UNIVERSITY OF ILLINOIS

DIGITAL COMPUTER LABORATORY

LIBRARY ROUTINE M 28 - 270

TITLE:

Matrix Multiplication with or without rescaling (SADOI)

TYPE:

Entire program

ACCURACY:

ll decimal places (see Note 1)

DESCRIPTION:

The routine will form the product of two matrices,

$$A_{ij} B_{jk} = C_{ik}$$
.

Features of the routine are:

- 1. Matrix C can either be punched on tape or stored on the drum.
- 2. Matrix B can be rescaled by any power of ten prior to the multiplication; this enables the user to scale down the elements of C to prevent overflow or otherwise to adjust the scaling of C.
- 3. A set of products of various sizes, $A^{(p)}_B(p) = C^{(p)}$, can be produced without rereading parameters, and these products can all be stored on the drum for use in subsequent operations.
- 4. Multiple products such as $A^{(3)}A^{(2)}A^{(1)}$ B = C can be formed without punching intermediate results on tape.

METHOD OF USE:

CASE I, $A_{ij} B_{jk} = C_{ik}$ Stops

1. Master tape 3402L

2. Parameter tape, type T 24060

3. Data tape B 240J7

4. Data tape A (with J term. sym.) 2402L

To begin a new problem at stop 2402L reading different parameters, raise the black switch.

Matrix C is either punched on tape by rows, each element to "d" decimal places, or else, starting at location "D" on the drum, matrix C is stored by rows with a row sum check at the end of each row. This option is specified by the parameter tape.

If matrix C is punched on tape, i, the rows of C, is not limited. The capacity of the computer for j and k can be

determined from the chart shown in the section on STORAGE OF MATRIX B. See also section on STORAGE OF MATRIX C. For alternate methods of use, see sections on CASE II, CASE III, and CASE IV.

PREPARATION OF DATA TAPES:

The elements of both B and A matrices are punched by rows as signed fractions with an N at the end of each row. If any row terminating symbol is an F instead of an N, the computer will stop. By raising the black switch, the reading of the matrix is resumed. (See Note 2)

In addition to row terminating symbols, each matrix has a matrix terminating symbol. After the final row symbol, a J or an L is punched. No distinction is made between a J or an L at the end of a B matrix. For each, the computer will stop. When the black switch is raised, the computer will begin to read an A matrix.

If a J terminates an A tape, when reading is resumed by raising the black switch, the computer will interpret the next tape as a parameter tape. If an L terminates an A tape, the previous parameters are retained, and the reading of a parameter tape is bypassed.

METHOD OF USE:

CAS	$E II, A^{(p)} B^{(p)} = C^{(p)}$	Stops
ı.	Master tape	3402L
	Parameter tape, type T	24060
3.	Data tape B(1)	2 40J7
	Data tape A(1) (with L term. sym.)	24060
5•	Data tape B(2)	240J7
6.	Data tape A ⁽²⁾ (with L term. sym.)	24060

If the several C matrices are punched on tape, 30 single hole delays, 3 carriage returns, and a figure shift will separate matrices.

If the C matrices are stored on the drum, they will be stored one following the other in successive locations by rows with a row sum check at the end of each row.

PARAMETER TAPE PREPARATION:

Except for CASE IV, there are three parameters. The order in which they must appear is as follows:

d space number of decimal places or drum address

+ S scaling exponent

X directive

Print or drum store parameter, d.

The parameter, d, must be followed by a fifth-hole character. If d < 13, the computer will punch the elements of matrix C to d decimal places. If $d \ge 13$, d will be interpreted as a drum address at which to store matrix C. Hereafter a drum address will be designated by a capital letter, D. See section called STORAGE OF MATRIX C.

Scaling exponent, + S.

The parameter, \pm S, may be omitted if no rescaling on matrix B is desired. Otherwise, \pm S or \pm S is an integer exponent of 10. Each element of the B matrix will be multiplied by this power of 10 before B is stored on the drum. This has the effect of rescaling the product matrix C. There are no restraints on the value of \pm S other than those imposed by the data. Of course, if the scaler is \pm 12, matrix B becomes a null matrix. Similarly, the largest sensible positive value for the scaler would be a value which would not cause overflow on the elements of C.

The directive, X

The directive, X, must be either an N, J, F, or L. When the directive is an odd number (J or L) and also d is less than 13, the rows of C will be punched in columnar form with a carriage return after each element. An N will be punched at the end of each row and a J at the end of the matrix.

When the directive is an even number (N or F) and also d is less than 13, the rows of matrix C will be printed across the teletype page. A carriage return and two delays will be punched after each n elements where n is the integer part of the quotient, 70/(d+1). At the end of each row of C, an N followed by two carriage returns and two delays will be punched. A J will be punched at the end of the matrix.

Whenever d is 13 or greater, matrix C is stored on the drum, and no distinction is made between odd and even directives.

Type T and Type D

The directive at the end of a Type T parameter tape is either an N or a J. When a Type T tape is read, the computer will stop on 24060. If the black switch is raised. a B matrix will be read from tape. (See Note 3) The directive at the end of a Type D parameter tape is either an F or an L. When a Type D tape is read, the computer will stop on 240SJ. If the black switch is raised at stop 240SJ, a B matrix will be read from the This matrix will be in fact the previously formed product matrix of size i by k stored at drum location D. The matrix will be read a row at a time, rescaled, and restored as a B matrix at location 2560. The method of use for this is explained under the heading CASE III. It is also possible to specify the size and drum location of a matrix which is to be treated as a B matrix. After a Type D parameter tape has been read and the machine stops on 240SJ, if the white switch is raised up and down, three additional parameters will be read as follows:

- D space drum location of matrix
- r space number of rows
- c space number of columns

To exercise this option, the matrix must have been stored on the drum at any time previously in successive locations by rows with a sum check at the end of each row. This is illustrated under the heading CASE IV.

ILLUSTRATIVE EXAMPLES OF PARAMETER TAPES:

METHOD OF USE:

Type T Both B and A matrices are read from tape

10 space N	Print the elements of places by rows across	C to 10 decimal the teletype page.
4 space +2J	Multiply each element to the matrix multipli elements of C to 4 dec rows with a carriage r element.	of B by 100 prior cation; print the imal places by
4558 space N	Store C by rows with a the end of each row in tions starting at drum	successive loca-
Type D The B ma	atrix is read from the	drum, A matrix from
tape		
	Read rows of previously duct from the drum, muby 1/10, and store as a the new product C and to 6 places; print by page.	ltiply each element a B matrix; form print each element
6100 space 53 space 21 space	A matrix Molocation 53, 21, is relation 6100, and restored at 2 matrix A is read from the duct matrix C is stored sum check at the end of successive locations stored (2) A(1) B = C	2560 as a B matrix; tape and the pro- l by rows with a f each row in
		Stops
	first to form the produ	
	s on the drum at locati	ion D.
1. Master tape		3402L
2. Parameter ta	pe, Type T	24060
3. Data tape B	1),	240J7
	l) (J term. sym.)	2402L
	rameter tape is read.	
	nge the scaler or to ch	
	drum, the parameter tap	
	rices terminated by L s	ymbols.
5. Parameter tar	pe, Type D	24 0 SJ
ba. Data tape A'	(2) (L term. sym.)	240SJ

6b. Data tape A⁽³⁾ (L term. sym.) 240SJ

If it is necessary to change the scaler or the drum store location, or, if it is the end of the sequence, and it is desired to print the final product, an A matrix can be terminated with a J, which enables the user to read a new parameter tape.

Data tape A (p-1) (J term. sym.) 2402L Parameter tape, Type D (with "d") 240SJ 8. Data tape A^(p) (J term. sym.) 2402L

CASE IV, A ir Mrc = Cic

are as follows:

Stops Let us assume that a series of steps (perhaps CASE I or CASE II) formed the matrix, M_{rc} , at drum location D* by rows with a sum check at the end of each row. sequent operations have cleared the Williams memory but not the drum. To form the product, A rc, the steps

3402L 1. Master tape 240SJ 22. Parameter tape, Type D

2b. Parameters: D space r space c space Raise white switch up and down

3. Data tape A (with J term. sym.)

240SF 2402 L

STOPS AND ERROR DIAGNOSIS:

Stops	Loc.	Diagnosis
3402L	18J	Master tape has read correctly; bl. sw. to read par. tape.
24060	053	End Type T par. tape; bl. sw. to read B; wh. sw. to convert to a Type D tape.
240SJ	053	End Type D par. tape; bl. sw. to restore B and read A; wh. sw. to read D*, r, c.
240SF	05L	D*, r, c, have been read; bl. sw. to restore M and read A; wh. sw. to read B from tape.
240J7	0 8 S	End of tape B; bl. sw. to read A.
2402L	OJJ	End of tape A with J term. sym.; bl. sw. to read par.
24088	06 S	F term. sym. end of 1st row of B; bl. sw. to continue.

METHOD OF USE:

Stops	Loc.	Diagnosis
20080	087	F term. sym. end of subsequent rows of B; bl. sw. to continue.
200F5	OJL	F term. sym. end of row of A; bl. sw. to continue.
FF001	06к	J or L end of 1st row of B; wh. sw. to continue.
FF002	084	Number of elements in rows of B are not equal; wh. sw. to continue as if =.
FF00 3	of8	Row vector of A does not conform to column vector of B; wh. sw. to new par. tape.
FF00 ¹ 4	0S2	Improper drum address for store of C; wh. sw. will calculate first available address and store C. (See Storage of C on Drum)
FF005	10K	Overflow on element of C; wh. sw. to read par.
FF00 6	109	B sum check failure; wh. sw. to try again.
FF007	18F	Master tape sum check failure; Reread.
FF008	010	Row of C read incorrectly from drum; wh. sw. to try again.

STORAGE OF MATRIX B:

In order that the columns of B can be read from the drum in minimum access time, the first element in each row is stored at 2560 + (j - 1)I. I is determined by the size of k. The capacity for B using the entire drum is shown in the chart below:

k	I	max.j
0 < k-≤ 65	65	157
სე < k ≤ 129	129	s 79
$129 < k \le 193$	193	53
$193 < \mathbf{k} \le 257$	257	39
$257 < k \le 311$	321	31

STORAGE OF MATRIX C:

If matrix C is not stored on the arum, i, the rows of A, is not limited. k and j can be determined from the chart. In any event, the maximum k is 311.

The first available location for the storage of matrix C on the drum will be after the final element of matrix B. This can be determined from the following formula,

$$D = 2560 + (j - 1)I + k$$

where I is the increment between rows of B. Matrix C is stored on the drum by rows with a row sum check at the end of each row. The number of locations required will be i (k + 1) and

$$D + i(k + 1) < 12,800.$$

To direct the computer to store C on the drum, the parameter, d, must be greater than 12, and d will be interpreted as the drum address, D, at which to store C. If d is any number greater than 12, but less than D, the first available drum address, the computer will consider this to be an error and will stop on FFOO4. If the white switch is raised up and down, the computer will print a 5-place decimal address which is D, the first available address. Matrix C will be stored in successive locations starting at D.

For CASE III when multiple products are formed D must be chosen to be warge enough to accommodate the largest B matrix.

About 30 seconds for the reading of the master and parameter tapes.

Time depends upon options exercised which are listed below:

- la. To read matrix B from tape and store on drum
 jk (.005 d_b + .013)
- 1b. To read matrix C from drum and restore as a B matrix

- 2. To read matrix A and calculate

 ij (.005 d_a + **c**010) + ik (**c**04 j + .009)
- 3a. To punch matrix C
 ik (.0167 d_c + .034) + .067 i
- 3b. To store matrix C on the drum i (.002 k + .008)

DURATION IN SECONDS:

NOTE 1:

NOTE 2:

NOTE 3:

Whenever matrix B is rescaled by a positive power of 10, + S, the accuracy of C is reduced from 11 decimal places to (11 - S) places.

It is not necessary to reproduce a large tape to punch a J or an L terminating symbol. The final row terminating symbol N can be hand punched to an F. After the computer stops, insert a single J or L character in the reader and raise the black switch. A Type T parameter tape can be converted to a Type D tape merely by raising the white switch up and down at the stop 24060.

DATE September 28, 1959

PREPARED BY

APPROVED BY

I	CATI)N	ORDER		NOTES	PAGE 1	M 28	1
Abs	Re	el Sym			4.5			1
			003K					
3	,		00F 00397F		Location of	A vector		
4			00F 00554F		Location of			
5	- 1		00F 00711F		Location of			_
6			OOF OOF		Document of	0 466.001		
7			40F L521 (N12)					
			0017K				**	
17	.	(A)	0083 0083			•		
	.	(B)	0054 0054		e e Albana			
1		(c)	0085 0085					-
		(N)	40s4 L521(N1 2)					
		(NL)	80F 00F	by 11,34(P)	Counter for	number of e	elements.	n,per line
		(-)	OOF 001000 0000	* *			· · · · · · · · · · · · · · · · · · ·	
	1	(+)	OOF 006250 0000) 0000J				
		(0)	OOF OOF	r Georgia (m. 1884)				
		(1)	00F 001F					
		(1-1)	001F 001F					
		(10)	OOF OOLOF					
		(12)	00F 0012F					
		(64)	00F 0064F					
		(70)	00F 0070F					
		(D1)	8511F 00F		실하는 경기의 기계 : 1 : 1 : 1 : 1 : 1 : 1 : 1 : 1 : 1 :			
		(D2)	8611F 00F					
		(D3)	00F 002560F					
	ŀ	(D4)	OOF OOF	by 4,14	Store of mat	riv C on dr	m	
		(防)	OOF OOF	by 48(P),7(B5)	IIA O OH UI		e e e e e e e e e e e e e e e e e e e
	1	(D6)	Olf OOF					
		(T1)	L5F 40F	by 4, 8(B2)		•		
,		(T2)	J013F 75F 7	by 5(B2)		. · ·	i i	
		(T3)	NO9F L5F		•		l	
:		(T4)	756F L4F	by 6(B2)				
		(T5)	NOF 4OF	by 5(B5)		er General General Grand	1	
		(T 6)	S68(A2) L5F	by 4 (B5)				
		(T7)	JOF 74F	by 3, 5(B 5)		• ,		
		(T8)	75F 40F	by 2(B2)				

LO	CATIO	N	ORDER		NOTES	PAGE 2	м 28
Abs.	Rel.	Sym.					
		(T9)	801F L5F	by 2(B2)			
		(T10)	N114F L5F	by 7(B2)			
		(110)	OOK	by (DE)	Read param e	ters	
47	0	(P)	414F 41F	from sum chec	_		
''	1	(1)	814F 50F	6(Al)	_ ·		
	2		74(10) S5F				
	3		40F 914F	•			
	4		321L 41(D4)		·		
	5		L5F 403F		Store "d" a	t loc. 3	
	6		F0(12) 3213L		test: d <	13 ,	
	7		F53F 50(0)			•	
	8		007F 40F		·		. '
	9		L5(70) 66F		Calculate N	, no. elements pe	r line
	10		'S5F 10 <i>3</i> 2F				
	11		42(NL) L53F				
	12		0020F 463(A4)				
	13		2215L L53F			÷	
	-14		L4(D2) 40(D4)		÷		
	15		524F 5015L		nead scaler	and directive;	
	16		26(N12) 405F		Store at lo	oc. 4 and 5	
	17		L34F 3230L				
	18		L54F 3223L				
	19		402F L5(-)		Negative sc	aling multiplier	at loc.13
67	20		4013F F52F				
	21		402F 3230L				÷
	22		5013F 7J(-)		e e		,
	23		2620L 50 (0)				
	24		L54F 0022F			•	
	25		4612(B4) L14F			٠ ٧	
ŀ	26		402F L5(+)		positive sc	aling multiplier	at loc.13
	27		4013F F52F				
	28		402F 32 30 L				
} .	29 30		5013F 7J(+) 2627L 4116F				a
	31		50(0) L55F				

×

LOCATION		V	ORDER		NOTES	PAGE 3	м 28
Abs	Rel.	Sym.					
	32		101F S3F				
	33		3234L L5(1)		test: directi	ve is odd or even	
	34		42(NL) L55F	from 12,14(Al	į		
	35		FO(1) 3236L		test: directi	ve is F or L	
	36		24(B1) 24(B6)	\	stop: 24060 -	240SJ	
	37		192F 4 01 F		·		
	38		L5(10) 4243L	Į	white switch t	o read	
	39		41F 814F		D*, r, c.	н.	
87	40		50F 74(10)		·		
	41		S5F 40F		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
	42		914F 3640L				
	43		L5F 40F				
	44		F543L 4243L				
	45		L51F L41F		ŀ		
	46		401F 3639L				
	47		L510F L4(D2)	Market			
	48		40 (D5) 241(B6)	Stop: 240SF		
			OOK			:	
96	0	(B1)	50S4 50L	from 36(P)	Read first ro	w of B	
	1		26(N12) 401F				
	2 .		L521(N12) 407	F	N12 store ord	er at loc. 7	
	3		LO(N) 1020F				
	4		4012F 504L		"k" at loc. 12	2	
	5		26(B2) L5(1)		tally "j" at	loc. 11	,
	6		4011F 416F		and the second s	•	
	7		L51F LO(1)		A. Carlotte and Ca		
	8		369L 2210(B3)		**************************************		
	9		LO(1) 3210L		FF1: Jor La	at end first row o	f B
	10		FF1F LO(1)		wh. sw. to cor	ntinue	
	11		3610L 2410 (B3)	Stop on F: 21	+088	
			00К				
108	0	(B2)		from 5(Bl)	Set test const	tants	
	1		L5(C) L412F	2(B6)	Security of	•	
	2		42 (T8) 42 (T9)		The state of the s		
	3		427(A3) L5(B)		A CONTRACTOR OF THE CONTRACTOR		
	4		L412F 42(T1)		F		

LO	CATIO	N	ORDER		NOTES	PAGE 4 M 28
Abs	Rel.	Sym.	·			
	5		42(T2) 42(T3)			
	6		42 (T4) 42 (T5)			
	7		42(T10) 0020F			
	8		46(T1) L512F			
	9		LO(1) 402F			
	10		F5 (64) 408F		Calculate drum	increment. I.
	11		152F FO(64)		for store of B	i i
	12		3613L 2215L			
	13		L4(1) 402F			
	14		F58F L4(64)			·
	- 15		2210L L5(D2)			
	16		L4(D3) L08F		preset drum sto	re order at loc. 9
	17		409F 22F			
	•		оок			
126	0	(B3)	50S4 50L		Read subsequent	rows of B
	1		26(N12) LO(1)			
	2		367L F511F		tally "j" at lo	e. 11
	3		4211F L521(N12	?)		
	4		LO7F 40F			·
	5		L3F 3210L		test: elements	of rows are equal?
	6		FF2F 2210L		FF2: elements	≠; wh. sw. to
	7		LO(1) 328L	,	continue	·
	8		2212L LO(1)			
	9		3212L 202L		Stop on F: 200	80
	10		50(0) 5010L	from 8,11,(B1)	
	11		26(B4) 22(B3)			
1	12		50 (0) 5012L			:
	13		26(B5) 24(A1)		Stop on J or L:	240J7
			оок		4	
140	0	(B4)	K5F 4225L	from 11(B3),2	1(Bó) Res	cale row of B and
	1		L5(B) 427L			·
	2		467L 4211L		store on drum	
	3		4212L 4217L			
	4		4222L L34F			
145	5		3215L L54F			
	6	9	3611L 5013F		negative rescal	ing
	7		75F 40F			

CATION		ORDER		NOTES PAGE 5 M 28
Rel.	Sym.			
8		L57L L4(1-1)		
9				
10	·			
11		·	·	
12		OOF 4OF	by 25(P)	positive rescaling
13		F511L 4211L		, o
14				
15		· · · · · · · · · · · · · · · · · · ·		
16		L48F 4018L		
17	. ,	409F L5F	by 3L	NA.
18		OOF OOF	by 16L	Store on drum
19	·	F518L 4018L		
20				
21				
22		*		sum check for B at loc. 6
23				
24			·	
25		3622L 22F		
		оок		
0	(B5)	K5F 4221L	from 13(B3),25	5(B6)
1			N. A.	Set additional test constants
2				
3	· ·			
4	·			
5				
6			•	clear row counter for A at loc.10
7				
8				
9				
10		* *		
11		` *		
12	ļ			FF4: Drum address too small
13			3)	for store of C; wh. sw. to
14				find first available address and t
15	*	40F 5022L		Print corrected address
	Rel. 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14	Rel. Sym. 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 0 (B5) 1 2 3 4 5 6 7 8 9 10 11 12 13 14	Rel. Sym. 8 L57L L4(1-1) 9 407L L0(T1) 10 326L 2215L 11 5013F 75F 12 00F 40F 13 F511L 4211L 14 4214L L0(T2) 15 3611L L59F 16 L48F 4018L 17 409F L5F 18 00F 00F 19 F518L 4018L 20 F517L 4217L 21 L0(T3) 3217L 22 L56F L4F 23 406F F522L 24 4222L L0(T4) 25 3622L 22F 00K 0 0 (B5) K5F 4221L 1 L5(A) L411F 2 0020F 467F 3 46(T7) L5(B) 4 L411F 42(T6) 5 42(T7) 42(T5) 6 4110F L5(D4) 7 40(D5) L3(D4) 8 3219L L316F 9 3610L 2221L 1	Rel. Sym. L57L L4(1-1) 9 407L L0(T1) 10 326L 2215L 11 5013F 75F 12 00F 40F by 25(P) 13 F511L 4211L 4214L L0(T2) 15 3611L L59F by 3L 16 L48F 4018L by 3L 17 409F L5F by 16L 19 F518L 4018L by 16L 20 F517L 4217L 21 21 L0(T3) 3217L 22 22 L56F L4F 406F F522L 24 4222L L0(T4) 7 25 3622L 22F 00K 0 (B5) K5F 4221L from 13(B3),25 1 L5(A) L411F 2 0020F 467F 3 46(T7) L5(B) 4 L411F 42(T6) 5 5 42(T7) 42(T5) 6 4110F L5(D4) 7 40(D5) L3(D4) 8 3219L L316F 9 3610L 2221L 10

LOC	ATION		ORDER		NOTES	PAGE 6	м 28
Abs.	Rel.	Sym.			·		
	16	6	75F S5F				
	17		505F 5017L		·	1 Mg	
1	18		26(P17) 92131	F			
	19		2221L 9259F	from 8L			
186	20		9259F 92139F			•	
	21		92707F 22F				
	22		00F 00 0000 1	000 0000J			
189	0	(18 6)	L510F 4011F	from 36(P)	Replace B w	ith C	
	1		416F 501L	from 49(P)			
	2	·	26(B2) L5(D5)		·	·	
	3		LO(D6) 408L				
	4		15(B) 1412F				
•	5		4217L 4114F				• .
	6		4115F L5(B)				
	7		429L 4213L		Carely Carely		
	8		OOF OOF	by 3L	Read row of	C from drum	
	9	14 A	40F 40F		with sum ch	e ck	
	10		F58L 408L				
	11		F59L 429L		s.		
	12		fo(T5) 368L		. *		
	13	1	4114F L5F	by 7L	Sum check f	or row at loc.	14
	14		L414F 4014F				
	15	l	F513L 4213L				
	16		IO(T10) 3213I				
	17	<u> </u>	L514F LOF	by 4L			
	18		40F L3F				
	19		3220L FF8F			f C read from c	
					incorrectly	, wh. sw. to ti	y again
	20		261L 5 020L			and the second s	
	21		26(B4) F515F	1			
	22		4215F L011F			•	
	23		3224L 226L				
	24		00F 5024L				•
	25		26(B5) 26(A1	1			

LO	CATION		ORDER		NOTES	PAGE 7	м 28
Abs .	Rel.	Sym.			; F		
215	0	(Al)	00K 50S 350L	from 13(B3),25(36) Read ro	ws of A	
	1			13(A3), 14(A4)	* 		
	2		363L 2214L				
	3		10(1) 367L				
	4		L3(D4) 325L				
	5		226L 92834F		Print "J"		a.
	6		92135F 24(P)		Stop: End o	of A; 2402L	
	7	le se	LO(1) 328L				
	8		2014L L3(D4)		Stop on F:	20 0F 5	
	9		3613L L55F	·			
	10		101F IO(1)				
	11	1	3234(P) L5(D1)				
	12	1	4016F 2234(P)				
	13		92834F 92135F		Print "J"		****
	14		2234(P) L521(I	112)			
	15		107F 40F				
	16		L3F 36(A2)				
	17		FF3F 26(P) OOK		FF3: row v	ector of A doown.sw.to new	es not co w paramet
233	0	- (A2) 4114F L5(D1)	from 16(Al)	- 1		
	1		14(D3) 10(1)				:
	2		409F F510F		tally "i" a	t loc. 10	
	3		4010F 41F				
	4		L5(C) 4227L				
	5		L5(B) 429L				
	6		4213L F59F				
	7		409F 408L				
	8		OOF OOF		Read column	of B from dr	um
	9		40F 40F				
	10	1	1581 148F				
	. 11		408L F59L				
	12		429L LO(T5)				
	13		368L L5F				
	14	·	L414F 4014F				
	15		F513L 4213L		form sum of	b _{ij} at loc.	14
<u> </u>		4					

LOCATION			ORDER		NOTES PAGE 8 M 28
Abs.	Rel.	Sym.			
	16		10(T6) 3213L		
	17		L5(A) 4620L		
	18		L5(B) 4220L		
	19		41F S5F		
253.	20		50F 74F	by 17, 18L	vector multiplication
	21		401F 3235L		
	22		L5F 3234L		
	23		L41F 3233L		
	24		40F L520L		
	25		L4(1-1) 4020L		
	26		LO(T7) 3219L		
	27		15F 40F	by 4L	store C _{ik}
	28		F527L 4227L		18
	29		LO(T8) 365L		
	30		156F 1014F		
	31		40F L3F		
	32		36 (A3) FF6F		FF6: B swm check failure;
	33		26L FF 5F		wh. sw. to try again
	34		26(P) IAIF		
	35		2624L L5F		FF5: Overflow on element
	36		363 7 L 2234L		of C; wh. sw. to read a
	37		141F 3624L		new parameter
	3 8		2233L 00F		
272	. 0	(A3)	00K 13(D4) 36(A4)	from 32(A2)	
	1		L5(C) 423L		Store row of C on drum with
	2		428L 41F		row sum check at end of each
	3		001F L5F		row.
	4		14F 40F		
	5	3	F53L 423L		
	6		10 (T 9) 323L	4.7%	
279	7		15F 40F	by 3(B2)	
	8		001F L5F		
	9		OOF OOF	by 10, 13(B5)	Store on drum
	10		F59L 409L		
	<u></u>		.		

LOCATION			ORDER	NOTES		PAGE 9	м 28
Abs.	Rel.	Sym.		·			
	11		F58L 428L				
	12		FO(T9) 328L				
	13		22 (Al) 00F				
286	0 4	(A4)	00k L5(C) 422L	from 0(A3)	Print row	of C	
	1		4114F 001F				
	2		4115F L5F	·			
	3		50F 503L	by 12(P)			
	4	·	26 (P17) F52L	DJ 12 (1)	·		•
	5		422L F514F				
	6		4214F LO12F				
·	7		3611L F515F		test: end	of row?	
	8		4215F LO(NL)				
	9		322L 92131F		test: end	of n elements	
	10		92519F 262L				
	11		92770F 92135F				
	12		92519F 22(Al)				
299		(N12)	оок		Input Rout	ine (N12)	
338		(P17)	оок (Р 17)		Print Rout	ine (Pl7)	
			00K				
397			L3F 34(P)				
398			FF7F 26(P)		FF7: Read	failure on	
399			F43691F 580478F		master tap	e.	
			26L 261N				
		}		·			
				•			•
						•	
-		1					