS
        "
                    ( COND
                       ((ATOM E) (GO ON)))
5
                    (SETQ H (NCONC D C))
                    (COND
STUDENT
                       ((NULL H) (RETURN E)))
                    (SETQ E (SOLVER H TERMS E))
                    ( COND
                       ((NOT (ATOM E)) (RETURN E)))
                       ((EQ E (QUOTE UNSOLVABLE)) (SETQ J E)))
                    (SETQ D (COMS B D))
                    (SETQ A C)
                    (90 START))))
```

```
(SOLVE1
   (LAMBDA (X TERMS ALTS) (PROG (A B C D E G H J)
                (SETQ A EQI)
                (SETQ J (QUOTE INSUFFICIENT))
        START (COND
                   ((MULL X) CRETURN 33))
               (SETQ B (GAR A)) (SETQ C (SETQ D (WATERS C))
                (COMD
                   ((MEMBER X D) (SO OM)))
               (SETO E (ONS & E))
(SETO A (COR AY)
                (GO START)
               (SETQ G (CHAS X TERMS X)
(SETQ H (EGGHTEUS D G))
(SETQ EQT (EFFACE D EQT))
                                                                  1.1
                ( COND
                ((MULL H) (SO SOLVER)))
(SETO G (SOLVER HE ALIS))
                (CONO
                   ((ATOM ) (@O D))) :
       (SETQ ALIS 6)-0
(SETQ C (SUBORD 8 ALIS))
SOLVEQ (SETQ G (SOLVEQ ) C)
               (APPEND ACIS (LIST
                                      D, ⊗
                                                                  T.
                (COND
                ((ED G (QUOTE UNSOLVABLE)) (SETQ J G));
(SETQ EQT (APPEND E A))
               ें (देश के)
```

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specifing regions of single-ordered analysis impact sentence in the form of the ordered and the meaning of the life and meaning of the ordered and the sentence of the ordered and the ordered

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A. Results. Beile for a province of production smorth beauty of rose

The purpose of the research reported here was to develop about 1979 techniques which facilitate natural language communication with a computer of Alsemantic theory of seehesent diageuree was proposed as a basis for the design and understanding of such managed in a systems. This theory was only outlined, and much additional work substituted remains to be done. However, in its present remains to be done. However, in its present remains to be done. However, in its present remains to be done as a guide for construction of the STUDENT system.

analytic portion of this theory. The STUDENT aystem has a very narrow semantic base. From the theory it is clear that by utilizing this knowledge of the limited range of meaning of the input discourse, the parsing problem becomes greatly simplified since the number of linguistic forms that must be recognized is very small. It is parsing system were based on any small semantic base of this same simplification would occur. This suggests that impagement language processor, some time might be spent autiting the input into a semantic context before going shead with the syntactic analysis or a

by the characteristics of the problem solving system embedded in it.

STUDENT is a question-answering system which answers questions posed in the context of "algebra story problem." In the introduction, we used four criteria for evaluating several question-answering systems. Let us compare the STEDENT system to these others in the light of these criteria.

1) Extent of Understanding. All the other question-answering systems discussed analyze input sentence by sentence.

Although a representation of the meaning of all input sentences may be placed in some common store, no syntactic connection is always ever made between sentences.

In the STUDENT system, an acceptable input is a sequence of sentences, such that these sentences cannot be understood by just finding the meanings of the individual sentences, signoring their local context. Inter-sentence dependencies must be determined, and inter-sentence syntactic relationships must be used in this case for solution of the problem given. This extension of the syntactic dimension of understanding is important because such inter-sentence dependencies (e.g., the use of pronouns) are very commonly used in natural language commendation.

normal security base. From the theory is as cally that by sailing

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The semantic model in the STUDENT system is based on one relationship (equality) and five basic aftermette functions. Composition of these functions yield other functions which are also expressed as individual linguistic forms in the imput language. The input language is richer in expressing functions than Lindsay's or Raphael's system. The logical systems discussed may have more relationships (predicates) allowable in the input, but do not allow any composition of these predicates. The logical combinations of predicates used are only those expressed in the input as logical combinations (using and, or, etc.).

The deductive system in STOPENT, as in Lindsey's and Raphael's programs, is designed for the type of questions to be asked. It can only deduce answers of a certain type from the input information, that is, arithmetic values satisfying a set of equations. In performing its deductions it is reasonably sophisticated in avoiding

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the general power of a logical system, but is much more efficient in obtaining its particular class of deductions them would be a general deductive system utilizing the axioms of arithmetic.

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2) Facility for Extending Abilities. Extending the syntactic abilities of any of the other question-answering systems discussed would require reprogramming. In the STUDENT system new definitional transformations can be introduced at run time without any reprogramming. The information concerning these transformations can be input in English, or in a combination of English and METEOR, if that is more appropriate. New syntactic transformations must be added by extending the program.

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wall you to provide the the formation of sampling, and the contrast of the con-

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by adding new program, as is true of the other question answering systems discussed. However STUDENT is organized to facilitate such extensions, by minimizing the interactions of different parts of the program. The necessary information need only be added to the program equivalent of the table of operators in Figure 4, in Chapter IV.

Similarly, the deductive portion of STUDENT, which solves the derived set of equations, is an independent package. Therefore, available new extended solver can be added to the system by just replacing the package, and maintaining the input-output characteristics of this subroutine.

3) Knowledge of Internal Structure Needed by User. Very little if any internal knowledge of the workings of the STUDENT system need be known by the user. He must have a firm grasp of the

grammar. For example, he must be aware that the same phrase must be always be used to represent the same variable in a problem, within the limits of similarity defined earlier. He must realize that even within these limits STUDENT will not recognize more than one variation on a phrase. But if the user does forget any of these facts, he can still use the system, for the interaction discussed in the next section allows him to make amends for climat any mistake.

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4) Interaction With the User of The STUDENT system is combedded as a stime sharing constituent (the MIT Project MAC time sharing as a second system (13)) and this greatly facilitates interaction with the constituent user. STUDENT differentiates between its failure to solve as a possible problem because of its mathematical limitations and failure from lack of sufficient sinformations of investigation for the constituent information possible suggests the mature of the needed beautiful information (relationships smoog wariables) of the problem as all the problem pronquintil of the problem in till it has seen as a consideration but it is a

an input sentence. Using this information as a guide, the user is in a teaching-machine type attention, and can quickly learn to speak STUDENT's brand of input English and young the sesumptions that STUDENT makes about the input and the global information it is an unwanted ambiguity, or add new general information to the second and global information store.

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The crucial point in this user interaction is that STADENT is embedded in an on-line time sharing system; and can thus provide more interaction than any of the other systems mentioned.

B. Extensions.

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The present STUDENT system has reached the maximum size allowable in the LISP system on a thirty-two thousand word IBM 7094. Therefore, very little can be added directly to the present system. All the programming extensions mentioned here are predicated on the existence of a much larger memory machine.

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Without inventing any new techniques, I think that the STUDENT system could be made to understand most of the algebra story problems that appear in first year high school text books. If new operators, new combinations of arithmetic operations occur, they can easily be added to OPEORM, the subroutine which maps the kernel English sentences into equations. The number of formats recognizable in the system can be increased without reprogramming through the machinery available for storing global information (this was discussed in more detail in Chapter V). The problems it would not handle are those having excessive verbiage or implied information about the world not expressible in a single sentence.

As mentioned earlier, the system can now make use of any given schema only once in solving a problem. This is because the schema equation is added to the set of equations to be solved, and the variables in the schema only identified with one other set of variables appearing in the problem. For example, if "distance equals speed times time" were the schema, then "distance", as a variable in the schema might be set equal to "distance traveled by train" or "distance traveled by plane", but not both in the same problem. This problem could be resolved by not adding the schema equation directly to the set of equations to be solved, but by looking for consistent sets of variables to identify with the schema variables. Then STUDENT could add an instance of the schema equations, with the appropriate substitutions, for each consistent set of variables

found which are "similar" to the schema variables.

At the moment the solving subroutine of STUDENT can only perform linear operations on literal equations, and substitutions of numbers in polynomials and exponentials. It would be relatively easy to add the facility for solving quadratic or even higher order solvable equations. One could even add, quite easily, sufficient mechanisms to allow the solver to perform the differentiation needed to do related rate problems in the differential calculus.

The semantic base of the STUDENT system could be expanded. order to add the relations recognized by the STR system of Raphael, for example, one would have to add on the lowest level of the STUDENT program the set of kernel sentences understood in SIR, their mapping to the SIR model, and the question-answering routine to retrieve facts. Then the apparatus of the STUDENT system would process much more complicated input statements for the SIR model. One serious problem which arises when the semantic base is extended is based on the fact that one kernel may have an interpretation in terms of two different semantic bases. For example, "Tom has 3 fish." can be interpreted in both SIR and the present STEDENT system. To resolve this semantic ambiguity, the program can check the context of the ambiguous statement to see if there has been one consistent model into which all the other statements have been processed. If the latter condition does not determine a single preferred interpretation for the statement, then both interpretations can be stored.

In addition to these immediate extensions of the STUDENT system, our semantic theory of discourse can be used as a basis for a much more general language processing system. As a start, one could implement the generative grammar described in Appendix E to produce coherent discourse—problems solvable by the STUDENT system.

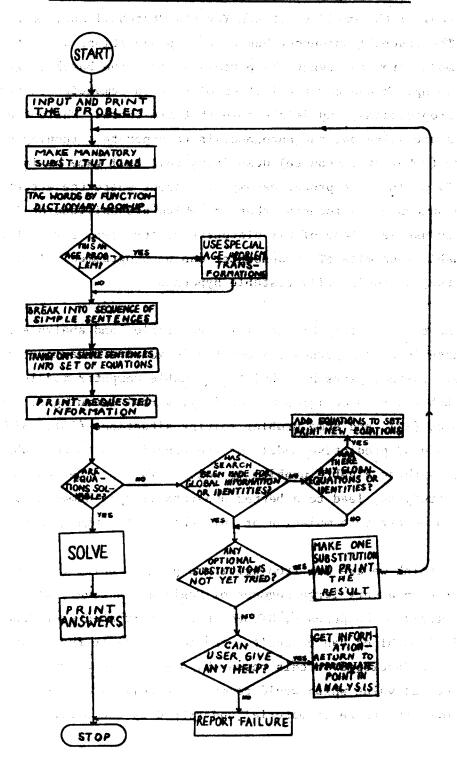
Another more exciting possibility is to utilize this type of speaker's model of the world to attack Yngve's "baseball announcer" problem. The baseball announcer has certain propositions added to his world model from the events he perceives, i.e. the baseball game he is watching. Mandatory application of certain semantic rules add other propositions, and delete some that are there. While these changes are going on, the announcer is to generate a running commentary (coherent discourse) describing this balk there the it watching. By making the proper assumptions about where the attention of the announcer is focused, that is, which propositions he is going to use as a base of his discourse at any time. I feel that a reasonable facsimile of an announcer can be programmed. This is, of course, an empirically testable hypothesis.

Another use for this model for generation and analysis of discourse is as a hypothesis about the linguistic behaviour of people. Psychologists have built reasonable computer models for human behaviour in decision making (17), verbal learning of nonsense syllables (15), and some problem solving situations (34). STUDENT may be a good predictive model for the behaviour of people when confronted with an algebra problem to solve. This can be tested, and such a study may lead to a better understanding of human behaviour, and/or a better reformulation of this theory of language processing.

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I think we are far from writing a program which can understand all, or even a very large segment of English. However, within its narrow field of competence, STUDENT has demonstrated that "understanding" machines can be built. Indeed, I believe that using the techniques developed in this research, one could construct a system of practical value which would communicate well with people in English over the range of material understood by the program.

APPENDIX A: PLOWCHART OF THE STUDENT PROGRAM



APPENDIX B: LISTING OF THE STUDENT PROGRAM

1) Definition of STUDENT

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APPENDIX C: GLOBAL INFORMATION IN STUDENT

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REMEMBER((
 (PEOPLE IS THE PLURAL OF PERSON)
 (FEET IS THE PLURAL OF FOOT)
(YARDS IS THE PLURAL OF YARD)
 (FATHOMS IS THE PLURAL OF FATHOM)
 (INCHES IS THE PLURAL OF INCH)
(SPANS IS THE PLUMAL OF SPAN)
(ONE HALF ALWAYS MEANS 0.5 )
(THREE NUMBERS ALWAYS MEANS THE FIRST NUMBER AND THE SECOND NUMBER AND THE THIRD NUMBER)
(FIRST TWO NUMBERS ALWAYS MEANS
THE FIRST NUMBER AND THE SECOND NUMBER)
 (MORE THAN ALWAYS MEANS PLUS)
 (THESE ALWAYS MEANS THE)
(TWO MIMBERS SOMETIMES MEANS ONE HUMBER AND THE
 (TWO NUMBERS SOMETIMES MEANS ONE OF THE NUMBERS AND THE OTHER NUMBERS
 (HAS IS A VERE)
(GETS IS A VERB)
(HAVE IS A VERB)
(LESS THAN ALWAYS MEANS LESSTHAN)
(LESSTHAN IS AN OPERATOR OF LEVEL 2)
(PERCENT LESS STHAN ALWAYS MEANS FERWESS)
(PERCENT LESS STHAN ALWAYS MEANS FERWESS)
(PERCENT LESS STHAN ALWAYS MEANS FERWESS)
(PEUS IS AN OPERATOR OF LEVEL 2)
(SUM IS AN OPERATOR OF LEVEL 1)
(SUM IS AN OPERATOR OF LEVEL 1)
 (SQUARE IS AN OPERATOR OF LEVEL 1)
(DIVBY IS AN OPERATOR OF LEVEL 1)
(DIFFERENCE IS AN OPERATOR)
(SQUARED IS AN OPERATOR)
(MINUS IS AN OPERATOR OF LEVEL 2)
(PER IS AN OPERATOR)
(SQUARED IS AN OPERATOR)
(YEARS OLDER THÂN ALWAYS MEANS
 (YEARS OLDER THAN ALWAYS MEANS PEUS)
(YEARS YOUNGER THAN ALWAYS MEANS LESS THAN)
(IS EQUAL TO ALWAYS MEANS IS)
(PLUSS IS AN OPERATOR)
 (MINUSS IS AN OPERATOR)
(HOW OLD ALWAYS MEANS WHAT)
(THE PERIMETER OF $1 RECTANGLE SOMETIMES MEANS
TWICE THE SUM OF THE LEMBTH AND WIDTH OF THE RECTANGLE)
(GALLONS IS THE PEURAL OF GALLONS
 (HOURS IS THE PEURAL OF HOUR)
(MARY IS A PERSON)
(ANN IS A PERSON)
(A FATHERE IS A PERSON)
(AN UNCLE IS A PERSON)
(POUNDS IS THE PLURAL OF POUND)
(WEIGHS IS A VERB)
))
REMEMBER ((
(DISTANCE FORCE)
 (DISTANCE EQUALS SPEED TIMES TIME)
(DISTANCE EQUALS GAS CONSUMPTION TIMES NUMBER OF GALLONS OF GAS USED)
 (1 FOOT EQUALS 12 INCHES)
(1 YARD EQUALS 3 FEET)
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(THE PROBLEM TO BE SOLVED IS)
(IF THE NUMBER OF CUSTOMERS TOM GETS IS TWICE THE SQUARE OF 20 PER CENT OF THE NUMBER OF ADVERTISEMENTS HE RUNS, AND THE NUMBER OF ADVERTISEMENTS HE RUNS IS 45, WHAT IS THE NUMBER OF CUSTOMERS TOM GETS Q.)
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(WITH MANDATORY SUBSTITUTIONS THE PROBLEM IS)
(IF THE NUMBER OF CUSTOMERS TOW GETS IS 2 TIMES THE SQUARE
20 PERCENT OF THE NUMBER OF ADVIATISEMENTS HE RUNS, AND THE
NUMBER OF ADVERTISEMENTS HE RUNS IS \$5, WHAT IS THE NUMBER
OF CUSTOMERS TOM GETS Q.)

(WITH WORDS TAGGED BY FUNCTION THE PROBLEM IS)
(IF THE NUMBER (OF / OP) CUSTOMER® TOM (GETS / VERB) IS 2 (
TIMES / OP 1) THE (SQUARE / OP 1) 20 (PERCENT / OP 2) (OF /
OP) THE NUMBER (OF / OP) ADVERTISEMENTS (HE / PRO) RUNS , AND
THE NUMBER (OF / OP) ADVERTISEMENTS (HE / PRO) RUNS IS &5 ,
(WHAT / QWORD) IS THE NUMBER (OF / OP) CUSTOMERS TOM (GETS / VERB) (QMARK / DLM))

(THE SIMPLE SENTENCES ARE)

(THE NUMBER (OF / OP) CUSTOMERS TOM (GETS / VERB) IS 2 (TIMES / OF 1) THE (SQUARE / OP 1) THE PERCENT / OP 2) (OF / OP) THE NUMBER (OF / OP) ADVERTISEMENTS (HE / PRO) RUNS (PERIOD / DLM))

(THE NUMBER (OF / OP) ADVERTISEMENTS (HE / PRO) RUNS IS 45

(SMAT / QHORD) IS THE NUMBER (OF / OP) CUSTOMERS TOM (GETS VERB) (QMARK / DLM))

(THE EQUATIONS TO BE SOLVED ARE)

(TOPAL GOZELE (HUMBER OF GUSTOMERS TOM (GETS / VERB)))

GODAL (NUMBER OF ASVERTISEMENTS (HE / PRO) SURS) 49)

(FONAL (NUMBER OF CUSTOMERS TOM CORTS / TVERDE) LTIMES 2 (EXPT. (TIMES . 2000 (NUMBER OF ADVERTISEMENTS (HE ? PRO) RUNS)) 2)))

(THE NUMBER OF CUSTOMERS TOM GETS IS 182)

(THE PROBLEM TO BE SOLVED IS)
(THE SUM OF LOIS SHARE OF SOME MONEY AND BOB \$ SHARE IS \$ 4.500
. LOIS SHARE IS TWICE BOB S . FIND BOB S AND LOIS SHARE .)

(WITH MANDATORY SUBSTITUTIONS THE PROBLEM IS)
(SUM LOIS SHARE OF SOME MONEY AND BOB S SHARE &S 4.500 DOLLARS
LOIS SHARE IS 2 TIMES BOB S . FIND BOB S AND LOIS SHARE .)

(WITH WORDS TAGGED BY FUNCTION THE PROBLEM IS)
((SUM / OP) LOIS SHARE (OF / OP) SOME MONEY AND BOB S SHARE
IS 4.500 DOLLARS (PERIOD / DLM) LOIS SHARE IS 2 (TIMES / OP
1) BOB S (PERIOD / DLM) (FIND / QWORD) BOB S AND LOIS SHARE
(PERIOD / DLM))

(THE SIMPLE SENTENCES ARE)

((SUM / OP) LOIS SHARE (OF / OP) SOME MONEY AND BOB S SHARE IS 4.500 DOLLARS (PERIOD / DIM);

(LOIS SHARE IS & (TIMES / OP 1) BOB S (PERIOD / DLM))

((FIND / CHORD) BOB S AND LDIS SHARE (PERIOD / DLM))

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL GO2518 (LOTS SHARE))

CLEQUAL GO2518 (BOS S))

CEQUAL (LOS SHARE) (TIMES & (BOE ST))

SQUAL (PLUS 48018 SHARE OF SOME MOREYS (SOR B SHARE)) (TIMES

THE MENT ON HERE MENT IS FINE & SOLUTION

((BOR \$)) E EQUAL TO (BOR & SHARE!)

(ASSUMING THAT)

((LOTS SMARE) IS EQUAL TO (LOTS SHARE OF SOME MONEY))

(BOE S IS 1.500 DOLLARS)

(LOTS SHARE IS 3 DOLLARS)

(THE PROBLEM TO BE SOLVED IS)
(MARY IS TWICE AS OLD AS ANN WAS WHEN MARY WAS AS OLD AS ANN
IS, NOW. . IF MARY IS 24. YEARS, OLD , HOW OLD IS ANN Q.)

(WITH MANDATORY SUBSTITUTIONS THE PROBLEM IS)
(MARY IS 2 TIMES AS OLD AS ANN WAS WHEN MARY WAS AS OLD AS ANN IS NOW . IF MARY IS 26 YEARS OLD , WHAT IS ANN Q.)

(MAIXH HORDS TARGED BY FUNDTION THE PROBLEM IS)
((MARY / MEMEON) 18 % (TIMES / OP 1) AS OLD AS (ANN / PERSON)
(AA) WESM (MARY / PERSON) WAS AS OLD AS (ANN / PERSON) IS NOW
(PERIOD / DUN) IF (MARY / PERSON) IS 2% YEARS OLD , (WHAT /
QMORD) 16 (ANN / PERSON) (QMARK / DLM))

THE SIMPLE SENTENCES ARE)

((MARY / PERSON) & AGE IS 2 (TIMES / OP 1) (ANN / PERSON) S AGE GDZBZ1 YEARS AGD (PERIOD / DIM))

COURSEL LEARS AGO CHARY / PERSON) S AGE IS (ANN / PERSON) S AGE NOW (PERIOD / DLN))

(MARY / PERSON) S AGE TS 2% (PERIOD / DLM))

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38101 2 MBS 12 193

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL GASS 22 LIANN / PERSON) & AGEN)

(EQUAL ((MARY / PERSON) S AGE) 24)

নি । কি এই ও কৈ মাজৰী হৈছিছে। তিনাৰ ৰাম্যা চন্দ্ৰৰ চাত্ৰিক কৰে। তাৰ কাৰ্য কৰি কৰি নক্ষান্ত্ৰিক চন্দ্ৰ চাত্ৰিক কৰে।

FERRORY S AGE)

CERT CONSTRUCTION DESCRIPTION S AGE) (TIMES 2 (PLUS ((ANN / PERSON)) S AGE) (TIMES 2 (PLUS ((ANN / PERSON)) S AGE) (TIMES 2 (PLUS ((ANN / PERSON)) X) TERMS OF AGENCIES TO BE AGENCIES TO

. 14 CONTROL 15 AR 2014 ACT | 14 AR 2014 ACT | 14 AR | 15 AR | 16 AR |

The section of the Bullion of

(THE PROBLEM TO BE SOLVED IS)
(THE SUM OF THE PERIMETER OF A RECTANGLE AND THE PERIMETER
OF A TOTAL THE PERIMETER OF THE TRIANGLE OF THE RECTANGLE
18 THIRD PERIMETER OF THE TRIANGLE, WHAT IS THE PERIMETER
OF THE TRIANGLE Q.)

(WITH MANDATORY SUBSTITUTIONS THE PROBLEM (S)
(STUM THE THREET OF A REGTANGLE AND THE PERIMETER OF A TRIANGLE
IS 24 INCHES . IF THE PERIMETER OF THE RECTANGLE IS 2 TIMES
THE PERIMETER OF THE THIANGLE , WHAT IS THE PERIMETER OF THE
TRIANGLE Q.)

THINTH WORDS TARGES BY FUNCTION THE PROBLEM IS)

((BUN) PIGF) THE PERIMETER (OF / OP) A RECTANGLE AND THE PERIMETER

(OF / OF) THE RECTANGLE IS BY INCHES (PERIOD / DLM) IF THE PERIMETER

(OF / OF) THE TREAMQLE IS 12 (THES / OP 1) THE PERIMETER (
OF (OF) THE TREAMQLE (WHAT / QWORD) IS THE PERIMETER (OF

/ OP) THE TRIANGLE (WARK / DLM)

CTHE SIMPLE SENTENCES ARE)

-(4SUM 1.9P) THE PERIMETER (OF / 9P) A RECTANGLE AND THE PERIMETER (OF / 0P) A TRIANGLE IS 24 INCHES (PERIOD / DLR))

THE PERIMETER (OF / OF) THE RECTANGLE IS 2 (TIMES / OP 1)

((WMAT / QWORD) IS THE PERIMETER (OF / OP) THE TRIANGLE (QMARK / DLM))

5880842 CERT SHROWS PERIMETER (OF / OP) THE TRIANGLE (QMARK / DLM))

5880842 CERT SHROWS PERIMETER (OF / OP) THE TRIANGLE (QMARK / DLM))

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL GOZSIT (PERIMETER OF TRIANGLE))

(EQUAL (PERIMETER OF RECTANGLE) (TIMES 2 (PERIMETER OF TRIANGLE)))

(EQUAL (PLUS (PERIMETER OF RECTANGLE) (PERIMETER OF TRIANGLE))

(EQUAL (PLUS (PERIMETER))

HE ROOVINGHE IN 25 REPLIES THE

(THE PERIMETER OF THE TRIANGLE IS & INCHES)

TO BEET MESSAGE TO SEE AND SEE AND THE SECOND TO SEE AND THE SECOND TO SEE AND THE SECOND TO SEC

(BILL S AGE IS 8)

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(THE PROBLEM TO BE SOLVED IS)
 (BILL IS ONE HALF OF HIS FATHER S AGE & YEARS AGO . IN 20 YEARS
HE WILL BE 2 YEARS OLDER THAN HIS FATHER IS NOW . HOW OLD ARE
BILL AND HIS FATHER Q.)
(THE EQUATIONS TO BE SOLVED ARE)
 (EQUAL 602556 ((SILL / PERSON) & (FATHER / PERSON) & AGE))
(EQUAL GOZSAS ((BILL / PERSON) S AGE))
(EQUAL (PLUS (CALL / MERSON) S AGE) 20) (PLUS 2 (CALL / PERSON) S (FATHER / PERSON) S AGE)))
 (EQUAL ((BILL / PERSON) & AGE) (TIMES . SOOO (PLUS ((BILL /
 PERSON) & (FATHER & PERSON) S. AGE) (MINUS. 4)3))
                                          COMMUNICATION OF THE PROPERTY OF A
(BILL S AGE IS 14)
(BILL S FATHER 8 AGENES 32) and to present the second of the second A
(THE PROBLEM TO BE EDITED IS)
(BILL S FATHER'S UNCLE IS THICE AS OLD AS BILL S FATHER . 2
YEARS FROM HOM BILL & FATHER MILL BE 3 TIMES AS OLD AS BILL
. THE SUM OF THETH ABEE IS $2. FIND BILL AGE .)
 (THE EQUATIONS TO SE SOLVED ARE)
 (EQUAL GORSES (COLLLING PERSON) & AGENT
(EQUAL (BUIL (ELL), PERSON) & (FATHER / PERSON) & (MOLE / PERSON) & AREX CHAIR ACTION PERSON) & (FATHER / PERSON) & PERSON) S AGE) (CALLA / BEREON) & (FATHER / PERSON)
 (EQUAL (PLUS (CALL / PERSON) & (FATHER / PERSON) & AGE) 2) (TIMES 5 (PLUS (CALL / PERSON) & AGE) 2))) (FATHER / PERSON) & AGE) (TIMES 5 (PLUS (CALL / PERSON) & AGE) (TIMES 5 (PLUS (CALL / PERSON) & AGE) (TIMES 5 (PLUS (CALL / PERSON) & AGE) (TIMES 5 (PATHER / PERSON) & AGE) (TIMES 6 (PATHER / PATHER /
 (EQUAL ((B)(L) PERSON) S (FAYNER / PERSON) S (UNCLE / PERSON) S AGE) (TIMES 2 (GRILL / PERSON) S (FAYNER / PERSON) S AGE)))
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परिष्ण है है । परिष्ठ एक स्टूरिय पता स्टूरिय अधिक अधिक अधिक प्राप्ति ।

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(THE PROBLEM TO BE SOLVED IS) CA NUMBER IS MULTIPLIED BY 6 . THIS PRODUCT IS INCREASED BY
 44 . THIS RESULT IS 68 . FIND THE MUMBER .)
          TANK NEWSTRANSEN STATES TO SELVE A TOTAL RESIDENCE
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL GRESSE (NUMBER))
(EQUAL (PLUS (TIMES (MUMBER) 6) 44) 68)
         CETTAIN TELE MEDIUM NE CONTROL CONTROL
CTHE MINDER IS 4)
(THE PROBLEM TO BE SOLVED 15)
(THE PRICE OF A RADIO IS 69.70 DOLLARS . IF THIS PRICE IS 15 PERCENT LESS THAN THE MARKED PRICE , FIND THE MARKED PRICE
         is pile.
                                     i dentro karajeko pi den izako bareko barekili eniko idako bilikoare
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL GO2515 (MARKED PRICE))
(EQUAL LPRICE OF BADIO) (TIMES . 1698 (MARKED PRICE)))
(EQUAL (PRICE OF RADIO) (TIMES 69.70 (DOLLARS)))
 (THE MARKED PRICE Jacobs DOLLARS)
 CTHE INCOME TO SE WELVER 3 S)
CTOM MEET TOTAL AS SAME MINE AS MARY HAS CUPPLED, IF MARY HAS SAME HARY HAS CUPPLED.
 CTHEST SQUARE TO THE THE CONTROL OF THE STATE OF THE STAT
  (EQUAL GOVERS THURSEN OF FISH TON (HAS / VEND))
 (EQUAL (NUMBER OF GUPPIES (MARY / PERSON) (MAS / VERB)) 3)
 CECURE CHARGE OF THE TON THAN THERE STIMES & CHARGE OF CHARGE PERSONS THAN THERE TO THE STIMES OF
                ටුය සුදුලෙසයාව යුතු එසු එසුවිද්ධය වෙමුව
 (THE NUMBER OF FISH TON HAS IS 6)
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(THE PROBLEM TO BE SOLVED IS)
(IF 1 SPAN EQUALS 9 INCHES , AND 1 FATHOM EQUALS 6 FEET , HOW
MANY SPANS EQUALS 1 FATHOM Q.)
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL 002529 (TIMES 1 (FATHOMS)))
(EQUAL (TIMES & CFATHOMS) FOT MES 6 (FEET)))
(EQUAL TYTHES 1 (SPANSE) (TIMES 9 (INCHES)))
        STOREST STORES OF STREET STORES
THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION
(USING THE FOLLOWING KNOWN RELATIONSHIPS)
((EQUAL (TIMES 1 (YARDS)) (TIMES 3 (FEET))) (EQUAL (TIMES 1)
(FEET)) (TIMES 2 (FUCHES)))))
                                                                                               1047.00
            KUTEAN OF SET OBJECT WASHER
See Sementa of Digoral of the
(1 FATHOR TS & SPARS)
                                                                                           STALL TALLED THE
 (THE PROBLEM TO BE SOLVED IS)
 (THE NUMBER OF SOLDIERS THE RUSSIANS HAVE IS ONE HALF OF THE
 NUMBER OF COMESTHEY WAYER THE NUMBER OF GUIS THEY HAVE IS 7000 . WHAT IS THE NUMBER OF SOLDIERS THEY HAVE Q.)
         CONTRACTOR OF CLOSE - 2
                                                                     <u>al right</u> acteons of the some of the constant a
 (THE EGGATIONSHTO) BE SOLVED ARE)
 (ECHAL GORSISOANUMBER OF SOLDIERS (THEY / POO) ANAVE / YERB)))
 (EQUAL (NUMBER OF GUNS (THEY / PRO) (HAVE / VERB)) 7000)
(EQUAL INUMERS OF SUCCESSIVE CAMBINATES, 12)
 THE COMMITTERS WERE CLASSIFFICIENT TO FIND A SOLATION.
 (ASSUME NEWTONATIME SE SE ZOFACE THEY / PRO) (HAVE / VERB)) IS EQUAL TO
  (NUMBER OF SOLDIERS RUSSIANS (HAVE / VERB)))
        MEMBER OF STREETS OF STREETS OF STREETS OF STREETS
CHARLES OF PROCESSOR COMMINES OF PART OF THE COMMINES OF THE C
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(THE PROBLEM TO BE SOLVED IS)
(THE RUSSIAN ARMY HAS 6 TIMES AS MANY RESERVES IN A UNIT AS
IT HAS UNIFORMED SOLDIERS . THE PAY FOR RESERVES EACH MONTH IS 50 DOCLARS TIMES. THE NUMBER OF RESERVES IN THE UNIT ... AND THE AMOUNT SPENT ON THE REGULAR ARMY EACH MONTH IS 5 150 TIMES
THE NUMBER OF UNIFORMED SOLDIERS . THE SUM OF THIS LATTER AMOUNT AND THE PAY FOR RESERVES EACH MONTH EQUALS $ 55800 . FIND THE NUMBER OF RESERVES IN A UNIT THE RUSSIAN ARMY RAS AND THE NUMBER OF ORIFORMED SOLDIERS IT HAS .)
    大色はど とは 不得力 きは機能さらまっ起去 ウェッキン
                                          THE ALE CONTROL OF SHEET OF
CITHE EQUATIONS TO BE SOLVED ARE)
(EQUAL GO2532 (MUMBER OF WILFORMED SOLDLERS (IT. (.PRO) (HAS
CEQUAL 002531 (NUMBER OF RESERVES IN UNLI RUSSIAN ARMY CHAS
TVERESTE CONTROL OF SHE OF SHEET CONTROL OF CHARLES
GEODAL (PLUS (AMOUNT SPENT ON REGULAR ARMY EACH MONTH) (PAY
FOR RESERVES EACH MONTHED (TIMES 45000 (BOLLARS))
(EQUAL (AMOUNT SPENT ON REGULAR ARMY EACH MONTH) (TIMES (TIMES
150 (DOLLARS)) (NUMBER OF UNIFORMED SOLDIERS)))
(EQUAL (PAT POR RESERVES EACH MONTH) (TIMES (TIMES SO (DOLLARS))
CHUMBER OF RESERVES IN UNITYY)
GROOM! (NUMBER OF RESERVES IN UNIT RUSSIAN AMAY (MAS ) VERS))
(TIMES & (MANGER OF UNIFORMED SOLDIERS (IT / PRO) (HAS / VERS))))
   LEGITAL BRITALS LIGHT CAT A PROT TARES TO TRAVEL PROM NEW YORK
THE FOUNTIONS HERE LINGUEFICLENT TO FIND A SOLUTION
CHANGES OF MILEUMED SOLDIERS) IS EGNY TO CHANGE OF MILEUMED
CARSON IN THE TREET OF A CO. STORE TO CHOMBER OF RESERVES IN UNIT HOSELAN SEE SEED OF A CO. STORE TO CHOMBER OF RESERVES
CTHE HOMBERISER RESERVES HE AFUNKT THE PROSESSA ARMY MAS IS GOOD
CTHE MUMBER OF UNIFORMED SOLDIERS IT HAS IS 100)
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COMPANIES D. COMPANIES OF HICE SUBSTICUTE AN EDITOR OF COURSE POSTS.

迈出 电运动与电池运动 门籍 经产品库 使切坏的有关

THE EQUATIONS TO BE SOLVED ARE)

\$2000/90000 **01 20**00**0**15/30 0000015(2) 6.

OF THEM THE STORY LINES.

ECONAL CO2553 (NUMBER OF STUDENTS IN HIGH SCHOOL))

(EQUAL (NUMBER OF SUCCESSFUL CANDIDATES) 72)

COULD COMMER OF STUDENTS WIND PASSED AGRICULOUS TEST) (TIMES 100 (TOTAL NUMBER OF STUDENTS IN HIGH SCHOOL))

- 1867 - 1988 - 1 84351 - 158855

THE EGUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

(ASSUMING THAT)
((NUMBER OF STUDENTS IN HIGH SCHOOL) IS EQUAL TO (TOTAL NUMBER OF STUDENTS IN HIGH SCHOOL))

THE EQUATIONS WERE VENSUFFICIENT TO FIND A SOLUTION OF A PROPERTY OF THE PROPE

TRYING POSSIBLE IDIOMS

代学的学学内的各LEN (株学学者的 IDIOMATIC SUBSTUTION IS) (THE NUMBER OF STUDENTS WHO PASSED THE ADMISSIONS TEST IS 10 PERCENT OF THE TOTAL NUMBER OF STUDENTS IN THE HIGH SCHOOL 京大学 等地学学的内容 (中ではいるとなっている。 「大学等では、対象など、16年 1985 Number 1985 までは、1985 N. GING HIGH GENOOL Q.) 「対象など、1986 とのでの対象に対象を対象を表しいるとは、2008年1885

WHE ECONOMICATE HERE SINGREGISTENCE TO SERVE A CONTINUE (THE EQUATIONS TO BE SOLVED ARE)

CEQUAL GO2564 THUMBER OF STUDENTS IN MICH SCHOOL))

TEQUAL (HUMBER OF STUDENTS HIND PASSED ADMISSIONS TEST) 72)

CEQUAL CHUMBER OF STUDENTS THE PASSED ADMISSIONS TEST) (TIMES 1900 (TOTAL NUMBER OF STUDENTS IN HIGH SCHOOL)))

THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

(ASSUMING THAT)
((NUMBER OF STUDENTS IN HIGH SCHOOL) IS EQUAL TO (TOTAL NUMBER OF STUDENTS IN HIGH SCHOOL))

CTHE NUMBER OF STUDENTS IN THE HIGH SCHOOL IS 724)

THE PROBLES TO SE SOLMED IS:
THE PISTANCE PROM NEW YORK TO LOS ANGELES IS 3000 ATLES.
IF THE AVERAGE SPEED OF A JET PLANE IS 600 MILES PER HOUR,
FIND THE TIME IT TAKES TO TRAVEL FROM NEW YORK TO LOS ANGELES
BY JET.

(THE EQUATIONS TO BE SOLVED ARE)

(EQUAL G02517 (TIME (IT / PRO) TAKES TO TRAVEL FROM NEW YORK TO LOS ANGELES BY JET))

(EQUAL (AVERAGE SPEED OF JET PLANE) (QUOTIENT (TIMES 500 (MILES))

CECNAL (AMBERT BREAK ON MEMILIAN WORK TO FOR MONTH, CTIMES (TIMES 2000) . (ANTER FOR THE MEMILIAN WERE CONTRACTED TO A MONTH OF THE STATE OF THE MEMILIAN WERE CONTRACTED TO A MONTH OF THE STATE OF THE MEMILIAN WERE CONTRACTED TO A MONTH OF

THE FOUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

TOST HO THE FOLLOWING KNOWN KELATIONSHIPS (MONTH OF THE COLORS OF THE C

(ASSUMING THAT)
TIPPEED OF JET PLANE)

(ASSIMING THAT) "(TIME) 'IS EQUAL TO (TIME (IT / PRO) TAKES TO TRAVEL FROM NEW YORK TO LOS ANGELES BY JET))

(ASSINTHE THAT)

(THE TIME IT TAKES TO TRAVEL FROM NEW YORK TO LOS ANGELES BY JET IS S HOURS)

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(THE PROBLEM TO BE SOLVED IS)
THE COST OF A ROY OF MIXED NUTS IS THE SUM OF THE COST OF THE ALMOHDS OF THE FOLK AND THE COST OF THE PECANS IN THE ROX FOR A LANGE BOX THIS COST IS $ 3.500 THE WEIGHT IN FOUNDS OF A BOX OF MIXED WITS IS THE SUM OF THE NUMBER OF POUNDS
OF ALMONDS IN THE BOX AND THE NUMBER OF POUNDS OF PECANS IN
THE BOX . THIS LARGE BUX WEIGHS 3 POUNDS . THE COST OF ALMONOS
PEG BONNO OF ALMONDS, IS, S. I. AND THE COST OF PECANS PER POUND OF PECANS IS $ 1.500 . FIND THE COST OF THE ACHONDS IN THE
BOX AND THE COST OF THE RECANS IN THE BOX .)
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FINE EQUATIONS TO RESOLVED ARE NEED BOOK TO THE THE THIRD NAMED
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(EQUAL BOZSSE (COST OF PECANS IN BOX))

LEGISLE GOEST COST OF ALMONOS IN BOX)

(EQUAL (QUOTIENT (COST OF PECANS) (TIMES 1 (POUNDS OF PECANS)))

(EQUAL (QUOTIENT (COST OF ALMONDS) (TIMES 1 (POUNDS OF ALMONDS)))

(femilial (file for form a pointer), for now of maxes not restably corn.)

TENNET THE TANTOF I A POUNDER OF MIX OF HAXENERUTED CROSS CHOINGER OF POUNDS OF ALMONOS IN BOX) (NUMBER OF POUNDS OF PECANS IN

(老**生の**はん(そのもちゃちゅう ちゅうから (Marker Marsy: (441mgs : (141500) (Bollars)))

BOX) (COST OF PECANS IN BOX)))

SAME EMPLITIONS WHERE INSUPERCHANCE TO FIND A SOLUTION

(ASSUMING THAT) CASEMINE THAT)

CREPOURDSERF PERSON IS EQUAL TO (NUMBER OF POUNDS OF PECANS

INTEQUES SENTERSON IS EQUAL TO (NUMBER OF POUNDS OF PECANS

INTEQUES SENTERSON IS EQUAL TO (NUMBER OF POUNDS OF PECANS

INTERPOLOGICAL SENTERSON IS EQUAL TO (NUMBER OF POUNDS OF PECANS

INTERPOLOGICAL SENTERSON IS EQUAL TO (NUMBER OF POUNDS OF PECANS

INTERPOLOGICAL SENTERSON IS EQUAL TO (NUMBER OF PECANS IN SOME)

OF THE PERSON INTERPOLOGICAL SENTERSON IN SOME OF PECANS IN SOME OF PECANS

INTERPOLOGICAL SENTERSON IN SOME OF PECANS IN SOME OF PECANS

INTERPOLOGICAL SENTERSON IN SOME OF PECANS IN SOME OF PECANS

INTERPOLOGICAL SENTERSON IN SOME OF PECANS IN SOME OF PECANS

INTERPOLOGICAL SENTERSON I (SHE DATE, CORA DE FISHER HOE & CHORE IN LIFE CACHARA CORE LASSIMOMENTATION CONTROL TO (NUMBER OF POUNDS OF ALMONDS) IS EQUAL TO (NUMBER OF POUNDS OF ALMONDS IN BOX))

(ASSUMING THAT)
((COST OF ALMONDS) IS EQUAL TO (COST OF ALMONDS IN BOX)) (THE COST OF THE ALMONDS IN THE BOX IS 2 DOLLARS) (THE COST OF THE PECANS IN THE BOX IS 1.500 DOLLARS) (THE PROPLEM TO DE BOEVER TS) (THE GAS CONSUMPTION OF MY CAR IS 15 MILES PER GALLON . THE DESTRUCTION THE DESTRUCTION THE YORK IS 250 MILES . WHAT IS THE NUMBER OF GALLONS OF GAS USED ON A TRIP BETWEEN NEW YORK

(THE EQUATIONS TO BE SOLVED ARE)

(ENHILL COSSE! (WINNER OF GALLENS OF GAS-USED ON THE PRETMEEN. CARE SHORTER MITH WE TO THE CHEST OF THE CHE

(EQUAL (DISTANCE BETWEEN BOSTON AND NEW YORK) (TIMES 250 (MILES))) 工艺人手物等 面面包管小装件的 工作工作的 (EQUAL (GAS CONSUMPTION OF MY CAR) (QUOTIENT (TIMES 15 (MILES)) (TIMES 1 (GALLONS)))

THE ELLINAS MERE INCORP. COUNTY TO FERD A SOLUTION THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

TEGETY (LETTE TONE DE HTHMESS) (OLICE MESSENS RECUSERS (USERS THE FOLLOWING KNOWN RELATIONSNIPS)
(CENNOW COASTANCE: GENERAL SPEED) 451MA) (COMAL (DISTANCE)
(TIMES (GAS CONSUMPTION) (NUMBER OF GALLORS OF GAS USED)))

(TERMINE THAT) (ONE OF MOMBERS!) (48 ATOMOSE TA BOUNTE TO (DISTANCE BETWEEN BOSTON AND NEW YORK))

(GAS CONSUMPTION) IS EQUAL TO (GAS CONSUMPTION OF MY CAR))

(ASSUMING THAT) CAMPAGER OF GALLONS OF GAS USED) IS SOUAL TO (NUMBER OF GALLONS (THE SUM OF ONE OF THE MUMBES AND THE STADS ADMERS IN SE

(THE NORSER OF BALLONS OF BAS USED ON A TRIP BETWEEN NEW YORK AND BOSTON IS 16.66 GALLONS)

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14 3081
 (THE PROBLEM (PO ) BE SOLVED IS)
  (THE DAILY COST OF LIVING FOR A GROUP IS THE OVERHEAD COST
PLUS THE THE THINKING COST FOR EACH PERSON TIMES, THE MAMBER OF PEOPLE IN THE GROUP EQUALS 100, AND THE NUMBER OF PEOPLE IN THE GROUP IS SO. IF THE OVERHEAD COST
  IS 18 THE THE RUNNING COST , FIND THE OVERHEAD AND THE RUNNING
  COSTAFORDEACHARERSON L'ESCOVIT LE CHORETE DE MODERT DE MECYMA
(THE EQUATIONS TOWNER SOLVED ARE) IN HEALT & BURNING
  (EQUAL GO2521 (RUNNING COST FOR EACH PERSON))
  (EQUAL COISTS TOVERHEAD) STATE FROM A CREAT COST, BE RESERVED THE
  (ÉGGAL (SVERNERD COST): (TIMES ID (RUNHING COST)))
 (EQUAL (NUMBER OF PEOPLE IN GROUP) 40)
   (ÉQUAL (SAILY COST OF LIVING FOR GROUP) (TIMES 100 (DOLLARS)))
 (ESUAL (BALLY COST OF LLVING FOR SHOUP) MARLOS MOUTERREAD COST)
(TIMES (RUMMING COST FOR EACH PERSON) (NUMBER OF PEOPLE IN
GEOGRAPH)))
(COST FOR EACH PERSON) (NUMBER OF PEOPLE IN
CEPTATION (COST OF CONTROL OF 
 THE TOPATIONS WERE THEOFFICIENT TO FIND A SOLUTION
  (ASSIMING THAT)
   TERMAN "BUTSTA" COST OF PRINCE IN SOME
   ((BUMMING CORT) IS EQUAL TO (RUNNING COST FOR EACH PERSON))
  CARE ONE MENTER TO THE TANKE TO USE BOX 11
  CTHE BURNING COST HER SACH HERSON IS 2 POLLARS
      OF ALCONOS IS THE COX AND THE SOX A 
CTHE PROBLEM TO THE SOLVED IST COME NUMBER IS IS LANGER THAN THE OTHER MUMBER. FIND THE TWO NUMBERS.)
   TRYING POSSIBLE IDIOMS
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1960 308156 - 2 - 25 63 9901
   THE PROBLEM WITH AN IDIONATIC SUBSTUTION IS
    (THE SUM OF ONE OF THE NUMBERS AND THE OTHER MUMBER IS 96
   AND OME MUMBER IS IS LARGER THAN THE OTHER MUMBER . FIND THE
CTHE EQUATIONS TO BE SOLVED ARE)
    (EQUAL: 602516 (QTHER HUMBER)) OF FRANCE OF WORLD CONTROL OF THE C
    (EQUAL GO2517 (ONE OF NUMBERS))
    (SOMAL COME MINNER) (MUS 16 (OTHER MUNBER)))
    (EQUAL (PLUS (ONE OF MUMBERS) (OTHER NUMBER)) 96)
   THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION
LECT LUAL CONSUMPLY
                                                                                                                               TRYING POSSIBLE IDIOMS
    (THE PROBLEM WITH AN IDIONATIC SUBSTUTION IS)
    THE SUN OF THE MANSER AND THE OTHER NAMER IS SO, AND ONE WORKER THE STREET THAN THE OTHER NUMBER OF IND THE ONE NUMBER
  AND THE OTHER MANBER .)
 THE THE TO BE SOLVED ARE)
  THE LAS CONSIDER OF MY TELL STANDARD OF MY TEL
   TROUBLE COSTO CONE MUNICERS)
    (COUAL COME MAMBER) (PLUS 16 (OTHER NUMBER)))
    (EQUAL (PLUS (ONE NUMBER) (OTHER NUMBER)) 96)
   并能 电电影电影 医电影 医艾姆 化合物 (1) "你们,你说是一个,这个不是有什么的。"
    (THE ONE NUMBER IS 56)
    CTHE PTHEN WINDER IS NOT A CORP. I A CORP. NO. 1 A CORP. NO. 1 A CORP.
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(THE PROBLEM TO BE SOLVED IS)
                                                                                                                                                                                                                         (THE EQUATIONS TO BE SOLVED ARE)
   (THE SUM OF TWO NUMBERS IS TWICE THE DIFFERENCE BETWEEN THE
TWO NUMBERS . THE FIRST NUMBER EXCEEDS THE SECOND NUMBER BY
                                                                                                                                                                                                                          (EQUAL G93516 (OTHER NUMBER))
    5 . FIND THE TWO NUMBERS .)
                                                                                                                                                                                                                           (EQUAL GO2515 (ONE OF NUMBERS))
    TRYING POSSIBLE IDIOMS
                                                                                                                                                                                                                           (EQUAL (ONE OF NUMBERS) (PLUS 1 (OTHER NUMBER)))
    (THE PROBLEM WITH AN IDIOMATIC SUBSTUTION IS)
   (THE SUM OF FLAST MIMBER AND THE SECOND NUMBER IS TWICE THE
DIFFERENCE SETWEEN THE FIRST NUMBER AND THE SECOND NUMBER.
                                                                                                                                                                                                                           (EQUAL (PLUS (ONE OF NUMBERS) (OTHER NUMBER)) 111)
   THE FIRST NUMBER EXCEEDS THE SECOND NUMBER BY 5 . FIND THE FIRST NUMBER AND THE SECOND NUMBER .)
                                                                                                                                                                                                                          (THE ONE OF THE NUMBERS IS 56)
                                                                                                                                                                                                                          (THE OTHER MANBER (18 55)
   (THE EQUATIONS TO SE SOLVED ARE)
   (EQUAL GGZSAS (SECOND NUMBER))
   (EQUAL GOZSA7 (FIRST MUMBER))
                                                                                                                                                                                                                          (THE PROBLEM TO BE SOLVED IS)
                                                                                                                                                                                                                         (THE SUM OF THREE NUMBERS IS 9. THE SECOND NUMBER IS 3 MORE THAN 2 TIMES THE EIRST NUMBER, THE THIRD NUMBER EQUALS THE SUM OF THE FIRST TWO NUMBERS. FIND THE THREE NUMBERS.)
  (EQUAL (FIRST NUMBER) (PLUS 5 (SECOND NUMBER)))
  (EQUAL_(PLUS_(FIRST_MUNBER)) (SECOND_NUMBER)) (TIMES 2 (PLUS_(FIRST_NUMBER)))))
                                                                                                                                                                                                                          (THE EQUATIONS TO BE SOLVED ARE)
                                                                                                                                                                                                                           (EQUAL G02527 (THIRD NUMBER))
 CTHE PURSE NUMBER AS A T. SOOD TO BE TO PROVIDE A SERVED STATE
                                                                                                                                                                                                                          (EQUAL G02526 (SECOND NUMBER))
  (THE SECOND NUMBER ALSO 2.500) of the year of warren and production of the control of the contro
                                                                                                                                                                                                                          (EQUAL GO2525 (FIRST NUMBER))
                                                                                                                                                                                                                            (EQUAL (THIRD NUMBER) (PLUS (FIRST NUMBER) (SECOND NUMBER)))
                                                                                                           (THE PROBLEM TORBE (SOLVED : 18)
 (THE SUM OF TWO NUMBERS IS 111 . ONE OF THE NUMBERS IS CONSECUTIVE
                                                                                                                                                                                                                           (EQUAL (SECOND NUMBER) (PLUS 3 (TIMES 2 (FIRST NUMBER))))
 TO THE OTHER MUMBER ( ) BENDETHE TWO NUMBERS .)
                                                                                                                                                                                                                                                     ECONT LATER LINES F
                                                                                                                                                                                                                                                                                                                                           THERE'S CATHER * (193)
                                                                                                                                                                                                                           (EQUAL (PLUS (FIRST MUMBER) (PLUS (SECOND MUMBER) (THIRD NUMBER)))
TRYINGEROSSIBLESEDIOMSCORP HAMSE ()
                                                                                                                                                                                                                                                   $200570 0030<del>00</del> (12)
(THE PROBLEM: STREAM: ADSONATECESURSTUTION IS)
(THE SUM OF ONE OF THE NUMBERS AND THE OTHER NUMBER IS 111
                                                                                                                                                                                                                                                   Title (Harriss Trans)
. ONE OF THE MUMBERS LES CONSECUTIVE TO THE OTHER MUMBER . FIND
                                                                                                                                                                                                                         (THE FIRST NUMBER 13 .. . 5000) | | TREE | 1941 |
THE ONE OF THE NUMBERS AND THE OTHER NUMBER .)
                                                                                                                                                                                                                         (THE SECOND NUMBER IS 4)
                 জ্ঞান এল করে পার্যা প্রতির কর
               THE PROPERTY OF THE PROPERTY O
                                                                                                                                                                                                                          (THE THIRD NUMBER IS 4.590)
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time between it of an energy

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(THE PROBLEM TO BE SOLVED IS)
(THE SUM OF THREE NUMBERS IS 100 . THE THIRD NUMBER EQUALS
THE SUM OF THE FIRST TWO NUMBERS . THE DIFFERENCE BETWEEN THE
FIRST TWO NUMBERS IS 10 PER CENT OF THE THIRD NUMBER . FIND
THE THREE NUMBERS .)
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL GO2536 THIRD NUMBER)).
(EQUAL GO2535 (SECOND NUMBER))
(EQUAL GO2534 (FIRST NUMBER))
(EQUAL (PLUS (FIRST NUMBER) (MINUS (SECOND NUMBER))) (TIMES
 .1000 (THIRD NUMBER)))
(EQUAL (THIRD NUMBER) (PLUS (FIRST NUMBER) (SECOND NUMBER)))
(EQUAL (PLUS (FIRST NUMBER) (PLUS (SECOND NUMBER) (THIRD NUMBER)))
(THE FIRST NUMBER IS 27.50)
(THE SECOND NUMBER IS 22.50)
STHE BURD HUMBER IS 50)
(THE PROBLEM TO BE SOLVED IS)
(IF C EQUALS B TIMES D PLUS 1 , AND B PLUS D EQUALS 3 , AND
B. MINUS D. EQUALS 1 ... FIND C ...
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL GOSSIS (C))
TEQUAL (PLUE (B) (MINUS (D))) 1)
(EQUAL (PLUS (B) (D)) 3)
(EQUAL (C) (PLUS (TIMES (B) (D)) 1))
(C.18-3)
```

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(THE PROBLEM TO BE SOLVED IS)
(3 + x + 4 + Y = 11 .
 5 * Xa - 2 * Y - 1 .
 FIND X AND Y .)
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL G02541 (Y))
(EQUAL G02540 (X))
(EQUAL (PLUS (TIMES 5 (X)) (MINUS (TIMES 2 (Y)))) 1)
(EQUAL (PLUS (TIMES 3 (X)) (TIMES 4 (Y))) 11)
(X IS 1)
(Y IS 2)
(THE PROBLEM TO BE SOLVED IS)
(x / 2 - (Y + 3) / 2 = 0.
(X - 1) / 3 + 2 + (Y + 1) = 5 .
(THE EQUATIONS TO BE SOLVED ARE)
(EQUAL G02543 (Y))
(EQUAL GOZEAR (X))
(EQUAL (PLUS (QUOTIENT (PLUS (X) (MINUS 1)) 3) (TIMES 2 (PLUS
(Y) 1))) $)
(EDUAL (PLUS (QUOTIENT (X) 2) (MINUS (QUOTIENT (PLUS (Y) 3)
2555 (0)
(X IS 4)
```

(Y, 18, 1):

```
(THE PROBLEM TO BE SOLVED IS)
(THE SQUARE OF THE DIFFERENCE BETWEEN THE NUMBER OF APPLES
AND THE NUMBER OF ORANGES ON THE TABLE IS EQUAL TO 9 . IF THE
NUMBER OF APPLES IS 7 , FIND THE NUMBER OF GRANGES ON THE TABLE
```

THE EQUATIONS TO BE SOLVED ARE)

(EQUAL GO2515 (NUMBER OF ORANGES ON TABLE))

(EQUAL (NUMBER OF APPLES) 7)

(EQUAL (EXPT (PLUS (NUMBER OF APPLES) (MINUS (NUMBER OF GRANGES ON TABLE))) 2) 9)

UNABLE TO SOLVE THIS SET OF EQUATIONS

TRYING POSSIBLE IDIOMS

(DO YOU KNOW ANY MORE RELATIONSHIPS AMONG THESE VARIABLES)

(NUMBER OF APPLES)

(NUMBER OF ORANGES ON TABLE)

"I CANT SOLVE THIS PROBLEM

(THE PROBLEM TO BE SOLVED IS)
(THE GROSS WEIGHT OF A SHIP IS 20080 TONS . IF ITS NET WEIGHT IS 15000 TONS , WHAT IS THE WEIGHT OF THE SHIPS CARGO Q.)

THE EQUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

TRYING POSSIBLE IDIOMS

(DO YOU KNOW ANY MORE RELATIONSHIPS AMONG THESE VARIABLES)

(GROSS WEIGHT OF SHIP)

(TONS)

(ITS NET WEIGHT)

(WEIGHT OF SHIPS CARGO)

TELL ME

(the weight of a ships cargo is the difference between the gross weight and the net weight)

THE ROUATIONS WERE INSUFFICIENT TO FIND A SOLUTION

(ASSUMING THAT) ((NET MELGHT)) IS EQUAL TO (ITS NET MEIGHT))

(ASSMING THAT) (COMMESS WEIGHT OF SHIP))

(THE WEIGHT OF THE SHIPS CARGO IS 5000 TONS)

APPENDIX E: A SMALL SEMANTIC GENERATIVE GRAMMAR

The grammar outlined here will generate only word problems solvable by STUDENT, though not the set of all such problems.

RULES

Create a set of simultaneous equations which can be
solved by strictly linear techniques, except that substitution of numerical values in
higher order equations which
reduce them to linear equations is allowed. These are
the propositions of the speaker's model.

Choose unknowns for which STUDENT is to solve. This is the question.

Choose unique names for variables without articles "a", "an", or "the". In the problem any of these articles may be used at any occurrence of a name. In a complete model these names would be associated with the objects in the chosen propositions.

Write one kernel sentence for each equation. Use any appropriate linguistic form given in the table below to

EXAMPLES

2x + 3y = 7 y = 1/2x $y + z = x^2$

z = ?

x = first number

y = second number Tom chose

z = third number

72 times the first number plus three times the second number Tom chose is 7. The second number Tom chose

represent the erithmetic and analyse equals .550f theafirstood political tion.

value is to be found, use a kernel sentence of the form:

Find ____ What is Find to y and the state of the or What are and and very last was for more than one such unknown.

If a name appears more than once in a problem, some (or all) occurrences after the first may be replaced by a "similar" name. Similar names are obtained by the Bearmail transformations which: The followings

- a) insert a pronoun for a noun phrase we are in the name, tental and
- b) delete initial and/ or terminal substrings of the name.

Only one such "similar" string can be used to replace an oca le currence of a name, though the any number; of replacements and out can be made. The statement with

functions in the equal yet the deposit number. The state of 2 of the equal entific subscring to the last company of the the last company For each unknown whose was the sum of the second numerical second numerica ber Tom choserandeaethird) "of lauge number is equalitation the on granuseur square of theaftest sime m in the E ma ber. Whatisignthe stated seatthe you ye "Raind" brow number?

> Ave pirase P, may be ្រុកសម្រឹញ កាក់សំស្រស់ មុស មាចាន់ជា្មថ Py wolen carrie the same Chirg. This would mean that Similar atabean told atabase bed TANGUTS "first" for the turnsbor" 11 2 1175 "second enumber the chosettes and base for "second number from to " of amoun . ".T 20×9m chose"

> > Two consecutives send tences may be comested by ្រុក្ស ស្រាស្ត្រាក្នុងការ គ្នានៅការប្រែក A without the day the and statyres can be connected to a question by preceding the sentande by "If" and is boired ada galusiqua the end of the sentence by

S it is the the town town chose! by "this second appropriate entire substring to the left of "is", "equals" ora" is a collection of tence. See an awar has do a collection of the second area of the s equal to" (or the sentire said of confident substring to theoright) when the base of in S 1+1' Ni may be maplaced to the by any phrase containing the state of the word "this".

Any phrase P may be replaced by another phrase P, which means the same thing. This would mean that STUDENT had been told of this equivalence using REMERR and the sentence "P2 always and always means P1" or "P2 sometimes means P₁".

Two consecutive sentences may be connected by replacing the period after the first by ", and". A sentence can be connected to a question by preceding the sentence by "If" and replacing the period at the end of the sentence by ",".

If Ni occurs in Sy and a case Replace "the second number The case choice" in the third sen-

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in the state of the state of the state of

Replace "2 times" by "twice" and ".5" by "one half".

Connect sentences 1 and 2, and sentence 3 and the final ques tion to giver only a market of

"Twice the first number plus three times the second number Tom chose is 7, and the second number he chose is one half of the first. If the sum of this second choice and a third number is equal to the square of the first number, what is the third number?"

Summary of Linguistic Forms to Express Arithmetic Functions and the Equality Relation

x = y	x is y; x equals y; x is equal to y
x + y	x plus y; the sum of x and y ; x more than y
х - у	x minus y ; the difference between x and y ; y less than x
x * y	<pre>x times y; x multiplied by y; x of y (if x is a number)</pre>
х / у	x divided by y; x per y

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Net : drot walk

Daniel G. Bobrow was born in New York City on November 29; 1935. He attended the Bronx High School of Science, received a B.S. degree in Physics from Rensselser Polytechnic Jast itstended 1957, one received an S.M. in Applied Mathematics from Harvard University In 1958.

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