DATA DRIVEN LOOPS

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Part I: Introduction

1.1 The HIBOL Language: A Brief Introduction

The notion of the data driven loop arises in connection with our work in the Very High Level Language HIBOL and the automatic programming system (ProtoSystem I) that supports it. Although the concept is of general interest outside of VHLL's and automatic programming, we find it profitable to use HIBOL as a vehicle for our discussion and a means of narrowing the scope of our discussion. Therefore we first present a brief description of the domain which HIBOL treats.

I.I.I Flows

The HIBOL language concerns a restricted but significant subset of all data processing applications: batch oriented systems involving the repetitive processing of indexed records from data files. It provides a concise and powerful way of dealing with data aggregates. HIBOL has a single data type, the flow. This construct is a (possibly named) data aggregate and represents a collection of uniform records that are individually and uniquely indexed by a multi-component index. The components of a flow's index are called keys and the set of an index's keys is called its key-tuple. Each record has a single data field (datum) in addition to the index information. (Real-world data aggregates, such as files, with more than one datum per logical record are abstracted in HIBOL as separate flows, one for each data field.)

This term is historical. A more expressive term would be "key set", but that has historically been used to indicate the universe from which a key may take its values.

1.1.2 Flow Expressions

Flow expressions can be formed through the application of arithmetic operators such as "+" or "*" to flows. The meaning of such an application to two flows is that the operation is applied to the data of corresponding records (those with matching indices) of the argument flows. The result is a new flow, having a record for each matched pair for which the operation was performed. The index value of such a record is identical to that of the matched pair, and the datum value is the result of the operation performed on the data of the pair. This concept is generalized to an arbitrary number of flow arguments.

Flow expressions can also be constructed using a conditional operator (similar to a "CASE" statement) which evaluates logical expressions in terms of corresponding flow records in order to select and then compute an expression as the individual records of the flows are processed. The logical expressions are constructed using the arithmetic comparison operators ">", "=", and "<". In addition the PRESENT operator may be used to test the presence of a record in a flow for a given value of the index of that flow. These may be composed using the logical connectives "AND", "OR" and "NOT".

Finally, there is a class of reduction operators permitted on flows and flow expressions. The function of such an operator is to reduce a flow with an n-key index to one with an m-key index, where m < n, and the key-tuple of the m-key index is a subset of the key-tuple of the n-key index.

All records of the argument flow that correspond to a single record of the result form a set to which a reduction operator (e.g. "maximum", "sum") can be applied to obtain a single value.

I.1.3 Flow Equations

Relationships between flows are are expressed by flow equations of the form:

<flow-name> IS <flow-expression>

where <flow-name> is a named flow and <flow-expression> is a flow expression in terms of named flows. The right- and left-hand sides must have identical indices.

I.L4 Example

Consider a chain of stores whose items are supplied from a central warehouse. The collection of store orders for item restocking on a given day can be thought of as a flow called, say, CURRENTORDER. A record of that flow contains the quantity ordered by a particular store of a particular item. Each record has as its datum the quantity ordered and a 2-component index identifying the store making the order and the item ordered (the keys of the index are a store-id and an item-id). Let BACKORDER be the name of a flow (of similar structure) representing the collection of (quantities of) previous orders that could either not be filled only partially. The HIBOL statement

DEMAND IS CURRENTORDER + BACKORDER

describes a new flow DEMAND representing the total demand of each item by each store. That is, each record in DEMAND contains a 2-component (item-id, store-id) index identifying its datum which is the sum of the data for the same item and store in the CURRENTORDER and BACKORDER flows.

The HIBOL statement

I TEMDEMAND IS THE SUM OF DEMAND FOR EACH ITEM-ID

illustrates the use of the reduction operator SUM. It describes across the USE of the reduction operator SUM. It describes across the USE of the reduction operator SUM.

the total demand of each item from all stores. That is, each of its records has a single-component index (item-id) identifying a particular item; and its damm is the total quantity in demand summed across all stores in the chain.

I.1.5 Additional Information

The computational part of a data processing system can be described by giving a full set of flow equations of the type shown above. To complete the system's description additional data and timing information must be given:

- for each flaw, the components of its index, the type of its data value, and the periodicity with which it is computed

AND DO NOT BE A SECTION OF

- for each key its type
- for each period its time relation to other periods

1.2 Iteration Sets and Explicit HIBOL

A flow expression, as explained above, represents a set of records obtained by the record-by-record application of a formula to the records of the flows that appear as terms in the expression. In this paper we shall be interested in exactly for which index values (and thus records) the indicated formula is applied. The set of these index values is termed the tteration set²

The HIBOL language is rather informal about specifying iteration sets. It contains abundant provisions (through the use of defaults) for implicit semantics based on the presence or absence of records in the flows appearing in flow expressions. For example, the HIBOL flow expression

CURRENTORDER + BACKTROER

² After Baron [1].

describes a flow that has a record for each index value for which either CURRENTORDER or BACKORDER (or both) has a record:

if both flows have a record for a given index value, the resultant flow has a record with the same index value, whose datum is the sum of those of the corresponding records in the two flows:

if only one flow has a record for a given index value, the resultant flow has a record with the same index value and the same datum value;

otherwise there is no record in the resultant flow.

One way of looking at the semantics of addition in HIBOL, then, is to convene that the operation + is performed if and only if at least one of its operands is present and that each missing operand is treated as if it were the additive identity (0).

Although such conventions are convenient in writing HIBOL, for the sakes of clarity and rigor, we require fully explicit iteration set specifications. Such can be obtained through the thorough use of the HIBOL primitives IF and PRESENT. Thus, the fully explicit form of the above HIBOL flow expression would be:

CURRENTORDER + BACKORDER IF CURRENTORDER PRESENT

AND BACKORDER PRESENT

ELSE CURRENTORDER IF CURRENTORDER PRESENT

ELSE BACKORDER IF BACKORDER PRESENT

Here the index values for which the flow expression's formula is to be applied have been made explicit by restructuring it as a three-clause conditional expression in terms of three sub-expressions, each of whose iteration sets is specified by an associated condition on the presence of records in the flows involved. This is a legal HIBOL flow expression, although in view of the existing conventions it is overspecified (redundant). For our purposes we will distinguish a

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not legal flow expressions in FE-HIBOL:

otherway there is no record in the resultant flow.

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thorough use of the HIBOL primitives IF and PRESENT. Thus, the fully explicit form of the

above HIBOL flow expression would be:

Throughout the rest of this paper, unless explicitly stated otherwise, all HIBOL expressions will be INGERENTORIES OURSELL OF THE PRESENT OF

written in FE-HIBOL 369 83080X0A0 CMA

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TV32784 H30R0TW38RD0

IF BACKONDER PRESENT

RECENT BACKGROER

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explicit by restructuring it as a force-clause conditional expression to terms of three sub-

expressions, each of whose iteration sets is specified by an associated condition on the presence of LORIH adT aman gaitmorn atch ai hostrohou ad tunn mitgitues LORIH adT ecords in the flows involved. This is a legal HIBOL flow expression, although in view of the

in ProtoSystem I, in fact, immediately after a HIBOL data processing system is described it is translated into an internal language (DSSL) which has exactly this supplement.

description is declarative in nature: it describes the relationships among the flows. An implemented data processing system is procedural in nature: it must describe in detail how the flows are computed. The flow equations must be reinterpreted as basic computation steps (with an output flow and one or more flows as inputs) and constraints on the order in which these computations can be performed (the computation producing a flow must be performed before any computations using that flow) must be made explicit.

Design:4

The implementation will make use of files of data to be processed by job steps which will in turn create other files. Each file will contain the information represented by one or more flows; each job step will perform the processing to satisfy one or more flow equations. The design of each file (information contained, organization, storage device, record sort order) and of each job step (equations implemented, loop structure, accessing methods used) should be made in such a way as to minimize some overall cost measure (e.g. dollars and cents cost, time used, number of secondary storage I/O events) for the execution of the data processing system. Typically this requires dynamic (behavioral) analysis of tentative design configurations.

Code Generation:

The system's design must be coded in a supported high-level language so that it can be executed.

1.4 Data Driven Loops

Each flow equation represents a computation whose implementation is essentially iterative in

⁴ In ProtoSystem I the design process is performed by the Optimizing Designer module.

there That is, the chilling and an innition and and the line and an over the records of the Cowled in the flow insprention or the right that Mill Deficient the Late Control of the to generate the request of the flow on the detailed big. The William William World longuages this flow and one or more flows as inputs) and continue of a sed with a good base of militaria. can be percusal that the constitution or distribution and the production of the constitution of the canal of a loop can be devised that will produce the entire flow appealing the life and state of the flow equation from the flows appearing on the right-hand side. In functional terms, the flows on the tight hand nice of the flat equation who called the highs to the militarial time their flats. turns create other files. Each file will corning to problem to the question and recourse the Bloghod the imprepatite by east white, for your will visit vitte it is cuspensis to be grammad band of shiften. For enough, and the will climb excitate the C. India (equations implemented, loop structure, accessing methods used) should be made in such a college to manufacte some overall cost measure of the measure of the measure and the same and a sumball of decondary storage 1:0 events) for the execution of the data processing system. Typically this requires dynamic (behavioral) analysis of tenlative design configurations. The body of the corresponding loop will distinguish two cases and even

I. Records in both A and B are present for the current value of the loop lader, in which case a corresponding record of the flow S is produced whose difficult in the said of A and B.

The system's design must be ceded in a supported high-level language so that it can be

2. Only A contains a record corresponding to the consent value of the index, in which patterness case a corresponding record of S is produced that is identified to \$5 record.

If neither of these cases obtains, no output record is produced."

14 Data Driven Looks

Clearly, in a correct implementation the body of the hop must be performed for every index of avitated villateness at notationesigni stocks retaining the and to produce an empat record. We call

⁵ APL demonstrapped and Richard additing County and of the second of VHLL

any set of values for a particular index an index set and we distinguish two special kinds of index sets:6

The set of index values for which a flow F contains a record is called the *index set* of F (denoted IS(F)).

The set of index values for which an input flow F₁ contains a record that will be used in generating a record of the output flow F the critical index set of F₁ with respect to F (denoted CIS_F(F₁)).

These two should not be confused. CIS_F(F_I) for some flow F will often be a proper subset of IS(F_I).⁷

The problem we face is that of finding some way of enumerating the critical index sets of each input so that loop can be properly driven. It is generally impractical to use the set of all possible (legal) index values for which an input might have a record: For one thing this set may be unbounded. Even if it is finite and enumerable, it will often be much larger than the critical index set and thus grossly inefficient. In the DEMAND flow equation example given above, for instance, the critical index set of the input flow CURRENTORDER is likely to be orders of magnitude smaller than its maximum possible size (the case where every store has orders for every item).

A much more efficient way of enumerating a set of index values that is assured to cover the critical index sets of the inputs is to use the union of the index sets of the input flows. This will work because a record of the output can be produced only if there is some input flow in which that

⁶ Unfortunately, this terminology is at variance with that used by Baron in his thesis [1]. Baron uses the term "critical index set" to mean what we call the "index set".

⁷ On no account, of course, can it be other than a proper or improper subset of IS(F₁).

⁸ This statement is somewhat oversimplified, but it will suffice for now. A fully precise statement of the problem is given by the Fundamental Driving Constraint in Part IV.

record is present Margarenethy animal shear and a north analytical shift by feeding the imput flows (which have to be read anyway). A hop that is thus driven by index values supplied by its inputs is said in his anderember and and thurburst to this driven by index values supplied as driving flows (the set of flows that drive a hop are called its driving flow and The structure and implementation of driving flow and the set of flows that drive a hop are called its driving flow and The structure and implementation of driving flow and the set of flows that drive a hop are called its driving flow and The structure and implementation of the set of flows that drive a hop are called its driving flow and The structure and

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Part II: Structure of Data Driven Loops

Before a general treatment of data driven loops can be developed it is necessary to examine the structures of the loops encountered in the HIBOL system. We begin by presenting a taxonomy of computation types and their corresponding loop implementations.

11.1 Loop Terminology

Before discussing loop structures it is useful to establish some terminology. By the term loop we mean a control construct which somehow enumerates a set of values for a loop-index and which performs a fixed sequence of statements (its body), once for each value of the loop-index. A loop may contain one or more loops within its body. The inner loops are said to be nested within the outer (enclosing) loop and the structure as a whole is called a nested loop structure. Each enclosure defines a different level of the nested loop structure. The degenerate case of a nested loop structure, where there is no loop in the body of the outer loop, is called a single-level loop, since there is only one loop level.

A totally nested loop is a nested loop structure whose component loops are totally ordered under enclosure (i.e. for any two loops L_1 and L_2 either L_1 is inside L_2 or L_2 is inside L_1).

11.2 Kinds of Computations and Their Loops

Each run (computation, job step, program) in the implementation produced for a HIBOL description of a data processing system is essentially a loop that iterates over the records of its input files to generate records of its output file(s). The structure of this loop depends on the nature of the computation being performed. We will begin with computations that directly implement single HIBOL flow equations of various types. Then we will consider computations that implement more than one flow equation (aggregated computations) simultaneously.

H.2.I Simple Computations

Part Il Structure of Data Driven Lords

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> PAY IS HOURS : 3.86

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Before discussing to the term the color dead to the term took This assumes that there is a flow APAIS induced by laughtpartify to as its, datum the number of hours the indicated salestiges resulted to Body salestipic to part of \$3.00 hours, with time and a hold for exercisms ANV is a flow additioning the green year thirties of the employee who worked the had a questionable reported to the tends to the questions in two The long implementary this kind of prosperation dead the single mind of the single loop having a single input life which is the driver Durant Annichment quainted the higher w is rend and used to provide both a datum and index value for the body, which calculates the datum of the corresponding unique sayed surveilles that assemblement this delicate and the durient under enclosure (i.e. for any two loops I., and L., enter I., is insole L.; or L. Streed I., sular salan in the SEAL language (see Appendix I) this would look like. 112 Kinds of Computations and Their Leaps

Earth run (computation, job step, program) in the implementation produced loss s MEOU description of a data processing system is excendably a loop that theretes over the records of its imput files to generale records of its output file(s). The structure of this hop depends on the nature of the computation being performed. We will begin with comprisations that directly implement thigh HIBOL Row's quations of various types. Their we sail oquator compositions that combonies inner than one flow equation (aggregated computations) sumificanco-usly for each (employee-id) from HOURS

get HOURS (employee-id)

- PAY (employee-id) - Pay (employee-id)

informed (HOURS (employee-id)) and not (HOURS (employee-id) > 48)

then HOURS(employee-id) * 3.0

else if defined (HOURS (employee-id))

then 120.0 + (HOURS(employee-id) - 40) * 4.5

F2.881280 9/48444 F1

else undefined

if defined (PAY (employee-id))
then write PAY (employee-id)

OF A SHORT ON THE

end

The for-end construct represents the basic iteration over values of the index employee-id. It specifies that the values for the index are obtained from the HOURS flow. For each index value, the corresponding record of HOURS is read, the corresponding record of PAY is generated, and (if generation was successful) that record is written out. Notice that the PAY calculation is a direct translation from the HIBOU flow equation.

For reasons of exposition the loop implementation presented here is of the most general form.

An actual implementation would incorporate various efficiency enhancing improvements.

Nevertheless, we shall continue to use such forms to show explicitly where I/O and testing occur conceptually.

For instance, since the for has to read the next record of the driver to get the current index value, the get could be omitted. Furthermore, the defined tests in the PAV calculation could be omitted since they are testing the presence of record which must be present. Finally, in this computation, the check before output could also be omitted.

II.2.2 Matching Computations

A matching computation computes a non-reduction flow expression involving two or more flows. Thus it is similar to a simple computation, but instead of operating on a single record of a single input flow to produce an output record, it operates on a set of corresponding records, one from each input flow. Correspondence is established by common index values. The name "matching computations" derives from the necessity of matching up the records of the inputs by index values before they can be operated on.

Two sub-classes of matching computations can be distinguished depending on whether all of the inputs have indices with identical key-tuples or not.

II.2.2.1 Expressions Involving Flows with a Uniform Index

Consider the a pay calculation similar to that given above, but where employees are paid various hourly rates. Let RATE be a flow, indexed by (employee-id), each of whose records has as its datum the hourly pay rate for the employee indicated by its index value. The pay calculation then becomes

PAY IS HOURS * RATE

F HOURS PRESENT
AND MAKE PRESENT
AND NOT HOURS > 48

ELSE
RATE * 48 +
(HOURS - 48) * 1.5 * RATE IF HOURS PRESENT

HOURS and RATE have identical indices, each consisting of the single key "employee-id". The loop that implements such a computation has a single level.

Because a record of the output is generated only if there is a record in the HIURS file, that

file alone is sufficient to drive the loop. (Alternatively, by similar reasoning, the RATE file could be used to drive the loop.) This is the simplest case of a matching computation because only one input is needed to drive the loop. (The computation of the flow S above is also of this type.) On each iteration the next record of the HOURS file is read, the corresponding RATE record is fetched, and the computation of gross pay performed.

This loop is represented in the SEAL language thus:

for each (employee-id) from HOURS

get HOURS(employee-id)

get RATE(employee-id)

PAY(employee-id) =

if defined (HOURS (employee-id)) and defined (RATE (employee-id)) and not (HOURS (employee-id) > 40)

then HOURS (employee-id) * RATE (employee-id)

else if defined[HOURS(employee-id)]
and defined[RATE(employee-id)]:

then RATE(employee-id) *40 + (HOURS(employee-id) *1.5

else undefined

if defined [PAY (employee-id)] then write PAY (employee-id)

end

Again, the defined checks on the driver, HOURS, are superfluous. But those on RATE are necessary (to determine whether the corresponding get was successful) and the defined check on PAY is necessary (so that a record is written if and only if a datum was generated).

Now consider the HIBOL flow equation for the DEMAND flow given above:

file alone is sufficient to deliberate case of a manching composition recesses only one used to drive the loop. This is the simplest case of a manching composition recesses only one imput is needed to drive the loop. The computation of the flow S above is also of the type.) On sach increasion the next record of the HOLES like is read the corresponding RATE record is particled, and the corresponding RATE record is particled, and the the corresponding RATE record is particled, and the the corresponding that is particled, and the the corresponding that the third computation of gross pay performed.

And the corresponding of the blank state of the stat

When there is more than one driver for a computation some of the drivers will have records (bi-osyolicas) child have records for a given index while the others do not. ** If the drivers have that records supply in the same order (say, alphabetically) by index values, the loop may be parliamed by analog only, one pass through the inputs in the flowing manner.**

if defined HOARS (employee-id))
and defined (RATE (employee-id))

- Q. Read the first record of each input. 184 < (b) 9-up (gree) 250(0) Jon bns
- I. Use the smallest today within annalythic the tolking the tolking their and perform the loop body, fetching other non-detver muscle if necessary.

 [thi-saus last 2010 then lab ti sale
- 2. Discard all driver records with the industrial with his his all the next record of every driver whose record was discarded.

 + 84 * {bi-sayoique} 37AR mad)
- 3. Repair (employed and # 184 (septemb) 205 (El)

yeivish and single his self-best states and at a steem and the rebre and the self-best states are states and the rebre and the rebre and the rebre and the states are states and the rebre and the rebre and the rebre and the rebrest self-best states and the states and the states are states and the states and the states and the states are rebrest and the states are rebrest and the states are respectively. His states are states and the states are necessary and the states are repersonance at states are necessary and states are necessary and states are necessary and states are necessary and states are repersonance whether the corresponding get was successful) and the defined check on PAV is

necessary (so that a record is matter for the call of the content of the call of the call

Now consider the HIROL flow equation for the DEMMI flow given above

These details are implicit in the SEAL representation of the loop which is simply:

for each (item-id, store-id) from CURRENTORGER, BACKONDER

get CURRENTORDER (item-id, store-id)

get BACKORDER (item-id, stone-id)

DEMAND (item-id, store-id) = ...

if defined [DEMAND (item-id, store-id)] then write DEMAND (item-id, store-id)

end

II.2.2.2 General Discussion of Expressions Involving Flows with Mixed Indices

The treatment of mixed-index flow expressions in this paper will be restricted to those that are legal in HIBOL. The restrictions that HIBOL imposes are made for good reasons. A brief discussion of the various conceivable types of mixed-index flow expressions is presented here in order to show the motivation behind these restrictions.

The various cases where the flows in a flow expression have mixed indices (i.e. their indices have different key-tuples) can be distinguished by the set interrelationships among the key-tuples.

Consider the case where flows have disjoint key-tuples (e.g. (w, x) and (y, z)). Correspondence among records of such flows is meaningless, so we do not allow them to appear in the same flow expression.

Now consider the more general case where there is intersection among index key-tuples, but the union of their pair-wise intersections is not identical to their (simple) union. In this case correspondence is always ambiguous. For example, consider the two flows: A with index (x, y) and B with index (y, z). Suppose that there are records in A for the particular index values (x_1, y_1) and

 (x_2, y_1) and that there are records on B for index values (y_1, z_1) , (y_1, z_2) and (y_1, z_3) . Which of A's records correspond to which of B's records?

For correspondence to be meaningful and unambiguous it must be the case that the union of the pair-wise intersections of the key-tuples of the indices involved is identical to their union. This is always the case when there exists an index among the flows involved whose key-tuple is a superset of all the key-tuples of the other flows.

To be sure, there are other ways of satisfying the condition of the preceding paragraph. These involve conjunctions of three or more indices. Consider, for instance, the three flows: A with index (x, y); B with index (y, z); and C with index (x, y). Corresponding triplets are all unique and unambiguous, of the form (x_i, y_i) , (y_i, z_k) , (x_i, z_k) . For the sake of simplicity, however, this case is prohibited in HIBOL.

IL223 Mixed-Index Flow Expressions Allowed in HIBOL

It is possible in HIBOL to apply operators to two or more flows having different indices as long as each index is a sub-index of the index of some unique flow involved (i.e. as long as the key-tuple of each index is a subset of the key-tuple of the index of the unique flow). Clearly, the index of this unique flow is identical to the index of the flow expression as a whole. HIBOL allows a mixed-index flow expression only if its computation can be driven by the set of those flows involved having indices identical to that of the flow expression.

¹² Of course, we could allow all pairs to match (in Cartesian product fashion) so that the expression A + B would represent the six possible combinations of additions for these 5 index values; but this would change (extend) the semantics of HIBOL.

For example, suppose we want to calculate the extended prices of the current store orders (the flow CURRENTORDER) in our store chain example. Let PRIEE be a flow indexed by (item-id), each of whose records has as its datum the per-item price associated with the item-identified by its index. The flow equation for EXTENDEDPRICE, indexed by (item-id, store-id) would be expressed in HIBOL thus:

EXTENDEDPRICE IS CURRENTORDER * PRICE IF CURRENTORDER PRESENT AND PRICE PRESENT

amoral of the design of the contract of the

The intent here is: for every record in CURRENTORDER find the corresponding record in PRICE and, if the latter is present, multiply their respective data to calculate the datum of a corresponding record in EXTENDEDERICE. Notice that because PRICE and SURRENTORDER have different indices ((item-id) and (item-id, store-id), respectively) the notion of correspondence must be extended in a natural way from pure identity of index values. We convene that for a particular value of item-id the index (item-id) matches any index (item-id, store-id) with the same value of item-id; regardless of the value of store-id. This augmented definition of correspondence is extended to the general case where the key-tuple of one index is a subset of the key-tuple of mother. That is, for given values of $k_1, ..., k_m$ the index $(k_1, ..., k_m)$ is said to match any instance of an index $(k_1, ..., k_m, k_{m+1}, ..., k_n)$ with the same values of $k_1, ..., k_m$ regardless of the values of $k_1, ..., k_n$.

Since a set of input flows; each with index identical to the flow expression's, can be used to drive a mixed-index matching computation, its implementation is similar to that for a uniform-index matching computation: the sorted drivers are read in such a way as to enumerate the critical index sets of all of the input flows; the resulting index values are used to fetch records from the rest of the inputs (including all those whose indices are sub-indices of the flow expression's index).

¹³ The extended price of a quantity ordered is the product of the quantity and the per-item price.

For example, suppose we wend doubted in the miniman polyment of the flow CEMELATERS.) In our store chair for miniman polyment of the flow CEMELATERS.) In our store chair for the flow central has as its datum the per tem price associated with relumnia damined by associated with relumnia damined by associated with relumnia damined by associated with relumnia to a supposed in the flow equation for EMERCOPRICE, indexed by (incord, stored) would be expressed in HISOL thus

EXTEMMEDIATION IS CUMPENTURDER & PRICE IF ... -CUMPENTATION PRICE PRICE PRICE PRICE PRICE

The colour bette of the every record in CURRENTORDER and its to executable broughprostific present, multiply their respective data to executate the datum of a contesponding of the latter is present, multiply their respective data to executate the datum of a contesponding record present qualificative present data and the data and the contesponding all the present present data and the contesponding all the present data and the executation of the present data and the pr

In the case, where the control of Carifoldian antimoral by tentral the Establishment CE: to comparation to implemental as a second top structure with tentral and tentral the willer).

Basically, the outer loop chooses a value of the sub-fidex (item-id) and fetches the corresponding PRICE record. Then it performs the inner loop. Within the inner loop the value of the item-id key is held constant. All corresponding records of CURRENTORDER are read and the computation described in the flow equation is performed using the data of these records together with the datum of the PRICE record fetched in the outer loop. The results are used to build and output the corresponding records of EXTENDEDPRICE. This process is repeated until the flows are exhausted.

In detail the implementation is as follows. Before either loop is entered a record of CURRENTORDER is read. The outer loop uses this record to obtain the first value of the sub-index (item-id) and fetches the corresponding record from PRICE. Then it performs the inner loop. The inner loop uses the current record of CURRENTORDER and continues to read records sequentially from CURRENTORDER until the sub-index is observed to change or an end-of-file condition occurs. When either of these conditions occurs, it exits to the outer loop. If an eof has occurred, the outer loop exits. Otherwise it iterates, using the sub-index value of the current CURRENTORDER record as the new value to be held constant in the inner loop, fetching the corresponding PRICE record and performing the inner loop again.

The corresponding SEAL code is:

for each litem-id) from CUPPENICADER

get PRICE(item-id)

for each (store-id) from CLAVENTOPOER(item-id)

get CUPPENIORCER(iten-id, store-idfa commet eur

EXTENDED PRICE (i ten-id, store-id) =

if defined (CURRENTORCER (item-id, wtere-idf) and defined (PRICE (item-id))

then CURRENTORDER (item-id, store-id) * PRICE (item-id)

else undefined

if defined (EXTENDEDPRICE (item-id, store-id)) then write EXTENDEDPRICE (item-id, store-id)

Notice that the outer loop is driven by CURRENTORDER (ohe whole flow); but that the inner loop is driven by CURRENTORDER (i ten-id) (the sub-flow of CURRENTORDER consisting of just those records whose indices correspond to the value of the sub-index (item-id) fixed by the outer loop). What this means is that for the outer loop the next value of the sub-index (item-id) will be taken from the next record of the CURRENTORDER flow. But for the inner loop the next value for the sub-index (store-id) will be taken from the next record of the sub-flow of CURRENTORDER corresponding to the current value of (item-id); if there are no further records in CURRENTORDER for this fixed value of (item-id) this will be treated just like an end-of-file condition and the iteration of the inner loop will terminate. Thus the inner loop is driven by a succession of sub-flows, one for each iteration of the outer loop.

This nested-loop implementation scheme is easily extended to 3 or more loop levels when appropriate sorting constraints hold among the flows involved. For example, suppose that there

are 3 flows involved: A with index (k1, k2, k3); B with index (k1, k2); and C with index (k1). And suppose further that B is sorted by k1 and that A is sorted first by k1 and, within segments corresponding to a fixed value of k1, the records of A are further sorted by k2. Then the flow equation can be implemented using a nested loop structure involving 3 loops (innermost loop, middle loop and outermost loop. The outermost loop chooses a value for the key k, to be held constant within the middle loop (and perforce in the innermost loop, which is contained in the middle loop). It also fetches the corresponding record of C for use within the contained loops. Then it executes the middle loop, which, in turn, choose a value for the key ke to be held constant within the inner loop. The middle loop also fetches the corresponding record of B for use within the innermost loop. Then it executes the innermost loop. In the innermost loop the values of the keys k₁ and k₂ are held constant. The innermost loop reads all corresponding records of A, using their data and those of the already read records to perform the calculations described in the flow AND THE PROPERTY OF THE PARTY O equation and to build and output the records of the output flow. When the innermost loop has July man day a remedia more than a contraction read and processed all records of A corresponding to the fixed values of k1 and k2, it exits to the forther and a contraction to a company of the influence o middle loop, which chooses a new value for k2 and iterates. When the middle loop has exhausted िक्षा । त्या : भोगापुर १ वस्ता १५० ०५००,५६०० १ हैंदे में द्वीतेष्य हो। सामास्त्रात्व प्राप्त सामार् all possibilities for the value of k₁ fixed in it, it returns to the outermost loop, which chooses a new and a fire to the property of the state of value of k₁ and iterates. This loop structure expressed in the SEAL language looks like:

are 3 flows involved: A with index (k₁₁ k₂, k₃h 3 with index (k₁₁ h₂h, h₃h 5 with index (k₁₁ k₂h, h₃h 5 with index (k₁₁ h₃h 6 with index (k₁₁ h₃h 6

equation and to build and output the records of the output flow. When the innermost loop has read and processed all records of a consequence of the fixed values of k₁ and k₂, it exits to the middle loop, which chooses a new value for k₂ and iterates. When the middle loop has exhausted middle loop, which chooses a new value for k₂ and iterates. When the middle loop has exhausted all possibilities for the value of k₁ fixed in it, it returns to the outermost loop, which chooses a new value of k₁ fixed in it, it returns to the outermost loop, which chooses a new value of k₁ and iterates. This loop structure expressed in the SEAL language looks like:

there Still is applied to CENNIA. However, constitutions such as:

TREMERNAD IS THE SAM OF COMPENSABLE + MICHAELER
FOR FACILITIES.

ITERCEPORE IS THE SAM OF DEBIND FOR EACH INCH-10

(written in HIBOL 19) are also possible. In any event, the augument to the suffection operator is

¹⁴ The standard HIBOL form is used here for chirty and constructs, the corresponding FE-HIBOL form is rather pendenge.

treated as a single flow.

Conceptually, the argument flow is partitioned into subsets (sub-flows) by an equivalence relation defined on the sub-index (a key or keys) indicated in the FOR EACH clause; then the reduction operator is applied to the members of each subset to generate the value of the datum of the output record corresponding to that subset. For instance, in the first example given above the DEMAND flow is conceptually partitioned into record subsets by item-id. Thus, all records in DEMAND whose index contains the value item-id, for the item-id key are in one subset, all records for item-id = item-id, are in another, and so forth (empty subsets are ignored). The datum for the record in ITEMDEMAND with index = (item-id,) is calculated by summing all of the data in the records in the subset corresponding to item-id = item-id.

Conceptually, the implementing iteration for a simple reduction expression in a single flow consists of two loops, one nested inside the other. The inner loop implements the application of the indicated reduction operation to a subset of the input's records. Within this loop the value of the sub-index defining the subset is held constant. Returning to the SUI OF DEMAND example, the inner loop implements the summation of the data of the records of each subset of DEMAND. That is, the inner loop is performed for each value of item-id; for which there are records in DEMAND. Within the inner loop the particular value of the key item-id is held constant, all records of DEMAND corresponding to that key value are fetched and their data are summed.

The outer loop performs clerical work. It chooses a value the subsetting sub-index (e.g. a value of item-id), executes the inner loop (which fetches records of the input corresponding to the chosen sub-index and, for example, adds them to the accumulator), and when the inner loop is finished, it uses the resulting value as the datum of the output record corresponding to the chosen sub-index, and writes that record out.

It continues to the state of th

Conceptually, the implementing iteration for a simple reduction expression on a single flow consists of two loops: one insteed inside the untel the inner toop implements the application of the indicated reduction operation to a subset of the liquid legicle. Within this loop the value of the subset is held constant. Seturing the san of the late of the late of the property of the late of the property of the late of the finite toop implements the summation of the data of the records of their in personnel in personnel to the finite times loop is performed for each value of item-id for which there are records in personnel the inner loop the particular value of the key item-id is held constant. All records of TEPANO.

corresponding to that key value are forched and their data are summed.

The outer hop performs cierical work. It chooses a value the subsecting sub-index (2.8. a value of from id), executes the inner hop (which fetches jecords of the input corresponding to the chosen sub-index and, for example, sold instance), and when the inner loop is finished, it uses the resulting value as the datum of the couplit record corresponding to the chosen sub-index and writes that record out.

It may at first seem unnecessarily baroque to initialize the actumulator sum to "undefined" in the outer loop, test it in the inner loop for definedness and then initialize it if undefined. In this simple example we could just initialize it to 0 in the outer loop and not bother with the definedness checks. We have chosen the former course for two reasons. First, we wish to make explicit the conditions under which the sum (and thus a record of the output ITEMPENANO) is defined for a given value of the key item-id. Second, a little thought will show that for other reduction operations (viz. MAX and MIN) initialization of the accumulator must (at least conceptually) be postponed until the inner loop where the initializing value is obtained by the first get: Moreover, in general, when computations are aggregated (see below) and more than one activity is performed in the inner loop, it is then possible (if some driver besides DENANO is used) that for some values of item-id no sum is calculated in the inner-loop and thus som is undefined on exit from that loop.

If the input flow is not sorted as above, the computation for a reduction operation becomes somewhat more complex. One possibility is to create and matrix in separate accumulators for each value of the sub-index value occurring in the input flow. Since the number of accumulators cannot be known a priori (i.e. at compile time), storage for their thost be allocated on the fly (during execution of the computation). In PL/I, for example, the following (roughly outlined) scheme might be used:

Declare an accumulator array to have CONTROLLED storage.

Make a pre-pass through the input flow to count the number of different sub-index values occurring.

Execute an ALLOCATE statement to define the size of the array:

Make a second pass over the input flow to perform the accumulation.

Write all accumulated values out to the output flow.

In this scheme there are two separate loops instead of a totally nested loop structure.

Alternatively, a nested loop, multi-pass scheme could be implemented. The outer loop would

outer loop, test it in the inner hop for defined as sum market is undefined as this support was policied as the support of the former course for two reasons. First, we wish to make explicit the contitues a until which the sum (and thus a record of the output i substantially counted for the support is substantially counted for the support of the output is substantially counted for other reduction operations (was the inner loop where the initializing value is obtained by the friends molecular molecular in successful molecular in the inner loop where the initializing value is obtained by the friends molecular molecular in the inner loop where the initializing value is obtained by the friends and the first field of the friends and the first field of the friends and the friends and the first field of the first field of the field of

If the input flow is not soried as above, the computation for a reduction operation becomes somewhat more consistence of the sub-index value occurring in the input flow. Since the number of accumulators cannot be input flow in the input flow of the computation. In PLH, for example, the following (marghty outlined) scheme might be used:

Declare an accumulator array to have COM HOLLED storage.

IL3 General Last Structure and Description

Make a pre pass through the input flow to count the number of different sub-index

Strating, we will formalise the structure of much adoptional property and the structure of the structure of

Make a second pass over the input flow to perform the accumulation.

Write all accumulated values our to the output flow.

in this scheme there are two separate keeps instead of a totally nested lemp crossure.

Alternatively a nested loop, multi-pass scheme could be impiercented. The contribute which

II.3.1 Formal Representation of Nested Loop Structures

We have seen that the basic control structure used in implementing a computation is the totally nested loop. Associated with each loop in the nesting is a set of keys that it will fix and which will remain constant in the loops it contains. It is easy to see that this constraint means that the set of keys fixed within any loop is necessarily a (proper) superset of the set of keys fixed within any of its enclosing loops. Thus, the set of keys fixed within a loop is sufficient to determine its level in the nesting.

Now notice that the body of every loop (except the innermost one) contains exactly one toplevel loop; thus, the body is naturally divided into three parts:

the prolog-those actions performed before the enclosed loop the enclosed loop the epilog-those actions performed after the enclosed loop.

Conceptually, then, a totally nested loop can be represented as a list of loop descriptions, one for each of the component loops. Each such description would consist of a level identifier (indicating at which level of nesting it occurs) and the prolog and the epilog. However, during the design stage, while implementations are being developed and, in particular, when computation aggregations are being considered, it is useful to distinguish 3 classes of actions within the body of a loop:

Prolog-those actions that must be performed before the enclosed loop

Epilog-those actions that must be performed after the enclosed loop

General-those actions that could end up in either the prolog or the epilog.

It is also useful to separate I/O actions from the other actions. Thus, we represent each loop in the nesting as a structure of the following form: 15

This representation, and the theory of computation aggregation associated with it are due largely to the work of R. C. Fleischer [2], who improved on the earlier work of R. V. Baron.

(Level.

(Inputsp. Prolog. Outputsp) (Inputsg. General, Outputsg) (Inputsr. Epilog. Outputsr))

where

Level indicates the depth of the loop in the nesting

Inputsp are the files (necessarily) read in the Protog section.

Inputs_G are the files (necessarily) read in the General section.

Inpute_E are the files (necessarily) read in the Epi log section.

Outputspare the outputs generated in the Prodograction (possibly used in the enclosed loop or in the Epi log section)

Outputs_G are the outputs generated in the General section.

Output s_E are the outputs generated in the Epi l og section.

II.3.2 Computation Implementation

The implementation of a computation as a nested loop structure reduces to the problem of determining how many and which levels are to be in the totally nested loop and where the I/O and computations go. The answers to these questions are constrained by the forces of necessity and efficiency.

11.3.2.1 Level Position of HO and Calculations

The levels at which each input should be read, each output should be written and each calculation should be performed are determined by the following guidelines:

Inputs: Each input flow of a computation should be read at a loop level whose associated

key-tuple is identical to that of the flow's index (and on this account the totally nested loop for a computation must contain a loop corresponding to the index afterch input flow). It cannot be read a higher level because at such a level the key information is incomplete. To read it at a lower level would be inefficient, because it would cause unnecessary re-reads of the flow's records.

Outputs: Similarly, each output flow of a computation must be written at a loop level whose associated key-tuple is identical to that of the flow's index. It cannot be written at a higher level because of insufficient key information, and to output it at a lower level would cause multiple writes of the records.

Calculations: A flow expression should also be calculated at a loop level whose associated key-tuple is identical to that of the flow expression's index. Again, the key information at a higher level would be insufficient to calculate the expression, and to perform it at a lower level would be redundant. Further economy can be realized, however, in a mixed-index flow expression if it contains a sub-expression whose associated index is a sub-index of the flow expression as a whole; such a sub-expression should be split off and calculated at its appropriate (higher) level.

II.3.2.2 Position of I/O and Calculations Within Their Assigned Levels

The placement of a read, write or calculation within a given loop level (i.e. in either the Prolog, Epilog or General section) should be done with a view toward imposing the minimum constraint on implementation. If done in this manner placement preserves the maximal flexibility in subsequent aggregation. For instance, if a calculation could go into either the Prolog or the Epilog it should be placed in the General section. If instead it were arbitrarily placed in the Epilog this unnecessary constraint would preclude subsequent aggregations that would require it to be in the Prolog (loop merging in computation aggregation is discussed below).

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Entering the continue and contemplative of the property of the property of the contemplative of the content of the content.

no abCalculation. A Terreportion of I/O and Calculation is suggested to surge of the surge of th

Spoil year to see soft at tail, mee at any at analyting seath to same passed one as A placement of a read, write or calculation within a given loop level (i.e. in either the protog, training of benefield the analytic stept of the protog of benefield section) though be done with a view toward imposing the maximum conditions and in the contract of the protog of the maximal flexibility in subsequent aggregation. For instance, if a calculation could go into either the Protog or the Epi log it should be placed in the General section. If much go into either the Protog or the Epi log it should be placed in the General section. If much go into either the Protog or the Epi log it should be placed in the General section. If much go into either the Protog or the Epi log it should be placed in the General section. If much constitution appreciate the subsequent top sibrary subsequently pideology that the Frotog (loop merging in computation appreciation is discussed belong VAO with reduction appreciation is discussed belong the reduction of the protog of the reduction appreciation appreciation is discussed belong the reduction appreciation of the protographic the protog of the protographic transfer and transfer and transfer and transfer and transfer and transfer and transf

PAY IS RATE * HOURS IF RATE PRESENT AND HOURS PRESENT

Here, both inputs have the same index (employee-id) so there is only one loop;

Level: (employee-id)
Inputsp: empty
Prolog: empty
Outputspempty

Inputs_G: {HOURS, RATE} General:calculate PAY Outputs_G:{PAY}

Inputs: empty
Epilog: empty
Outputs:empty

As explained above, everything is placed in the general sections.

Now consider a simple reduction flow equation:

ITEMBEMAND IS THE SUM OF DEMAND FOR EACH ITEM-ID

We have seen that the implementation of such a flow equation will always have two loop levels:

Loop I (outer loop)

Level: (item-id)

Inputsp: empty

Prolog: initialize sum

Outputspempty

Inputs_G: empty General compty Outputs_Gempty

Inputs_E: empty
Epilog: empty
Outputs_E:(ITEMDEMAND)

Loop 2 (inner toop)

Lovel: liten-id, store-idl

Level: liten-id, store-idl

Prolog: mpty

Level: liten-id, store-idl

Prolog: mpty

Level: liten-id, store-idl

Level: li

Toputso: BERES, SATES
General scatculate PAY
Outputso: BPAY
Utqua spolicy
Gutputso: PAY
Utqua spolicy
Utqua spolicy

inpute_i: **em**piy Epi**log:** - cepty

The input DENMID has the keys item-id and store-id in its indestable of its file read in the (item-id, store-id) level loop (the inner and otherwise) and inthe periodical distribution of periodical distributions and its index described and its in

A mixed-index matching computation like: Utans :qe tuqui

Project initializa sum

EXTENDED PRICE IS COMMENTARIES * PRICE IF COMMENTARIES PRESENT

must have two loop levels when implemented, one for each identified of its imputs. Its uppersonation looks like:

insule_s, empty Epilogi empty Outpute<u>rditEMDESAADI</u>

Loop I (outer loop)

Level: (item-id)

Inputsp: IPRICE empty

Prolog:

Outputspempty

Inputs_G: empty General: empty Outputsgempty

Inputs_E: empty

Epilog:

OutputsEempty

Loop 2 (inner loop)

Level: (item-id, store-id)

Inputsp: empty

Prolog: empty

Outputspempty

Inputs: (CURRENTORDER)

General:calculate EXTENDEDPRICE

Outputs_G: [EXTENDEDPRICE].

Inputs_E: empty

Epilog:

OutputsEempty

Part III: Computation Agreement and Long Marine (good retter) I good

As explained above the aggregation of two or many distributed with a single years "polor" to process of composition of the process of the process of the process of the process of composition of the process of the pro

When two computations are found to be cardidates for applicable that their suitability for aggregation must be tested, and then, if they are aggregatable, their supuritive below a good rearry 2 doo.

must be merged to form a single totally nated tony allowable their below 1 bel

III.I Loop Aggregatebility

Intenting: ICLARENTOFICERI
General:calculate EXTENSECORICE

A listle thought will show that when two passed lightlife and the section (read, write or calculation) in the aggregate must be performed at the securibility lightlife before aggregation; uf gate 100 i i q. 100 i q. 100

Furthermore, there are certain enduting containing that the article of the individual hope satisfy and which must be satisfied by the appropriate larges that entails gradient before it can be used; a Protog action must occur before its associated hour large, and an Epit log action must occur after its inner large.

If two computations have level compatible loops and if the ordering constraints of the two loops can be mutually satisfied in a single totally nested loop, aggregation is possible.

III.1.1 Level Compatibility Between Loops

It is easy to show that two loops are level compatible if and only if their level structures are identical or empty levels (levels at which no actions are performed) can be inserted to make their level structures identical. Some examples of level compatible totally nested loops (TNL's) and the level structures of their aggregated results are: 16

loop	levels	levels in aggregate
TNL ₁	(K), (K,L)	(K), (K,L)
TNL2	(K,L)	
TNL	(K,L)	(K,L), (K,L,M)
TNL2	(K,L,M)	
TNL	(K), (K,L)	(K), (K,L), (K,L,M)
TNL2	(K,L), (K,L,M)	

It is interesting to note that when aggregation occurs loop levels are meither added nor deleted; that is, the set of loop levels in the aggregate is simply the union of the sets of loop levels in the component computations.

Some examples of loops whose level structures are incompatible are:

<u>loop</u>	levels
TNL,	(K)
TNL2	(L)

¹⁶ In this section the symbols K, L and II denote different keys.

TNL₁ (K), (K,L) TNL₂ (L), (K,L) TNL₁ (K), (K,L), (K,L,M)

TNL₂ (K), (K,M), (K,L,M)

HLL2 Order Constraint Compatibility Between Loops

Consider the computations for the following two flow equations:

I TEMBERAND IS THE SUN OF DENAND FOR EACH TYEN-ID

FRACTION IS DEMAND/ITENDEMAND IF DEMAND PRESENT

It would seem immanently reasonable to aggregate these two computations since they have a common input (DEMAND) and the output of the first is an input to the second. Yet they cannot be aggregated into a totally nested loop! Their implementation descriptions reveal why. Recall that the description of the first is:

HE TO A COMPANY OF COURT OF STATE

and the second of the second of the

Loop I (outer loop)

Level: (item-id)

· Inputso: empty

an a cope out of

Prolog: initialize sum

Outputs-empty

Inputs_G: empty General: empty Outputstantu

Inputse: empty

Epilog: empty

Outputse::ITEMENMO

Loop 2 (inner loop)

Level: (item-id, store-id)
Inputsp:empty
Prolog: empty
Outputspempty

Inputs_G: (DEMAND)
General:calculate sum
Outputs_Gempty

Inputs: empty
Epilog: empty
Outputs: empty

The FRACTION computation also has two nested loops:

Loop i (outer loop)

Level: (item-id)

Inputsp: (DEMAND)
Prolog: empty
Outputspempty

Inputs_G: empty General: empty Outputs_Gempty

Inputs_E: empty
Epilog: empty
Outputs_F: empty

Loop 2 (inner loop)

Level: (item-id, store-id)
Inputsp: empty
Prolog: empty
Gutputspempty

Inputs_G: IDEMANDI General: do division Outputs_G:IFRACTIONI

Inputse: empty
Epilog: empty
Outputsempty

Clearly these computations are level compatible since they have identical level structures. But the

(and reint) S good Level: item-id, store-id (item-id) level loop of the first requires that I TEMESUME be an or (item-id) level hop of the second requires that it he an input in the White "Flate aggregate would :pelong utons thus require records of I TENCETMID before they are congre

The basis for all ordering countraints is the simple distribution for just be produced or note at a large status as 15 to 15 t read before it is used. Totally nested hop implementations are willied with a way that this rule is observed exactly. That is, things are in a loop's Prolon if said all it is ipol (q3 emp ty the enclosed loop(s); things are in a Epi log If and only If the Bullianud after the enclosed loop. Listed explicitly, the constraint with hitse and the missing will have a party of the constraint with the const Loop I (outer loop) two totally nested loops are:

tevelt (item-id)

-- an output of an Epi log cannot be an input to a Profitation (192) ugn) Prologs u laste

Output spensity - every Prolog action must remain in the Prolog

utame sactuant - every Epi log action must remain in the Epi log Ceneral: mapty

Untputsonmoty - Prolog I/O must remain in the Prolog

utone tachion! -- Epi log I/O ment remain in the Epi log :pelin3 utane Outputscempty implicit are the constraints that

Loop 2 (inner loop) was all of subsect that lending at each boven ad tennes soits as -- Level: Tites-Id, Ators-Id)

- I/O cannot be moved from its original level to a Prologi u) que

10 can be moved The only thing that one change is that actions and their from the General section to either the Prolog or Epilog of Military Livel. Such a n Denoralide division merely reflects the addition of a constraint that does not all the Thus, such a move may be made when necessary to me :polia3 ut des to be merged, but should never be done arbitrarily, so as to fill the best states Clearly these computations are level compatible since they have identical level structure adiapolitic Computations whose totally nested loops are level compatible and satisfy the above order constraints are aggregatable.

111.2 Merging Loops

Because each action and all I/O must be performed at the same level in the aggregate as it was before aggregation, the loop structure of the aggregation of two computations can be obtained through a level-by-level merge of the loop levels of the two computations to be aggregated.

The algorithm for merging two totally nested libops is:

For each loop in one:

If the other has no loop at the the same level, just add the representation of that level to the description of the aggregate.

If there is a corresponding loop, the two loops must be merged into one for the aggregate. The full details of merging loops are complicated, but a rough sketch follows. Let the corresponding loops be L_1 and L_2 , where no output of L_2 is an input to L_1 . There are three cases:

- 1. Some output F of the Epilog of L₁ is an input to L₂.
 - a. F is an input to L2's Prolog section: aggregation impossible.
 - b. F is used by an action in L₂'s General section: move that action to the Epilog of the the corresponding level in the aggregate, along with any actions in L₂'s General section which use, as input, some output produced by the action; all other actions remain in the same sections in the aggregate action with any L₂.

What has been seeded the company

c. All other cases; all other actions remain in the same sections in the aggregate as they were in L_1 and L_2 .

¹⁷ Obviously, the case where no output of L_1 is an input to l_2 will be handled exactly the same, mutatis mutandis. The remain case, where each has some output that is an input to the other, is impossible.

- 2. Some output F, generated by some action A in the General section of L₁, is an input to L₂.
 - a. F is an input to L_2 's Prolog section: move A from the General section to the Prolog section of the aggregate, along with any actions in the General section which have, as output, something used as input to that computation; all other actions remain in the same sections in the aggregate as they were in L_1 and L_2 .
 - b. All other cases: all actions remain in the same sections in the aggregate as they were in L_1 and L_2 .
- 3. Neither 1 nor 2: all actions remain in the same sections in the aggregate as they were in L_1 and L_2 .

Basically, what this means is that a General vaction must move to the Prolog of the aggregate if it must come before some action in that Prolog or if it must come before another General action which must be moved to the Prolog; a General action must move to the Epilog if it must come after some action in the Epilog or if it must come after another General action which must be moved to the Epilog.

111.3 Non-Totally Nested Loops

In this report the treatment of data driven loop implementations is restricted to loop structures that are totally nested. Totally nested implementations are not only broadly applicable, but generally simple and efficient as well. In fact they often provide the most efficient and expeditious implementations, especially when sequentially organized files, sorted by key values, are used. For the sake of completeness, though, something should be said here about non-totally-nested loops. Indeed, a great deal could be said about such implementations enough, certainly, to make one or more separate reports. Because of this the discussion here is necessarily brief and incomplete.

Most importantly, it should be said that non-totally nested loop structures are by no means

perhaps most interesting when two or more computations cannot be performed entirely concurrently (i.e. in the same loop), but they can be performed with partial concurrency. The following two examples illustrate.

III.3.1 Example 1: Aggregating Computations with Incompatible Order Constraints

Recall the flow equations:

ITEMDEMAND IS THE SUM OF DEMAND FOR EACH ITEM-ID

FRACTION IS DEMAND/ITEMDEMAND IF DEMAND PRESENT AND LIEMDEMAND PRESENT

and their implementing computations. We saw in Section III.1.2 that the implementing computations for these flow equations could not be merged into a totally nested loop structure because the inner loop for the first had to be completed before the inner loop of the second could be performed. They can, however, be aggregated into a single loop with a structure like:

for each (item-id) from DEMAND

sum = undefined

for each (store-id) from DEMAND(item-id) <calculate sum>

if defined (sum) then ITEMDEMAND (item-id) = sum

for each (store-id) from DEMAND(item-id) <calculate FRACTION> end

end

This is a non-totally nested loop structure, since two loops (the inner ones) appear at the same level.

It is interesting to compare this aggregate implementation with the unaggregated implementation of the two computations involved (as separate loops in separate job steps). On the one hand, in either implementation every record of the DEMND flow must be accessed twice, so no accesses are eliminated by aggregation. On the other hand, accesses of the records of the ITEMDEMAND flow are eliminated by aggregation. If the computations are implemented separately, every record of ITEMDEMAND must be written into a file by the first computation and then read back by the second; whereas in the aggregate implementation the records are used as they are generated, so no re-reading is necessary. ¹⁸

In general we have seen that when two implementations are level-compatible, the only case in which their aggregate cannot be implemented as a totally nested loop is where, for some loop level, the output of the Epi-log section of one is an input to the Prolog section of the other (as is the case with 1 TEMBERAND above). In such a case the corresponding loop level of the aggregate can be implemented (as above) as two loops of the same level performed in sequence, and re-reads of the flow in question will be saved.

III.3.2 Example 2: Aggregating Computations That Are Not Level-Compatible

In Section III.I.I we saw that computations with the following fevel structures were not level compatible with one another:

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TNL₁ (K), (K,L), (K,L,M) TNL₂ (K), (K,M), (K,L,M)

The fact that they are not level-compatible means that it is impossible to devise a total

¹⁸ In fact, if these records are not used by any other computation in the data processing system, it is not necessary to write them out into a file either.

nesting of loops that will implement their aggregate. They might, however, be said to be partially level-compatible, since the outermost levels have identical keys. If a common driver set can be found for that level, they might be implemented as a non-totally-nested loop structure. The following is a possible implementation skeleton:

```
for each (K) from D_0 for each (L) from D_1 for each (M) from D_2 end end for each (M) from D_3 for each (L) from D_4 end end
```

end

where the D_i are distinct drivers.

This is another commonly found construct in file data processing. It is the case where, for a common set of values for the sub-index (K), two or more independent computations are to be performed. As in the previous example, there is some I/O saving (over separate implementations of the computations involved) because each record of D₀ has to be read only once.

negring of loops that will implementate an entering the said to be said to be soundly of the soundly said to be soundly

We have also seen that, in general, computations and that "All all the hape mested by nested loop structures. That is, an implementation torontons the Whitehall all the body to see of about the mast have a driving flow set.

In Part I we saw that for a computation as a whole assess implaining the paper of the elective enumeration of the critical index sets of each of its impats. This constraint obviously extends to the individual loop levels. Additionally, the table is disable in the part of a level count be effectively enumerated so that all records will be unition. Granting these quickenists in terms of drivers we have

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where the 0 are distinct deixection made and a getterordigal volumes qual forteen with all acres on the country found construct in the data processing. It is the case where, for a

common set of values for the sub-index IK), two or more independent computations are to be

performed. As in the previous example, there is some 1/0 saving (over separate implementations

In order to discuss the determination of loop level delants we take that develop a practice theory of index sets and critical index sets.

IV.1 A Theory of Index Sets and Critical Index Sets for Data Driven Loops

Let us begin with some definitions and useful consequences of these definitions.

IV.1.1 Definitions and Useful Lemmas

We redefine the notions of a flow's index set and critical index set formally and introduce the operators Proj. Inj and Restr:

Definition: The index set of a flow F with index I is defined as

$$IS(F) = \{1 \mid \text{there is a record in } F \text{ for } I\}$$

Definition: The critical index set of a flow F (with index I) with respect to a flow X is defined as

<u>Definition</u>: The projection of an index set S with index $(k_1, ..., k_m, k_{m+1}, ..., k_n)$ onto the sub-index $(k_1, ..., k_m)$ is defined as

Proj(S,
$$(k_1, ..., k_m)$$
) = { $(k_1, ..., k_m)$ } $\exists (k_{m+1}, ..., k_n)$ such that $(k_1, ..., k_m, k_{m+1}, ..., k_n) \in S$ }

<u>Definition</u>: The injection of an index set S with index $\{k_1, ..., k_m\}$ by the index set T with super-index $\{k_1, ..., k_m, k_{m+1}, ..., k_n\}$ is defined as

Inj(S,T)=
$$\{(k_1,...,k_m, k_{m+1},...,k_n) \mid (k_1,...,k_m) \in S \land \{k_1,...,k_m, k_{m+1},...,k_n\} \in T\}$$

<u>Definition</u>: The restriction of an index set S with index $(k_1, ..., k_n)$ by the condition C (whose truth depends on the values of the keys $k_1, ..., k_n$) is defined as

Restr (S,C) =
$$\{(k_1,...,k_n) \in S \mid C \text{ is true}\}$$

From the last three definitions the following simple but useful results (stated without proof) can be obtained:

Lemma 1: If A is an index set with index I, then

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IV.1 & Theory of index Sets and Critical Index Sets for Data Disease Low- 11. Alford Lemma 2. If damid there industries up all inhunberess their brownist. West 18 J. Inj (A,B) - B a inj (A,B) IV II Definitions and Useful Lemmas In particular, if A and B are index sets with the same index, then We redefine the notions of a flow's index set and critical index set formally and introduce the Inj(A.8) - B a / operators Proj. Inj and Restri-Definition: The index set of a flow F with index I is defined as Inj(S,T) c T IS(F) = {| | | there is a record in F for | | Lemma 4: If T is an index set with index Iz and S is an index set with index Iz a sub-index Definition: The critical index set of a flow F (with index I) with respect to a flow X is defined as . of In then CISx(F) = [1] there is a record in F for 1 Proj (Inj (SNN), between Symposium and pressoon at last decumes to K,S is an impressed with the bid in the company of the bid a significant index iki..., kal is defined as of le then Proj(S. (ki. . . ka)) -Restr(S, F PRESENT) - Inj(IS#1.S) (kg. . . ka) I Bismer such that Isp kas tons . . . kal c S) Definition The injection of an index set 5 with the the Control of We begin with two theorems concerning the artifall haben sets of flows involved that computations. The results are expressed in terms of the index sets of the inputs and disjutes. Theorem 1: If F is a flow defined in testas of the flower F. . If F, by a non-reduction flow Definition. The restriction of an index set S without a said said and the constituents. cis, (F.) - Projits Flathend is defined at less the keys kin de three ballion in a charge but it That is, an input record is needed in the collectation of a flow of it and thely it is contracted to the index or sub-index subjects to serve served of \$1.5 bit differ this quantity forms

Lemma I we have that

Lemma It, if A is an index set with index I, then

can be obtained

Corollary 1: Let F be defined as in Theorem I. Then for any flow F, with index identical to that of F

$$CIS_F(F_i) = IS(F)$$

Theorem 2: If R is a flow (with index I_R) described by the application of a reduction operator to a flow expression expr in terms of the flows F_1, \dots, F_m where each flow F_i has index I_i , (e.g. the flow equation for R is: R IS SUM OF expr FOR EACH $\langle I_R \rangle$), then

$$CIS_p(F_i) = Proj(IS(expr), I_i)$$

(Note that the index of expr must be a super-index of In)

This theorem simply says that when a flow (as that described by expr) is reduced every record of that flow is used in calculating the result. From Theorem I we have in turn that the critical index set of each F_i with respect to the flow to be reduced is given by the expression on the right-hand side of the above equation.

Corollary 2: If R is a flow (with index I_R) described by the application of a reduction operator to a flow F (e.g. R IS SUM OF F FOR EACH $< I_R >$), then

The following theorems concern the nature of the index sets of flow expressions. First, a simple result about flows described by reduction:

Theorem 3: If R is a flow (with index I_R) described by the application of a reduction operator to a flow expression expr (e.g. the flow equation for R is: R IS SUI OF expr FOR EACH $< I_R >$), then

$$IS(R) = Proj(IS(expr), I_p)$$

This theorem says that the provide an amount in about the state of the life of the life has at least one corresponding record.

(1) = (3) (3) (3) (3) (4)

For flows described by non-reduction flow expressions a more entensive treatment is appropriately and the state of the described of the flow of the fl

to the description of the description of the state of the

The following unequipment one in the supplemental of the following unique result about flows described by reduction:

Theorem 3: If R is a flow (with index la) described by his application of Jean Family and the start of the flow equation for R is R is Sun OF start Family to the flow expression order (e.g. the flow equation for R is R is Sun OF start Family to the

Corollary 9: Let safe F_1 , ..., F_n) be a flow expression defining at in Theorem 4 with the additional constraint that the F_i are of uniform index. Thus

$$IS(safe(F_1,...,F_n)) = \sup_{n \in \mathbb{N}} \prod_{i \in \mathbb{N}} IS(F_i) f(n) = \sup_{n \in \mathbb{N}} \prod_{i \in \mathbb{N}} IS(F_i) = \lim_{n \in \mathbb{N}} \prod_{i \in \mathbb{N}} IS(F_i) = \lim_{n \in \mathbb{N}} \prod_{i \in \mathbb{N}} IS(F_i) = \lim_{n \in \mathbb$$

As mentioned above the only legal arithmetic flow expression in FE-HIBOL is a safe or a safe further qualified by some condition. This further qualification must take the form of a logical expression ANDed with the safe. Thus, to complete our treatment of arithmetic flow expression we only need the following simple theorem:

Theorem 5: The index set of a simple arithmetic flow expression safe qualified by the condition C is given by

Consideration of special cases leads to three simple corollaries:

Corollary 4: By Lemmas 2 and 5

Corollary 5:

Corollary 6:

IS(safe AND (
$$C_1$$
 OR C_2)) = Restr(IS(safe), C_1) U Restr(IS(safe), C_2)

For conditional expressions with two cases 19 we have the following result:

Theorem 6: Let E be a conditional flow expression of two terms:

$$E = expr_1 \text{ If } C_1$$

$$ELSE expr_2 \text{ If } C_2$$

¹⁹ The extension of this theorem to more than two cases is trivial.

where expr $_1$ and expr $_2$ are legal PE48100C flow expressions and C_1 and C_2 are logical expressions. Define the flow-explication $(I_1, I_2, \dots, I_d) = 160 |C_d|$ expressions.

As mentioned above the only legal arithmetic flow expectation of PEHIBOL is a sale or a sale further qualified by some condition. This defined definition must take the form of a logical expression ANDec with the sale. Thus, to complete our designant of arithmetic flow expression we must need the following simple theorem:

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Theorem is The index set of a simple arithmetic flow expression us is quainfied be the

condition Cas given by

Consideration of special cases leads to three simple corollaries: 18 FF FOR FACE A 1 signer 3

Corollary 4: By Lemmas 2 and 5
where R has index (k₁) and F has index (k₁, k₂). As we have not above the typical
15 (safe AM) G PRESENT) = Inj(G, 15 (safe))

- 15(saint it la) (C, 15(saint)

Corollary 5:

for each (kg) from F

(5) saie AND (C, AND Ca) = Restr((Steste), C,) Thestr((Steste), Ca)

for each they from Fitty)

Corollary 6:

15(sate AND (C) OR C211 - Restriblestel, C, Pt 1867 (Steafe), C21

For conditional expressions with two cases 19 we have the following result:

Theorem is Let E be a conditional flow expression of two terms tamelbonisch li

ELSE expr. IF.C. tubb estru

¹⁹ The extension of this theorem to more than two cases is trivial.

In level I we have the output R and the driver F. The index set D₁ enumerated by this driver at this level is²⁰

$$D_1 = Proj(IS(F), (k_1)) = IS(R)$$
 (by Theorem 3)

thus satisfying the driving constraint for the input R.

In level 2 we have the input F and the driver F. The index set D_2 enumerated by this driver at this level is

$$D_2 = IS(F) = CISp(F)$$

(by Corollary 2)

thus satisfying the driving constraint for the output F.

Example 2:

PAY IS HOURS * 3.00

IF HOURS PRESENT AND NOT HOURS > 48

ELSE 120 + (HOURS - 40) * 4.5 IF HOURS PRESENT

We shall use this example to illustrate Theorem 6. Define Exand Example to

E1 = HOURS * 3.00 IF HOURS PRESENT AND NOT HOURS > 48

and

E₂ = 120 + (HOURS - 48) * 4.5 IF HOURS PRESENT AND NOT (HOURS PRESENT AND NOT HOURS > 48)

By pure logical simplification the last equation can be rewritten:

From Theorem 6 we have that

Theorem 8 of the next section provides a formal treatment of enumerated index sets.

in level i we have the output R and the driver F. The inteat a trada red WRRL driver at

- Restr (ISORUES), NOT MINES > 400 (by Theorem 5) (5% a) (5 vol siri)
U Restr (ISORUES), NOMB > 401 (by Theorem 5)

O: - Projils (Fi, M. 1) . is (R) (by Theorem 3)

- Restr (ISAU)(IS) , NOT 10005 > 40 08 10005 > 40)

thus satisfying the distinct of the input R.

- Restr (ISOCHAS), T)

In level 2 we have the input F and the driver F. The index set Us enumerated by this driver ...

at this level is

and by Corollary !

02 = 15(F) = C15g(F) (by Corollary 2)

CISPAN MOURS) - ISMAN) - ISMANS)

thus satisfying the driving constraint for the output F.

Example 3:

Example 2

bus

EP IS P + C IF P PRESENT MB C PRESENT

PAY IS HOURS . 3.00 IF HOURS PRESENT AND

where EP and D have the individe that id, atom-igh and P has the index (i ton-id). (This is

our familiar EXTENDERMONEY aquentual with extensional ville subject to the connectioner

We shall use this example to illustrate Theorem 6. Define Exhalling 3 box 9.43 ye bostiveredes

E1 - HOURS # 3.88 IF HOURS PRESENT AND NOT HOURS - 48 Just swed sW

CISTO - ISON THERE - CHUCH (I) COMMING - SHUCH) + BSI - 57

- Idjesson (deta) (di en Terre d

AND NOT HOURS > 48)

CISHP) - Proj(ISEP), (item-id)

By pure logical simple calculations continued become logical simple calculation?

- ISP) a ProjilBED, francial ... Surface 4.

EZ . 120 + BELLES - NOI . 1.5 IF HOURS PRESENT AND

As we have seen above, the base of the base being a few boats buy, with both loop.

From Theorem 6 we have that

levels driven by C:

²⁰ Theorem 8 of the next section provides a formal treatment of enumerated index sets.

```
for each (item-id) from C

get P(item-id)

for each (store-id) from C(item-id)

get C(item-id, store-id)

EP(item-id, store-id) = ...

if defined(EP(item-id, store-id))

then write EP(item-id, store-id)

end
```

In level I the input is P and the driver is C. The index set D_j enumerated by this driver at

```
D_1 = Proj(IS(C), (item-id))

\geq IS(P) = Proj(IS(C), (item-id)) = CIS(P(P))
```

In level 2 the input is C, the output is EP and the driver is C. The index set D_2 enumerated by this driver at this level is

```
D<sub>2</sub> = IS(C)

2 Inj(IS(P), IS(C)) (by Lemma 3) (15 in the charge and a gradual state a
```

Thus we see that the flow C is (at least) adequate to drive both levels.

IV.1.4 Driving Flow Set Sufficiency

end

this level is

We wish to be able to determine whether a set of input flows is sufficient to drive a computation loop level. Let us begin by defining the notion of the necessary index set for a computation level:

<u>Definition</u>: The necessary index set at level i for a computation C (denoted NIS_i(C)) is defined as the set of index values necessary to drive level i of the totally nested loop implementing C.

By the fundamental driving constraint we have

for each (item-id) from C

Theorem 7: The necessary index set for level i of a computation belong to 1 se

EPlites-id, store-id) = ...

whereO(C)= outputs of computation C

if defined EP litem-id, store-ing i book to sugare - i

then units EP(litem-id, store-id) from to study

Now a loop level can be driven by inputs only at the same or lawer levels (those at higher bers do not have enough keys in their indices). Obviously the index sat enumerated by a driving

In level I the input is P and the driver is C. The under set It committeed by this driver at a tempt griving a yellow to be because its artist and it is forth that the state of the level is

lower level is given by the following theorem:

0; = Proj(18(6), (jten-id))

Theorem & The index set S. ([A comparated to a long best settle dester I by an input F read

In level 2 the input is C, the output is EP and the driver is C. The index set Us enumerated

S_r(1) = Proj(IS(F),1)

by this driver at this level is

 $0_5 = 15(0)$

Using the terminology just introduced we have smens Jyd)

2 inj(15121,1916))

Theorem 9: A set 8 of flows is sufficient to drive level i (mile index 1) if and only if

Thus we see that the flow C is (at less) adequate to drive both levels.

MIS,IC) c U S_{F,}(I)

IV.1.4 Driving Flow Set Suffictency

that is, if and only if the index set commented by a set in the property of the authorise in drive a set of input its sufficient to drive a

computation loop level. Let us begin by defining the notion of the necessary index set for a

computation level

There is some redundancy in this expression. The critical index set of any laped in inputer with health to \$200 \text{last} \t

IV.1.5 Minimal Driving Flow Sets

The set of all inputs of a computation is sufficient to drive that computation. We are interested in finding the smallest subsets of this set that will provide sufficient drivers for each level. This interest stems from our implementation constraint that all drivers must be read sequentially and must have compatible sort orders. If all contained inputs were used to drive each level of a computation loop, all inputs to that computation would have to have compatible sort orders and all would have to be read sequentially, a constraint that is often unnecessarily severe.

Moreover, from an efficiency point of view, we generally want the set of indices enumerated by the drivers at any level to be as small as possible (while satisfying the fundamental driving constraints) so as to minimize the number of iterations. For example, if we are trying to minimize I/O accesses and we have a loop that reads some (non-driving) flow by random access, the fewer iterations there are the fewer attempts there will be to access records from that flow.

Consider, for example, the EP computation (Example 3 above). The inputs contained in the outer loop are P and C. Both together could have been used as a driving flow set for that level. We were able to show, however, that C alone was sufficient to drive the outer loop. Thus, we came up with an implementation in which only the flow C had to be sorted and read sequentially. Additionally, in this implementation only those records of P that can actually be used are fetched.

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It is important to note that the using some smallest driving flow set for each level does not always improve efficiency. In the computation above it can be shown that P alone is sufficient to drive the outer loop. However, such an implementation would be no better than one in which the outer loop is driven by both inputs. Since the inner loop must be driven by C in any case, we would still end up using both inputs as drivers; both would have to be sorted compatibly and read sequentially; and more records of P would be read than would actually be used.

IV 15 Minimal Diving Flow Sell and an are rewind to reduce off selection of the Sell bearing and the sell of all inputs, of a selection of the selection of the

by the drivers at any level to be as small as possible (while satisfying the fundamental driving moistraints) so as to minimize the number of iterations. For example, if we are trying to minimize

rejection to see and severe time are the privite legal a si to well a toth work of the fewer access, the fewer seeds to the see of severe the seeds making for the fewer seeds to the fewer seeds the see of severe the fewer seeds are the fewer attempts there will be to access records from that flow.

to harding found of the EP computation (Example 3 above). The inputs contained in the outer loop are P and C. Both together could have been used as a driving flow set for that level.

Address, first to the state of the state of

and reported distributed by satisficial as allow existing the boundarings of used are teletical.

The trimportant to note that the using same smallest driving flow set for each level does not a nitriportant to note that the trimportant of the computation above it can be shown that P alone is sufficient to drive the outer loop. However, such as implementation would be no better than one in without the

Policy completes that represent with the noting of the policy control of the policy cont

Insofar as set inclusion is provable. It can be shown that the provide providing of provide subject inclusion is not solvablebused of classical actually be used there are noticed actually be used devotes ton as not solvable of the control of the

A ⊃ B ↔ B_{char} → A_{char}

The expression on the right of the equivalence symbol (44) is a formula in the first order predicate calculus. If this formula can be shown to be a tautology the corresponding set inclusion is proved. Showing that a formula is a tautology is equivalent to showing that it simplifies to T. Since powerful first order predicate calculus simplifiers exist, the task of proving set inclusion can be solved by recasting the hypothesis as a predicate calculus formula and trying to simplify it. If it can be simplified to T inclusion is proved; if it simplifies to F inclusion is disproved.

When the formula cannot be simplified to either T or F, the meaning of the result is not clear. Either the simplification is correct (in which case the formula is not a tautology, and thus set inclusion does not hold) or the simplifier has run up against a fundamental limitation²⁴ and has failed to simplify the formula completely. In the latter case the formula may in fact be equivalent to T (implying set inclusion), but the simplifier is unable to determine it. Because of this ambiguity, the wisest assumption is the conservative one: whenever simplification to T does not occur, set inclusion does not hold.

IV.2.1 Characteristic Functions for Index Sets

In this section the particulars of the syntax²⁵ and semantics of characteristic functions for index sets are presented.

The characteristic function for an index set is a logical expression (predicate) in terms of its the keys of its index that is true for an assignment of values to those keys in exactly those cases in

Because our work is implemented in the LISP programming language the notation is unabashedly LISPish.

²⁴ It is a well-known fact that it is impossible to devise a procedure that will correctly simplify every formula in the first order predicate calculus.

which the index set contains a corresponding index value. That is, if $S_{class}(k_1, ..., k_n)$ denotes the characteristic function for the index set Sthem

 $S_{closs}(k_1, \ldots, k_n) = 1$ iff S contains an index value with $k_1 = k_1, \ldots, k_n = k_n$

The logical operators from which characteristic functions are formed are:

I. Standard logical operators²⁶

- a. AND (AND p_1, \ldots, p_n) = T for a particular key-tuple instance iff all of the p_i are true for that instance
- b. OR $(OR p_1, ..., p_n) = T$ for a particular key-tuple instance iff any of the p_i are true for that instance
- c. NOT (NOT p) = T for a particular key-tuple instance iff p is false for that instance
- d. FOR-SOITE (k_1, \ldots, k_n) $p(k_1, \ldots, k_m, k_{m+1}, \ldots, k_n)$) = T for a particular key-tuple instance $\{k_{m+1}, \ldots, k_n\}$ iff there exist values for the keys k_1, \ldots, k_m such that the predicate $p(k_1, \ldots, k_n)$ is true; this is existential quantification.
- 2. Standard arithmetic comparison operators (their arguments must be arithmetic expressions in terms of variables (see bolow) and constants formed using the arithmetic operators +, -, * and /)
 - a. EQUAL (EQUAL expr₁ expr₂) = 1 iff expr₁ and expr₂ have the same numerical value
- b. GREATERP (GREATERP expr₁ expr₂) = T iff the numerical value of expr₁ is greater than that of expr₂
- 3. The special operator DEFINED; (DEFINED (V per $k_1, ..., k_n$) = 1 iff there is a record in the variable V in period per for the key-tuple instance $(k_1, ..., k_n)$. The argument to a DEFINED operator must be a variable.

The terms introduced here are explained in greater detail in the following sections.

²⁶ The symbols p and p_i denote predicates.

IV.2.1.1 Variables

A variable is a representation of a HIBOL flow with key and period information attached. The period uniquely identifies the variable in time (i.e. it specifies a particular "incarnation" of the flow). An assignment of values to a variable's index and its period specifies an instance of that variable and this instance is said to be defined if there is a datum (and thus record) corresponding to the key and period values named in the assignment.

The general form for a variable is

(flow-name period key, ... key,)

where flow-name is the name of the associated flow²⁷, the slot period contains the name of the period in which the variable is generated or input, and the slots key, contain the names of the keys of the variable. An example of a variable specification is

(ENROLLED term student subject-number)

where

ENROLLED is the name of the variable term is the name of a period student and subject-number are the names of the variable's keys

An occurrence of a variable in a predicate is called a variable reference. In a variable reference the form in the period slot identifies a particular incarnation of the variable (e.g. if the period slot contains TERM that means that this term's incarnation of the variable is being referred to; if it contains (PLUS TERM -1.), last term's incarnation is referred to).

²⁷ The variable and the flow have the same name.

IV.2.1.2 (DEFINED variable-reference)

This expression is true if and only if variable-reference is defined. In particular an expression like

(DEFINED (ENROLLED term student subject-number))

is true for an assignment of constant values to each of its keys and its period if and only if the variable ENROLLED in the specified period contains a record corresponding to the specified index value; otherwise it is false. Thus, for example, the predicate above is true for subject-number = 33 and term = TERM if and only if in this term's incarnation of EMPOLLED there is a record for the index value (JOE 33) (i.e. if and only if loe is enrolled in subject • 33 during the current term).

IV.2.1.3 Correspondence Between Logical and Set Theoretic Notations

In our characteristic function/index set duality the general correspondence between logical and set operators is given by:

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logical operator	set operator
AND COLOR BOOK OF	ေလည္းသို႔ ကြားေကာင္းက မိန္းႏိုင္း က်ားက (ကို က်
ne	
(FOR-SOME (km.), km) School	Proj (5, (k), : , k,))
(AND S _{char} U)	↔ Hestr(5,U)
(AND Schor Tchor)	injts, ii
(DEFINED (Y))	 IS(V) (2) (2) (2) (2) (2) (2) (2) (2) (2) (2)

That is:

the characteristic function of the intersection of two sets is the logical AND of their characteristic functions:

the characteristic function of the union of two sets is the logical OR of their characteristic functions:

the characteristic function of the projection Proj (S, I') of an index set S onto the sub-index I' is the FOR-SOME operator applied to the characteristic function of S and the remaining keys;

the characteristic function of the restriction Route (5, C) of an index set 5 by the condition C is the logical AND of the characteristic function of S and the condition C;

the characteristic function of the injection Inj (S, T) of an index set S by the index set T is the logical AND of their characteristic functions;

the characteristic function of the index set IS(V) of a variable V is the DEFINED operator applied to that variable.

This mapping can be used to determine the characteristic function of any set expression encountered above.

Examples:

The index set

15(P)

has the characteristic function

(DEFINED (P DAY item-id))

The index set

IS(P) n Proj(IS(C), (item-id))

has the characteristic function

(AND (DEFINED (P DAY item-id))

(FOR-SOME (store-id) (DEFINED (C DAY item-id store-id))))

The index set

Restr(IS(HOURS), NOT HOURS > 40)

has the characteristic function

(AND (DEFINED (HOURS HEEK employee-id))
(NOT (GREATERP (HOURS HEEK employee-id) 48)))

IV.2.2 Back-Substitution of Characteristic Functions

We would like our characteristic functions to contain as much information as possible so as to be able to determine as much as possible about the inclusion properties of index sets.

The only possible characteristic function for a variable (V per $k_1, ..., k_n$) that is a system input (i.e. a variable whose flow is not computed by the system; for example a supplier list) is the trivial one (DEFINED (V per $k_1, ..., k_n$), because all that can be said is that it contains a record iff it contains a record.

In some cases an input variable may have the special property that it will always contain a record for every allowable index value. (Knowledge of such a property cannot be deduced from the HIBOL specification of a data processing system; it must be supplied separately.) Such a variable is termed dense or full. An example might be the PRICE variable, which in every incarnation should have a record for every possible value of the index (i tem-id). In such a case the characteristic function of such a variable is simply T.

We could use the trivial characteristic function for a computed variable as well, but more (useful) information can be obtained through the application of Theorems 3-6 to the defining HIBOL flow equation. Likewise, we can use Theorems 1 and 2 to obtain useful characteristic functions for critical index sets. Characteristic functions thus obtained are called one-step characteristic functions.

It should be easy to see that for any characteristic function if an occurrence of (DEFINED variable) is replaced by the characteristic function for variable, the result will be a logically equivalent characteristic function. This is termed back-substitution of characteristic functions. If back-substitution is applied recursively, the result will be a characteristic function containing only

DEFINED's whose arguments are non-computed variables. This is called total back-substitution.

Total back-substitution of all characteristic functions has the advantage of making them: all into a uniform form, thus facilitating comparison and logical manipulation.

IV.2.3 Example

Consider the flow equations:

S IS H * R IF H PRESENT AND R PRESENT

X IS (H - 40) * R / 2 IF H PRESENT AND R PRESENT AND H > 40

P IS S + X IF S PRESENT AND X PRESENT

ELSE S IF S PRESENT

ELSE X IF X PRESENT

where the flows H and R are system inputs, all flow have the index (key) and all computations are performed daily. The one-step characteristic functions of the necessary input sets are:²⁸

NIS(S)_{cher} = (AND (DEFINED (H DAY key)) (DEFINED (R DAY key))

NIS(X)_{cher} = (AND (DEFINED (H_DAY key)) (DEFINED (R_DAY key)) (GREATERP (H_DAY key) 40))

NIS(P)_{cher} = (OR(DEFINED (S DAY key)) (DEFINED (X DAY key)))

From these we deduce (by Theorem 9) the following results

1. Computation S can be driven by either H or R, since both

²⁸ We use the outputs as the computation names and drop the level subscript since there is only one level.

2. Computation X can be driven by either H or R, since both

$$NIS(X)_{cher} \rightarrow (DEFINED (H DAY key))$$
 (2a)

and

$$NIS(X)_{cher} \rightarrow (DEFINED (R DAY key))$$
 (2.b)

are true

3. Computation P must be driven by both S and X, since neither

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nor

are true, but

is true

However, we know that

so back-substitution of characteristic functions yields

```
NIS(P) cher = (OR (DEFINED (S DAY key))
                                                                                                                                                                                                                                                        (DEFINED (X DAY key)))
                                                                                                                                                                                                                                                                                                                          (DEFINED (H DAY key))
                                                                                                                                                                                                                                                                                                                              (DEFINED AR DAY koul))
                                                                                                                                                                                                                                                                                                                          (DEFINED (H DAY key))
                                                                                                                                                                                                                                                       (AND
                                                                                                                                                                                                                                                                                                                           (DEEINED (R DAY key))
                                                                                                                                                                                                                                                                                                                             (GREATERP (H DAY key) 48)))
                                                                                                                                                                                                                                                                                                                                                                                                   · 我的我们是这个意識和做了一种的心思。 (1995年)
                                                                                                                                                                                                                                                                             (DEFINED (H DAY key))
                                                                                                                                                                                                                                                                             (DEFINED (R. DAY key)) ) and with the following the second second
                                                                                                                                                                                                                                                                                                                                                                                                                    The state of the s
Thus, formula (3.a)
```

```
becomes
   (AND (DEFINED (H DAY key)) (DEFINED (R DAY key)))
   (AND (DEFINED (H DAY key)) (DEFINED (R DAY key)))
```

which is obviously true. Thus, back-substitution has revealed that computation P can be driven by S alone.

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Each (aggregate) computation (jub step, program) in the dealing produced by ProtoSystem (s. (1994 YAC H) (3M1/3C) ((M1/AC)) =

Optimizing Designer is enough a loop distributed allocated belong to the loop at the to generate the (figs I YAC H) (EMITS). (St.)

records of its empor files). Implementation is the plantage of the appropriate specific (160) (yes! YAI) III 9637A3931

countrel and data structures encounty for this large and the NO tendent⁽²⁾. The main complications (400 Year) (300) (300) -

that arise in this process stom from the dutal litting, little of the little, as he implemented and the hybrid nature of files and loops resulting from aggregation. It is easies to engless deposits a series of examples, highway with this highlight half highly in the CHE forward case.

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which is obviously true. Thus, back-substitution has revealed that competation P can be driven by

In order to show the based manufactor of computation buildings but as begin by facility at the implementation of the most build single facilities the implementation.

S alone.

VIII Simple Computations

Consider the HIBOL flow equation:

PAY IS HERES . 3.00 IF HOME PRESENT

(recall that PAY and HUSES are files keyed on oursings id). Suggest that the design specifies that both files are to be stored on disk in sequential farmet.

The basic implementation of this computation is a PLA 00 MILE loop, whose body will:

read a record of the HELIES file

²⁹ We make a distinction between implementation and only generation, which it the problem of writing the actual code. Although we will show a good dool of decided we will not go into a detailed discussion of only generation here.

extract the data item (the number of hours worked)

multiply it by 3.00,

assemble the corresponding record of PAY

whose employee-id key is the same as the record read

whose data item's value is the result of multiplying the value of the data item of the record read by 3.00

write the newly created record to the file PAY

To support this iteration, there must be declarations of the data objects to be used

loop initialization

EOF (end-of-file) checking (to terminate the loop)

V.I.I.I Necessary Data Objects and Their Declaration

First there must be declarations for all input and output files. Assume that the files PAY and HOURS are known by these names to the PL/I environment (JCL code can be generated to make this happen). Then the following declarations must appear in the PL/I code:

DECLARE HOURS INPUT FILE SEQUENTIAL RECORD.

PAY OUTPUT FILE SEQUENTIAL RECORD:

There must also be declarations for data structures ancillary to the I/O and control to be performed. In particular, for every input file there must be a record image data structure into which a record of that input can be read. Likewise, for every output file there must be a record image data structure into which a record of that output can be built so that it can be written out. In our simple example, the HOURS and PAY files must have such associated data objects. The PL/I structure can be used for this purpose:

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DECLARE 1 PAY_RECORD.

- 2 EMPLOYEE FIXED DECIMAL (4).
- 2 PAY FIXED DECIMAL (4).

I HOURS RECORD.

- 2 EMPLOYEE FIXED DECIMAL (4)
- 2 HOURS FIXED DECIMAL (3):

Finally, for each input a flag is needed to indicate the EQF condition for that input. Thus, for the 殿中 医脱氧的现在分词 经人 mit of her but it in HOURS file we would have the declaration:

ং এক প্রকৃত্র হয় ১৮ জন্ম সংগ্রহণ করিব বিশ্ব DECLARE 1 EOF ALIGNED. 2 HOURS BIT (1) UNALIGNED INITIAL ('8'B):

When EOF occurs on the associated file this flag is set to '1'B

V.I.M. Loop Initialization

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Before iteration all flags must be initialized. This can be done by the use of the INITIAL statement in the declaration (as above for EOF. HOURS). Also all drivers must be read to establish initial values for their indices. In our example, the initialization section would consist of merely:

READ FILE (HOURS) INTO (HOURS RECORD); In the property of the

V.I.I.3 EOF Checking and Loop Termination

To detect an EOF condition on a file and set its corresponding flag the PL/I ON construct can be used. For the HOURS file the appropriate code would be: · 續 (a) [1] - 中國大量 知 (1) [2] - 中科 數

ON ENDFILE (HOURS) EOF.HOURS = '1'B;

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To enforce iteration termination upon EOF of the driver, the loop is constructed using the 三溴酚 医二甲磺胺磺胺 网络海绵蜂 form DO WHILE (- EOF.driver). assert the company of the state of the company of

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V.1.1.4 The Loop Itself

Given this supporting structure, the rest of the implementation is easy. The loop itself can be written simply as:

DO WHILE (- EOF.HOURS);

PAY_RECORD.PAY = HOURS_RECORD.HOURS * 3.0:

PAY_RECORD.EMPLOYEE = HOURS_RECORD.EMPLOYEE;

WRITE FILE (PAY) FROM (PAY_RECORD);

When the loop terminates, the job step is ended and the input and output files are automatically (1980) and 1980 of the complete PL/I program for the pay calculation computation is given in Fig. 1.

V.1.2 Uniform-Index Matching Computations ... PROPERTY OF THE PROPERTY OF THE

Let us extend our treatment of single-level loop implementations to these with more than one input. We use as our vehicle the variation of the pay calculation that includes a rate file findexed by employee-id):

PAY IS RATE * HOURS IF RATE PRESENT AND HOURS PRESENT

Suppose that the input files RATE and HOURS are to be read sequentially, that their records are sorted by employee-id and that HOURS is used as the loop driver.

Again because the loop is driven by a single input file, it is implemented using the form DO WHILE (- EOF, driver). However, the computation description dictates that a record of the output file PAY for a given value of the key employee-id is to be produced if and only if there is a record for that employee in HOURS and there is a corresponding record in the RATE file. Therefore, in the body of the loop, before the output record can be calculated, the record (if any) of the non-driving input that matches the current value of the driver's index must be found.

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To find the matching record of the non-driving input we read successive records from its file comparing the index value of each record with the current loop index. The general matching algorithm consists of the following loop:

For each non-driving input:

1. If FOUND, input is true (indicating that the record currently held in the input's image structure has been used) read the next record of the input.

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- 2. If an EOF condition has occurred on the input, set FOUND, input to false (0) and exit the loop.
- 3. Otherwise, check the index of the current input record against the index of the current driver record:

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If <, read the next record of the input and go to step 2.

If >, there is no corresponding record in the input. Set FOUND, input to false (in case the index of the record, just read may match that of some subsequent driver record)

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To support this algorithm a flag FOUND. Input must be declared for each note driving input and initialized to true (1) before the main loop.

The implementation of the rest of the main loop's body (following the matching code) consists of code that attempts to compute the output record using only those non-driving inputs whose FOUND flags are true. Basically, in this code, the PRESENT checks of the HIBOL description become checks on the corresponding FOUND flags.

This matching process must be implemented for every non-driving input in a data driven

Data Driven Loops

```
PAY_COMP: PROCEDURE;
(declarations)
ON ENDFILE (RATE) EOF.RATE = '1'B;
ON ENDFILE (HOURS) EOF. HOURS = '1'B;
READ FILE (RATE) INTO (RATE_RECORD);
LEVEL_1_MINIMUM.EMPLOYEE = RATE_RECORD.EMPLOYEE;
DO WHILE ( EOF .RATE);
   IF EOF . HOURS
      THEN DO: /* THIS READS ITEMS, SEQUENTIALLY, FROM A FILE UNTIL THE REQUESTED-
                 RECORD IS FOUND (SET FLAGS TO TRUE) OR PASSED (SET FLAGS, TO FALSE). */
              IF FOUND . HOURS_RECORD
                                           ns and disker
                                                          三世界自治療性疾病(1) (2) (2) (2)
                 THEN READ FILE (HOURS) INTO (HOURS_RECORD);
                                                                          ·普勒基中的标题的"2016年
                                                                      温度设计设置 建油铁矿
          HOURS_RECORD_COMPARE:
              IF EOF HOURS
                                                        SUMMEDIAN TO THE JOSE CAND
                 THEN FOUND . HOURS_RECORD = '8'B;
                                                      (8 9 ) NATER OF
                ELSE IF HOURS_RECORD_EMPLOYEE = LEVEL_1_MINIMUM_EMPLOYEE
                        THEN FOUND HOURS RECORD : 11'S ATT STORES STORE SEE SAUT
                        ELSE IF HOURS RECORD EMPLOYEE > LEVEL 1 MINISHIM, EMPLOYEE
                                           THEN FOUND HOURS RECORD . . . . . .
                                ELSE DO: READ FILE [MOURS] INTO (HOURS_RECORD):
                     GO TO HOURS RECORD COMPARE;
                                     END:
           END:
                          ..... e opprødja også a distable for te te
   IF FOUND HOURS THEN DO; PAY RECORD PAY - RATE RECORD RATE + HOURS RECORD HOURS;
                          PAY RECORD . EMPLOYEE . LEVEL 1 MINIMUM . EMPLOYEE;
                          WRITE FILE (PAY) FROM (PAY_RECORD);
                       END:
                               ÁR MORRE BARRES A BLI
   READ FILE (RATE) INTO (RATE_RECORD);
   LEVEL_1_MINIMUM.EMPLOYEE = RATE_RECORD.EMPLOYEE;
END:
END PAY_COMP;
```

Figure 2: PL/I code for PAY IS RATE * HOURS

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First, notice that the iteration structure is fundamentally different from that for a single driver loop. The index value determination and EOE checking is now performed at the beginning of the loop body. As always, the iteration is terminated when all drivers are exhausted (when the flag EOE_SO_FAR ends up true efter all drivers have been read). Thus the toop exit must appear before the output calculations and the form OO WILLE ('1'B) is used instead of OO WILLE (-EOF, driver) (as in the single driver case). This is just a minor variation on the basic scheme.

What is interesting in the implementation of Fig. 3 is the use of the PL/I ACTIVE structure MERCHARD SHOUTH AND THE ! and the ACTIVE_DRIVER_COUNT variable in determining the proper next index value. The idea is CHAN SHARESH AND SANS to look through the drivers in succession. The first is used to establish a tentative index value for homelow of respondent or medelined f the current iteration. The first driver is also given a number that marks it active (for the time िया के निवादी से स्वरूप अवस्था के कार्य के कार्य के की बेरिक प्राथमित अने के अने के कार्य कार्य के अने कार्य के being). If the next driver has the same index value it is given the same number, indicating that it will be active when the first is if it has a lower index name the loop index is reser and the second the of tem is and go to step 5 (existing loner hop) driver is assigned a higher number, meaning that it is tentatively active (and, effectively, that the ordinal compression accomplished by the compression of the compression first is inactive). When all drivers have been examined, those sharing the trighest ACFIVE number (held in ACTIVE_DRIVER_COUNT) are masked defined, and the main are marked not defined. mateinunis selt steambore vetingselt formet in a cess

V.2 Multiple-Level Loops, with this the best of the passed and the best respectively to the following and the

Multiple-level loops introduce the need for maintenance of current index values for each distinct loop level and for control structures to implement loop driving from loops at lower levels.

Multiple-level loops arise from two basic sources reduction computations and mixed-index matching computations. Let us examine the implementation of each in turn.

³¹ It could be done at the end of the body if the same code were duplicated as an initialization before the loop were entered. We have refrained from doing this to minimize code.

First, nexts that the sequence structure is fundamentally dult the state of the s of the long half. It disable PROPERTY OF THE PARTY OF THE PA A COLUMN TO THE SHAPE OF THE SH the correct because, the

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Data Driven Loops

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Jagorija (2005.) Politika (1906.)
  I TEMDEMAND_COMP : PROCEDURE ;
 (declarations)
READ FILE (BEMAND) INTO (DEMAND RECORD):
 IF EOF DENAMED THE LEGIC OF THE RESERVENCE AT A SPECIAL PROPERTY OF THE PARTY OF TH
                      THEN DO; LEVEL_2_MINIMUM.ITEN . DEMAND_RECORD.ITEN;
                                                                                     LEVELS_1_THINL2_MININUM.LIEN - LEVEL_2_MENINUM.ETEN; AND THE ADDRESS OF THE ADDRE
                                                           END:
                      ELSE LEVEL_1 = '0'B;
DO WHILE (LEVEL 13:00 MONTH TO CONTROL TO THE ST. BOOK MATERIAL TO BE A TO DESCRIPTION OF A ST.
                       DEFINED. ITEMDEMAND . '8'B:
                                                                   ्रमुख्य इंडिया करका प्रोप्त के अन्यक्षण के के करका एवं के कुलिक के किस्सार के कर का का किस के किस के आसी.
                      BO WHILE (LEVEL_2);
                                              EF. DEF THEO, I VENDERAND 2000 FOR 1994 OLDER OF SOME REGION 1999 FROM HUMAN SEGMENT OF THE VENDER TO THE TRAINS
                                                                    THEN ITEMDEMAND RECORD ITEMDEMAND = ITEMDEMAND RECORD. ITEMDEMAND + DEMAND_RECORD. DEMAND;
                                                                   ELSE DO: LTEMDEHAND RECORD TEMPENAND DEMAND DEMAND PLANTED OF LEGISLAND PROPERTY OF LEGI
                                                                                                                                 BEFIRED. ITEMBEMAND = '1'8:
                                                                                                      EMD:
                                                                                                                                                                                                                                                                                                                                                                                               Anything to the feet state Company China
                                              READ FILE (DEMAND) INTO (BEMAND RECORD):
                                                                                                                                                                                                                                                                                                                                                                                               where the continue of the desire that the state of the st
                                               IF EOF DEMAND
                                                                    THEN DO; LEVEL_2_MINIMUM.ITEM = DEMAND_RECORD.ITEM;
                                                                            IF LEVEL & MANAGEMENT TEN & LEGELS 5 WIND 2 MANAGEMENT STEN
                                                                          ne unare
                                                                                                                                                      THEN LEVEL: 2 - 1078:
                                                                                                END;
                                                                   ELSE DO: LEVEL 2 14 1914: But III VSD/A and System PRESTOR BUT IN BUT IN THE FOR A
                                                                                                                                  LEVEL_1 = '0'5:
                                                                            and 🕬 🕻 i de la la graph de de la completa del completa de la completa de la completa del completa de la completa del la completa de la completa del la completa de la co
                      END:
                                                                      ITEMDEMAND_RECORD.ITEM = LEVEL_1_NINIMUM.ITEM;
                                                                                                                                                                                                                                                                                                                                                                                                                                    一元以。此與數據的資本的一個目的一人自由的人才的一個人
                      WRITE FILE (ITEMBERAND) FROM (ITEMBERAND RECORD):
                        IF EQT. DEMAND SHEET OF CONSTRUCT ON THE LEFT OF CONTROL OF CONTRO
                                               THEN LEVELS_1_THRU_2_MINIMUM.ITEN . LEVEL_2_MINIMUM.ITEM;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Jack Strain
 ENO:
  END ITEMDEMAND_COMP:
                                                                                                                                                                                                                                                                                                                                          ya yakindanaksii ikkin kakanin aproduton maad
```

Figure 4: PL/I code for ITEMDEMAND IS THE SUM OF DEMAND FOR EACH ITEM-ID

The reader should have little difficulty in understanding this code. This that the variables LEVEL_1 and LEVEL_2 are used as flags to control the hundres of the outer and "blist" local respectively. LEVEL_I is countiedly equivalent to ESF. in all the The Counties and the latest the l READ FILE (BEMAND) INTO (BEMAND MEGDES); or the attention of . It when the file to be reduced is eshoused. LEVEL 2 has **-- --** ---THER BO: LEVEL 2 MINISTER . DEPAND RECORD . I TEM: accumulated is exhausted (i.e. whose there The state of the s inner value.

THE THE PERSON NAMED IN The variables LEVEL 2 NIMBERN, FEET and LEVELS 1 NIMB 2.1 AND . BOOM SERVICE . 0 381736 heap track of the current input record's hour of value and the enough process THE RESERVE AND IN IT. I WAS IN perpetitively. A > comparison between these two is and THEN TEHNERAND SECOND STRENGIAMS . STEINGHAMD RECORD STRENGENAM . OF MAND SECOND DEMAND; ELSE SO, LIENDERSON acouse the input's records are unded but at . 8"1" · DAMESTON ST. | 0.38"1 138

V22 Mixed-Index Marking Computations

READ TILE (DEMAND) 18TO (BENAMO RECORD);

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Consider the natural lastes can

THEN DO: LEVEL 2 MIREIMIN. ITEM . REMAIN MECORD. LIER.

EXECUTATE IS NO **通过 图**别 . 牌 : 0#3

where EXTENCEIPRICE and COMENSURER have the links it has the school life Shell WRICE has WW . 1 19733 ...

the index (item-id). Suppose that, as above, the Optimizing Deligner has a

seconds of CONTENTIONER are sorted by the key I top-Id. As my harm disconsidered, CONTENTIONER TEMPERARD RECORD, LIEN . (ENG.) PERSONAL LINES. VRITE FILE (ITEMBERAME) FROM (ITEMBERAME RECORD):

can be used to drive the computation.

Recouse CONCENTINEER is sected by I tem-id first, the template THEN LEVELS T THRUE 2 MINISTERN LEGY & LEWEL 2 MINISTERN LICHT.

several as follows:

: 243

WHO DEMANDERSTI ON S

9. (Initialize) Read a record of the CLIMENNINER Me.

Figure & PL/I code for ITEMERAND IS THE SUM OF DETINAD FOR EACH ITEM-ID

I. Read records from the PRICE file until either:

- a. one is found that has an item-id value matching the driver's item-id value, in which case all EXTENDEDPRICE records for that value can be generated; or
- b. one is found that has an item-id value greater than the driver's, or the PRICE file is exhausted, in which case there is no matching value and the inner loop can be skipped.

Treatment of the company of the New York

2. (Inner loop) Generate all output records for the given Pten-Id value, reading records from the driver as you go. When a driver record is read that has an Item-Id value greater than that of the current PRICE record, or the driving file is exhausted, exit: 10 13 13 13 13

3. If neither input file is exhausted go to step I and repeat; otherwise exit.

In this way each record of the PRICE file is read only once 32

A PL/I implementation of this algorithm is shown in Fig. 5. The reader will notice that this implementation is unnecessarily inefficient because when a matching PRICE record is not found the inner loop is executed anyway. This is done to Missirate what happens in the general case where there may be calculations in the inner loop that can still be performed without the use of a missing input.

V.3 Aggregated Computations

The aggregation of two or more computations into one nested loop introduces a consideration not seen before: the synchronization of computations at different loop levels. Consider the two HIBOL computations:

EXTENDEDPRICE IS PRICE * CURRENTORDER IF PRICE PRESENT AND CURRENTORDER PRESENT

VALUESHIPPED IS PRICE * ITEMDEMAND IF PRICE PRESENT AND ITEMDEMAND PRESENT

³² If CURRENTORDER had been unsorted or sorted differently, records from PRICE would generally be read more than once.

TERRETOR TO WAR AND THE TERRET

where CURRENTORDER is the same as above (with index (i.tem-id, store-id)) and ITEMDEMAND is a file with index (i.tem-id). As we have seen above, the first computation can be implemented as a two-level nested loop. The second computation iterates over the single-key item-id and so has only one level.

When aggregated the result is a two level loop: 33 The Property of the second s

Logo I (outer logo), and secretary an expectage three transport early feel and improve the Maria Maria

Level: (item-id)

gent value sets to inputers PRICE, LIFTDENANDES seas the second of the color and in order

Protog:

calculate value-shipped

Outputspempty

egraphie og de **de neutre entu**al é la service de la la companie de la companie de la companie de la companie de

Epilog:

empty

OutputsedVALUESHIPPEDL and area to anorarcies, at reas aid as a biora

Loop 2 (inner loop)

the prince that later affects the area in appearing the second second second second second second

Inputso: ICURRENTORDER)

he agreed gue Reo logist the Galoulate textended price a bettee den a paid of the banks

Dutput spilextendedPRICEI

Imputs: empty

Epidog: grafi panetur in paline bear actors, par to accomplic the tonions of their

Outputscemptu

What is significant here is that the computations in the aggregate occur in different levels.

Suppose that the PRICE file is guaranteed to have a record for every 1 ten-id. Then I TEMDEMAND is the natural choice for a driver for the value-shipped computation because a record of the output will be generated if and only if there is a record in I TEMDEMAND for the same key. As for the extended-price computation, CURRENTORDER is the only possible choice for the driver.

Now the outer loop iterates over iten-id values determined by both drivers. Suppose the first record of each driver is read. There are three cases, distinguished by the relative values of the item-id keys in these records:

³³ Notice that in finalized loop description there is no General section.

And a feet of the participation of the participatio

Data Driven Louis

```
(declarations)
(ON conditions)
(read CURRENTORDER and initialize LEVEL_2_NININUN_ITEN = CURRENTORDER_RECORD_ITEN;)
(read ITEMDEMAND and initialize
                                                                                              LEVEL_1_MINIMUM.ITEM . ITEMBEMAND_RECORD.ITEM;)
                    (code to set the synchronization flag for each level to false if its driver had no records)
IF LEVEL_2_MINIMUM.IYEM > LEVEL_1_MINIMUM.ITEM
                       LEVEL 2 - '0'8;
                                               LEVELS_1_THRU_2_MIN HUM. FEM = LEVEL_1_MINIMUM_1YEM:
                 ELSE IF LEVEL_2_MIN ININ. I TEN C LEVEL_T_NINNIN. I TEN
                                             THER DO: BO_LEVEL_1 = '0'8;
         opportunity of a transportunity of the property of the propert
                                                                     LEVELS_1_THRU_2_NINIMUM.ITEM = LEVEL_2_NINIMUM.ITEM;
                                                                                                             led Ideagle Dalici and housest broken confirm content on net consist
                                                          EMD:
                                             ELSE 90; BO LEVEL 1 = '1'8;
                                                                                                                                                                        TO STATE OF THE PARTY OF THE PARTY OF
                                                                    LEVEL 2 . '1'8:
                                                                    LEVELS_1_THRU_2_MIN PRIM. STEN = LEVEL_1_MINISHEN. TTEN:
                                                                                                                                                       CONTROL A BANKED.
                                                          END: )
                                                                                                                                                  HIS THE BRANK S.
                                                                                                                                     LINGUIS EN UNI.
   BO WHILE (LEVEL_1):
                                                                                                                                经额付额的复数 经转进 医线照接的
            (read PRICE record)
            IF DO_LEVEL_1 THEN (calculate value-shipped) / Freig LEVEL_1 /:
          IF FOUND. PRICE RECORD THEN (calculate and write extended-price)
        ( read Countationner, and reset Levelys Minimum Litten & Colone attonic Record . Livelys Minimum Litten & Colone & Co
                    (check for eof)
                    ELSE LEVEL_2 - '1'8;
           ENB /* LEVEL_2 */;
                                                                                                                                                                  蟾蜍 1966年1968年 1966年第四日日,于西南部市市市大学中央基础
            IF DO_LEVEL_1 THEN DO /* Epilog LEVEL_1 */;
                                                  LIF DEFANED WHEDESHIPPED THEIR (units value shipped record)
                                                                        (read ITEMBEMAND and reset
                                                                   ALENET J. WIN HOUR THEN WIT TESTACHOOM TECONO TYEN: 7
                                                               END /* Epilog LEVEL_1 */;
(synchronization code exactly as above)
END /* LEVEL 1 */:
```

Figure 6: Illustration of synchronization code for aggregated computations

and all fillers and substitute design.

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ile Compani del

Figure 9: [Bisedalare of spectrosidation code for appropriations

Data Driven Loops

```
DECLARE DSAGI INPUT FILE SEQUENTIAL RECORD,
        PAY OUTPUT FILE SEQUENTIAL RECORD:
DECLARE 1 PAY RECORD.
            2 EMPLOYEE FIXED DECINAL (4).
            2 PAY FIXED DECIMAL (4).
        1 DSAG1 RECORD.
            2 EMPLOYEE FIXED DECIMAL (4).
            2 DEFINED ALIGNED.
                 3 HOURS BIT (1).
                 3 OVERTINE BIT (1).
           2 HOURS FIXED DECIMAL (3):
            2 OVERTIME FIXED DECIMAL (3);
            2 EMPLOYEE FIXED DECIMAL (4).
            2 HOURS FIXED DECIMAL (3):
DECLARE 1 EUF ALIGNEU.
            2 DSAG1 BIT (1) UNALIGNED INITIAL ('0'8):
ON ENDFILE (DSAG1) EOF. DSAG1 = '1'B;
READ FILE (DSAG1) INTO (DSAG1_RECORD);
DO WHILE (- EOF.DSAGI):
    IF DSAGI.DEFINED.HOURS
      THEN DO:
           PAY_RECORD.PAY = DSAG1_RECORD.HOURS * 3.0;
           PAY_RECORD.EMPLOYEE - DSAGI_RECORD.EMPLOYEE:
           WRITE FILE (PAY) FROM (PAY RECORD);
           READ FILE (DSAG1) INTO (DSAG1 RECORD):
                                编码设施 医克克克曼氏病 计数据设置
           END:
                               property with the first of the second of the second
      ELSE:
           READ FILE (DSAG1) INTO (DSAG1_RECORD);
```

PAY_COMP: PROCEDURE:

END:

END PAY_COMP;

Figure 7: PL/I code for PAY IS HOURS * 3.88 with Aggregated Flow

ma per la como deta de la misma de estre discolado

PAY COMP: PROCECURE:

V.5.1 Sequential Access

DECLARE DSAGI INPUT FILE SEPTENTAL SECTED The state of the s Segrential access of segrentially over DECLARE I PAY RECORD. IN THE PERSON OF THE PERSON OF THE 2 PAY FIXED DECIME (M). with regional (2) augmination is not promitted. I DSAGI RECORD,

2 FIFLOYEE FIXED DECIMAL (4).

2 DEFINED A ICHED.

V.52 Core Table Acres

3 HOURS BIT ELL.

3 OVERTILE BLI (II) When the records of an input file are to be address by the received, code is 2 HORS FIXED DECIN CONTRACTOR OF THE SECOND that holds not just a single record, but one house on S parel billing in the like II, for example, the Wille M. W. L. Ball ON ENDETTE TORNETT ECT VALET organized sequentially and were to be assured by our falls in READ FILE (DSAGI). HATO TOSAGI RECORDI: unerated:

00 WHILE (- EOK. DSAGE):

THEN DOS

IF CEAST. CEFINED. HOLES

1 PRICE RECEND (64000). 2 1 EM FIRM DECEMBER (A) 2 PRICE FIRM METERS (4).

and the code to fall up this table wa PAY RECORD. PAY - DEMOL RECORD. HOURS . 3.6;

SS PRICE RECORD MINEY = 1 TO 44 READ FILE CONCEPT IF EUF.PRICE THE IN

READ FILE (DSAGL) INTO IDSAGL RECORD);

ENTRIE PRICE: PRICE PERME SIZ - PRICE PERME EWD:

If the laput file is rejuctably at indexed appointed suggestion, the section in t in some order by the record keps. The LEGISTAN CASH AND LIGHT 11 13 (0.38) ONS imput is compatible with the sect order associated with the drivers of the

Figure 7. PLH code for PAY 15 HOURS * 3.88 with Aggregated Flow

The only difference is in the ICL distinction of the Mr.

used. If the sort orders are compatible the method of access is completely analogous to sequential access except that "records" are "read" from the table instead of secondary storage (see Fig. 8).

If the input file is "randomly" organized (regional (2)) the access code generates a hash index and then mimics the PL/I access procedure: compare the key values of the indicated table entry with the desired ones; if identical stop; otherwise examine successive entries in wrap-around fashion until an empty slot is found (end of the bucket) or a complete cycle has been made. If the sort orders are not compatible a more complicated binary search is implemented.

V.5.3 Random Access

When the records of an input are directly (regional (2)) organized the file is randomly accessed. Instead of using a loop, as with sequential access, a single read, using a calculated key is executed. For example, if the PRICE file in the EXTENDEDPRICE computation (above) were randomly accessed, the accessing part of the code would be:

```
PRICE_RECORD_HASH_VALUE = MOD (5 * (MOD (LEVEL_2_MINIMUM.ITEM,)),);

PRICE_RECORD_HASH_VALUE_STRING = PRICE_RECORD_HASH_VALUE;

PRICE_RECORD_HASH_KEY =

LEVEL_2_MINIMUM.ITEM || PRICE_RECORD_HASH_VALUE_STRING;

FOUND.PRICE_RECORD = '1'B;

READ FILE (PRICE) INTO (PRICE_RECORD) KEY (PRICE_RECORD_HASH_KEY);
```

The first three statements calculate the source key string which has two parts: the region number (rightmost 8 characters) and the comparison key (the remaining characters). The case where the record is not present is handled by the statement:

ON KEY (PRICE) IF ONCODE = 51 THEN FOUND.PRICE_RECORD = '8'B; which resets the FOUND flag if a "keyed record not found" error occurs.

Data Driven Loops

```
IF EOF .PRICE
                                THEN DO: IF FOUND.PRICE_RECORD
                                                                                                                                                         THEN IF PRICE RECORD INDEX ( = PRICE RECORD SIZE
                                                                                                                                                                                                                                                   THEN PRICE_RECORD_INDEX = PRICE_RECORD_INDEX + 1;
                                                                                                                                                                                                                                                 ELSE EGG. PRICE . "1"A: Ferri De Com Cara de Sala de S
                                                                                 PRICE_RECORD_COMPARE: We have a second and the second seco
                                                                                                                                   IF EOF . PRICE
                                                                                                                                                         THER FOUND PRICE RECORD = 1818;
                                                                                                                                                               ELSE IF PRICE_RECORD.ITEM = LEVELS_1_THRU_2_MINIMUM.ITEM
                                                                                                              the entropy of the stay of the property of the stay and the stay of the stay o
                                                                                                                                                                                                                                                   THEN FOUND . PRICE_RECORD * '1';
                                                                                                                                                                                                                                               ELSE_IF_PRICE_RECORD.+TEN > LEVELS_1_THRU_Z_MINIMON:1TGN
                                                                                                                                                                                                                                                                                                                                      THEN FOUND . PRICE_RECORD = '8'8;
                                                                                                                                                                                                                                                                                                                                     ELSE DO; IF FOUND.PRICE_RECORD
                                                                                                                                                                                                                                                                                                                                                                                                                                                             THEN IF PRICE_RECORD_INDEX < = PRICE_RECORD_SIZE
                                                                                                                                                                                                                                                                                                                                                                                                                                      THE PRICE PR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             PRICE_RECORD_INDEX + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                   GO TO PRICE_RECORD_COMPARE;
                                                                                     END:
```

Figure 8: PL/I Code for Reading PRICE by Core Table in the Extended Price Computation

in the second second second

V.6 The General Case-A Summary

We have seen that the basic code structure for a computation consists of the following four parts:³⁵

declarations

on-conditions

loop initialization

the nested loop³⁶

The basic structure of the body of each loop in the nested loop is as follows:

read & match non-driving inputs

Prolog calculations

inner loop (if any)

Epilog calculations

write outputs

read active drivers

determine new active drivers and index values for the next iteration

loop synchronization code

exit on EOF or (for inner loop) sub-index change

³⁵ It may be interesting to note that ProtoSystem I's code generator generates these sections simultaneously as four separate output streams (rather than sequentially) that are catenated together when they are all finished.

There is no clean-up code following the loop because the end of the job step which is the computation does everything necessary, including the closing of files.

Appendix I: The Simple Expositional Artificial Language (SEAL)

As an aid to discussing loops we invent an artificial language similar in form to traditional high-level languages such as ALGOL, PL/I and FORTRAN. The basic constructs of this language are:

Iteration: expressed by the construct:

for each <loop-index> from <driving-flow-set>
 <body>

which has the meaning: perform the actions contained in the

sody: perform the <loopindex> obtained from the flows in the <driving-flou-set>. <loop-index> is the either the
name of the index associated with the flows in the <driving-flou-set> or (for reasons that
become evident in this paper) a sub-index of corresponding sub-flows. The set of values that the

<loop-index> takes on is the union of the index sets of the drivers. This set is enumerated at
execution time by reading successive records of the drivers.

I/O and defined: input (record fetching) is expressed by the get operator, thus:

get <variable-instance>

where <variable-instance> specifies a flow and a particular value for its index, represented as a variable (see below). A statement like this means: fetch the indicated record if it exists.

Output is expressed by the unite operator, similarly:

write <variable-instance>

The defined operator is a logical operator for use in conditional expressions. It is applicable only to flow variable instances. The form

defined[<variable=instance>]

evaluates to "true" if the specified record or the indicated flow exists. In particular, if the record is an input (obtained through a get) it is "defined" if and only if the pet subceeded; if the record is an output it is "defined" if and only if the generating code produced a datum for the record.

Conditional Execution: expressed by the familiar if then the construct:

```
if <condition> then <statement-list>; else <statement-list>;
```

which means that if the logical expression < condition> evaluates to "true" perform the statements in < statement-list>1; otherwise, perform the statements in < statement-list>2.

Logical expressions can be formed using the arithmetic comparison operators, the defined operator, and the logical connectives and, or and not.

Conditional Expressions: expressed by the construct:

```
if <condition> then <expression><sub>1</sub>
```

which evaluates to the value of <expression>₁ if the logical expression <condition> evaluates to "true" and to the value of <expression>₂ otherwise.

Variables and Assignment: expressed by the construct:

<variable> = <expression>

where = is the assignment operator.

A variable can be either a scalar or an indexed variable. Flows are represented as indexed variables with an index identical to the flow's index. Thus, DEMAND-Litens id, atore-id) is the variable corresponding to the DEMAND flow and an instance of its index selects the datum of the corresponding flow record. That is, for example, the statement

DEMAND (1234, 5678) = CURRENTORDER (1234, 5678) + BACKORDER (1234, 5678)

means that the datum of the record of DEFINED for item #1234 ordered by store #5678 is to get the value obtained by adding the data of the corresponding records from CURRENTORDER and BACKORDER.

Typically, the record-by-record computation implied by a HIBOL flow equation would look like that equation translated into our artificial language (with a generalized index), such as

DEMAND(item-id, store-id) =

if defined[CURRENTORDER(item-id, store-id)] and defined[BACKORDER(item-id, store-id)]

else if defined[CURRENTORDER(item-id, store-id)]

then CURRENTORDER (item-id, store-id)

else if defined (BACKORDER (item-id/store-id))

then BACKORDERfiten id, store-id)

else undefined

and would appear somewhere in the body of loop.

Sub-flows: A sub-flow (for use in the for each construct) is expressed by:

<flow-variable>(<sub-index>)

For example,

CURRENTORDER (item-id)

denotes the sub-flow of CURRENTORDER consisting of just those records whose indices correspond to the value of the sub-index (item-id). Generally, the value of the indicated sub-index is fixed by an enclosing loop.

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